

Experimental review of (semi-)leptonic charm decays

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Contents

- **Introduction**
- **Data sample**
- $D_{(s)} \rightarrow l^+ v$
- $D \rightarrow K(\pi) e^+ v$
- **Other topics (D, D_s, Λ_c) at threshold**
- **Summary**

Introduction

Studies of (semi-)leptonic charm decays are important to explore weak and strong effects in charm decays

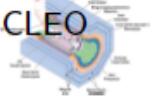
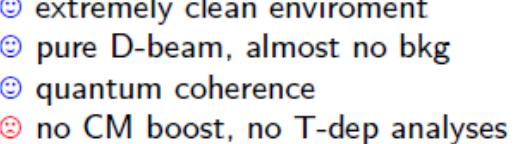
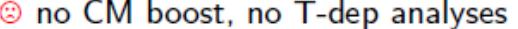
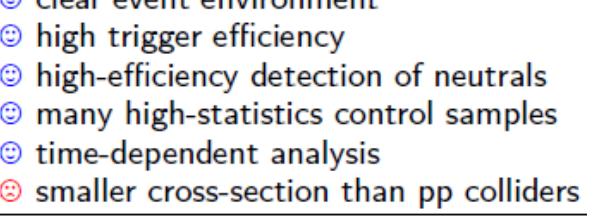
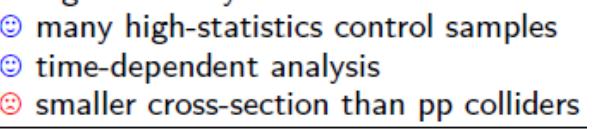
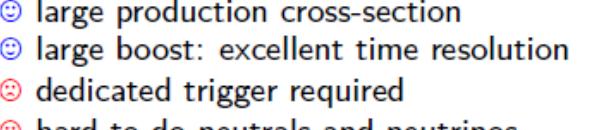
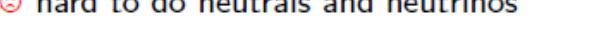
$$\Gamma(D_{(s)}^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_\ell^2 m_{D_{(s)}^+} \left(1 - \frac{m_\ell^2}{m_{D_{(s)}^+}^2}\right)^2$$

$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 |V_{cd(s)}|^2}{24\pi^3} p^3 |f_+(q^2)|^2$$

- Precise measurements of decay constants f_{D_s+} , $f_{D_{s+}}$, form factors $f_+^{D(s)\rightarrow P}(q^2)$ of semi-leptonic (SL) $D_{(s)}$ decays will calibrate LQCD calculations at higher accuracy. Once they pass experimental tests, the precisely LQCD calculated f_D/f_B , f_{D_s}/f_{B_s} and $f_+^{D\rightarrow P(0)}/f_+^{B\rightarrow P(0)}$ will be helpful for measurements in B decays
- Improved LQCD calculations on $f_{D_{(s)+}}[0.5(0.5)\%]$, $f_+^{D\rightarrow K(\pi)(0)}[2.4(4.4)\%]$ help to precisely measure the CKM matrix element $|V_{cs(d)}|$, which are important for the CKM matrix unitarity test and search for NP beyond SM
- Test on lepton flavor universality in charm sector

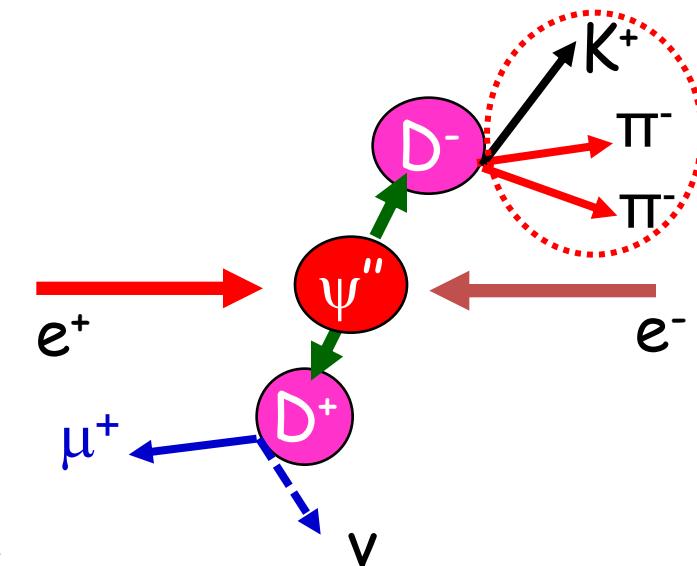
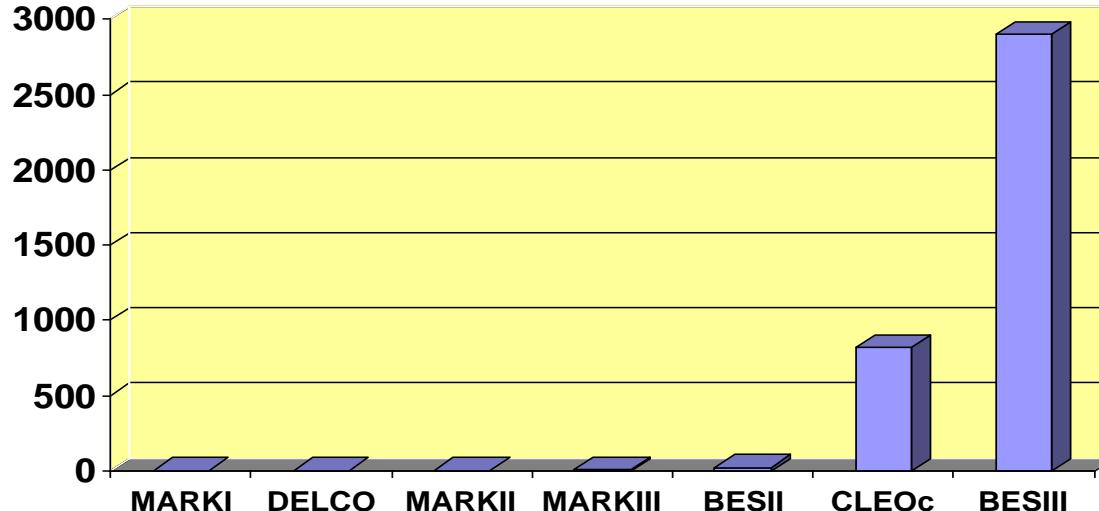
Recent $D^0(+)$, D_s^+ and Λ_c^+ samples

Taking from Longke Li's talk at joint workshop of BESIII/Belle/LHCb at Nankai

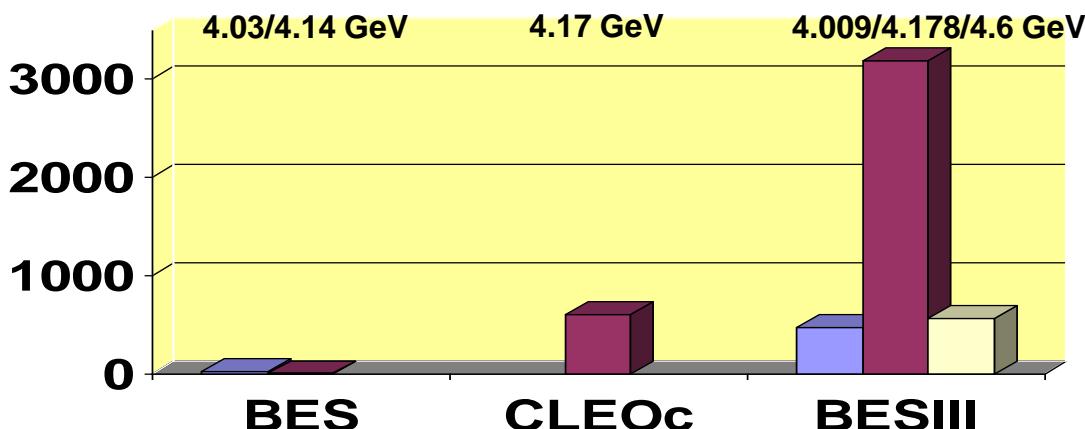
Experiment	Machine	C.M	Lumin.	$N(D)$	efficiency	advantage/disadvantage
	CLEO (e^+e^-)	3.77 GeV	0.8 fb^{-1}	2.9×10^6	$\sim 10\text{-}30\%$	
		4.17 GeV	0.6 fb^{-1}	$2.3 \times 10^6 (D^\pm)$		
	BEPC-II (e^+e^-)	3.77 GeV	2.92 fb^{-1}	0.6×10^6		
		4.18 GeV	3 fb^{-1}	10.5×10^6		
	4.6 GeV	D_s^+	8.4×10^6	$3 \times 10^6 D^0(+)$		
		Λ_c^+	0.567 fb^{-1}	\star		
	KEKB (e^+e^-)	10.58 GeV	1 ab^{-1}	1.3×10^9		
	PEP-II (e^+e^-)	10.58 GeV	0.5 ab^{-1}	6.5×10^8		
				$\star\star$		
	Tevatron ($p\bar{p}$)	1.96 TeV	9.6 fb^{-1}	1.3×10^{11}		
	LHC (pp)	7 TeV	1.0 fb^{-1}	5.0×10^{12}		
	8 TeV	2.0 fb^{-1}			\star	

Charm samples (pb^{-1}) at threshold

➤ $D^0(+) \text{ samples}$



➤ $D_s^+/D_s^+/\Lambda_c^+ \text{ samples}$



$$N_{\text{ST}}^i = 2 \times N_{\bar{D}\bar{D}} \times B_{\text{ST}}^i \times \epsilon_{\text{ST}}^i$$

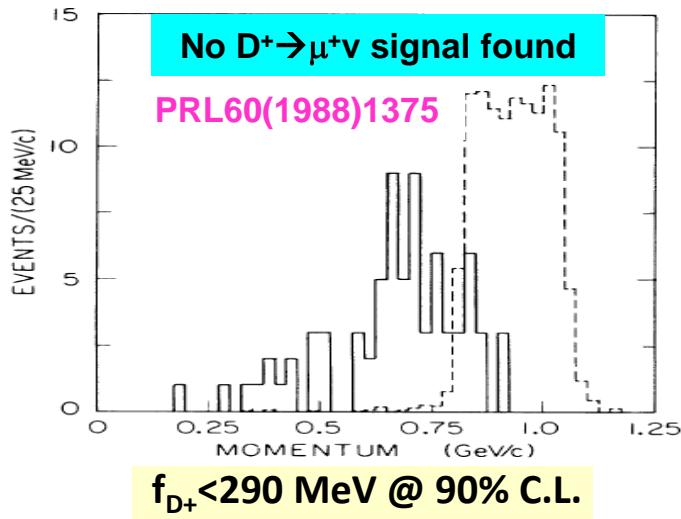
$$N_{\text{DT}}^i = 2 \times N_{\bar{D}\bar{D}} \times B_{\text{ST}}^i \times B_{\text{sig}} \times \epsilon_{\text{ST vs.sig}}^i$$

$$B_{\text{sig}} = \frac{N_{\text{DT}}^{\text{tot}}}{N_{\text{ST}}^{\text{tot}} \times \epsilon_{\text{sig}}}$$

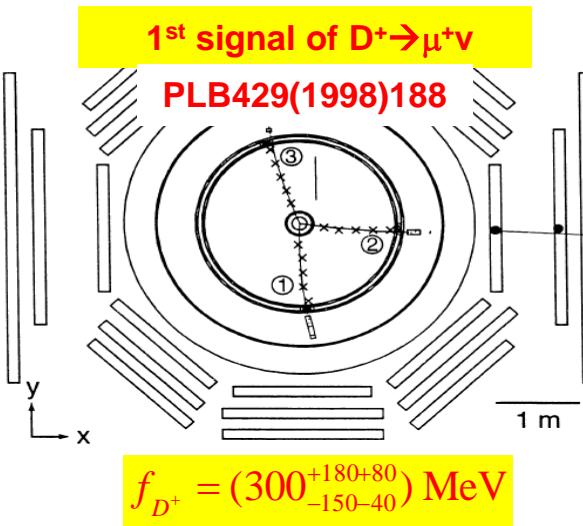
$$\bar{\epsilon}_{\text{sig}} = \sum_{i=1}^N (N_{\text{ST}}^i \times \epsilon_{\text{ST vs.sig}}^i / \epsilon_{\text{ST}}^i) / \sum_{i=1}^N N_{\text{ST}}^i$$

Earlier searches or measurements of f_{D+}

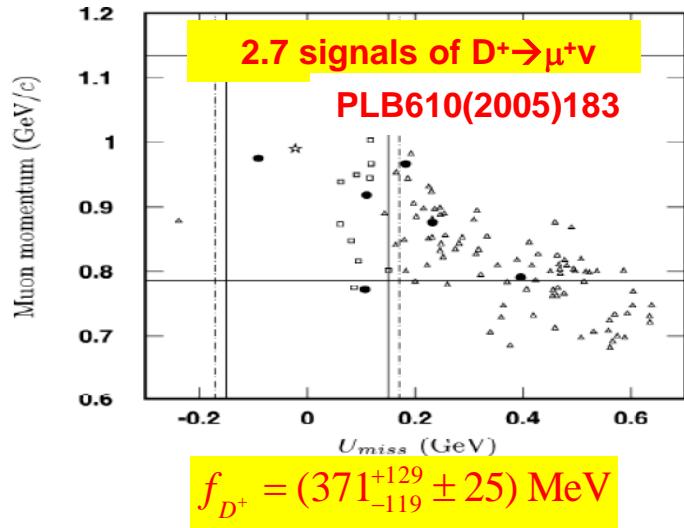
■ MARKIII, 9.6 pb⁻¹ at ψ''



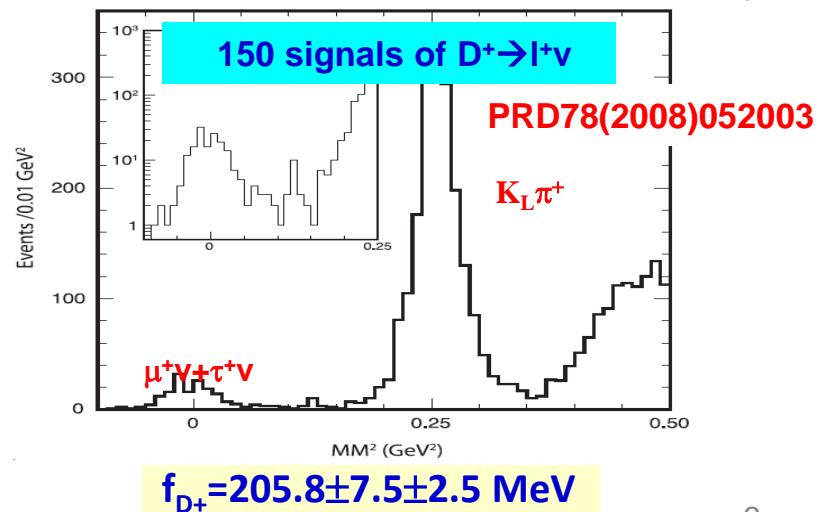
■ BESI, 22.3 pb⁻¹ at 4.03 GeV



■ BESII, 33 pb⁻¹ data at ψ''



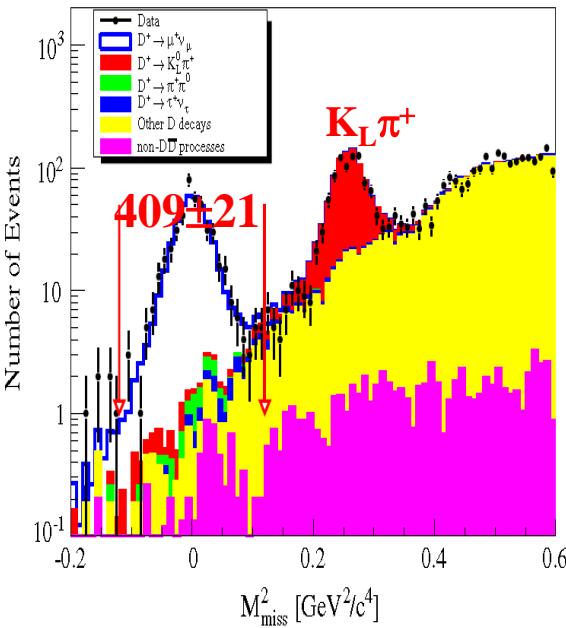
■ 2004-2008, CLEO-c, 818 pb⁻¹ at ψ''



Results on $B[D^+ \rightarrow l^+ v]$, $f_{D^+} |V_{cd}|$

2.93 fb^{-1} data@ 3.773 GeV

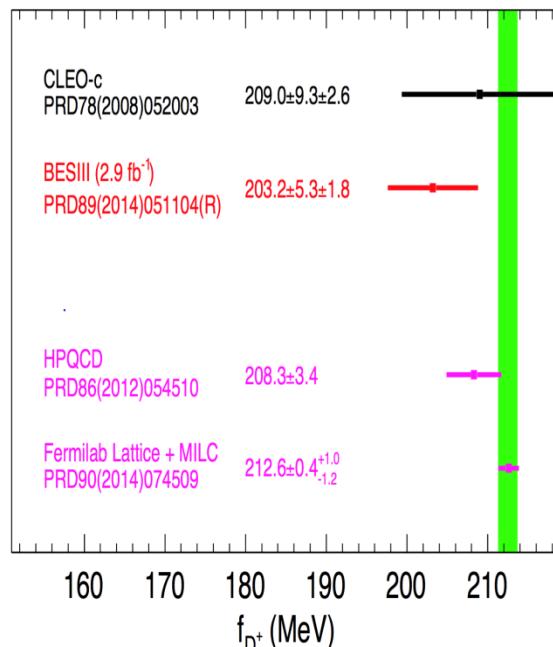
BESIII, PRD89(2014)051104R



$$B_{D^+ \rightarrow \mu^+ \bar{\nu}} = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

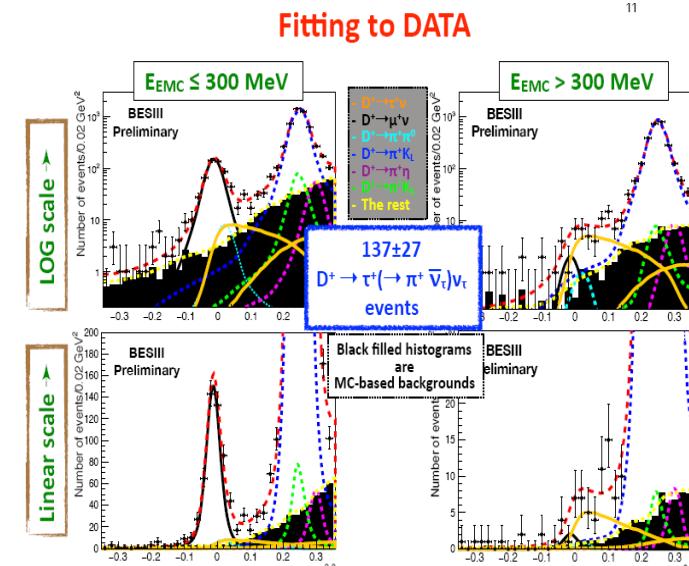
$$f_{D^+} = (203.2 \pm 5.3 \pm 1.8) \text{ MeV}$$

$$|V_{cd}| = 0.2210 \pm 0.0058 \pm 0.0047$$



20 fb^{-1} data can reduce the statistical error of f_{D^+} to 1%

Evidence of $D^+ \rightarrow \tau^+ \bar{\nu}$



$$B[D^+ \rightarrow \tau^+ \bar{\nu}] = (1.20 \pm 0.24_{\text{stat.}}) \times 10^{-3}$$

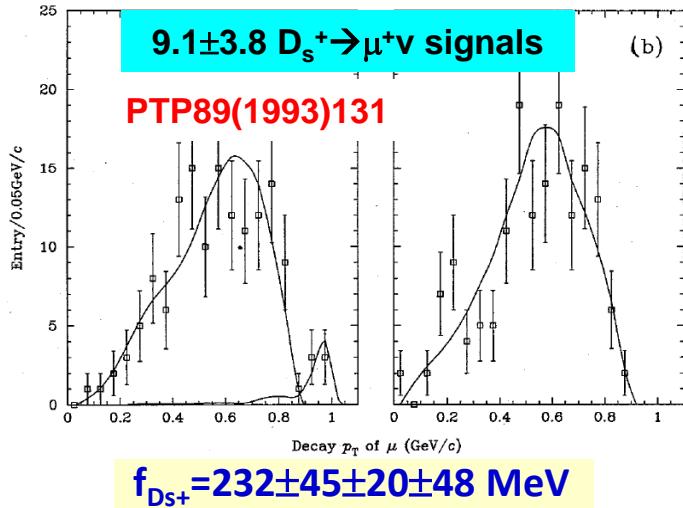
$$R \equiv \frac{\Gamma(D^+ \rightarrow \tau^+ \bar{\nu})}{\Gamma(D^+ \rightarrow \mu^+ \bar{\nu})} = \frac{m_{\tau^+}^2 \left(1 - \frac{m_{\tau^+}^2}{M_{D^+}^2}\right)^2}{m_{\mu^+}^2 \left(1 - \frac{m_{\mu^+}^2}{M_{D^+}^2}\right)^2}$$

SM prediction: 2.66

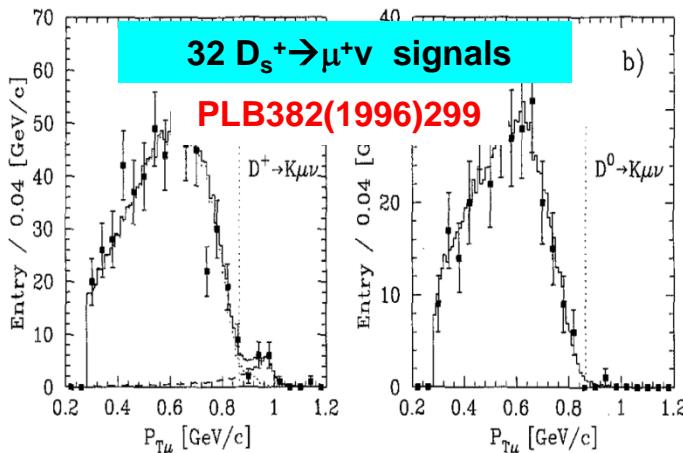
BESIII: 3.21 ± 0.64

Earlier measurements of $f_{D_s^+}$

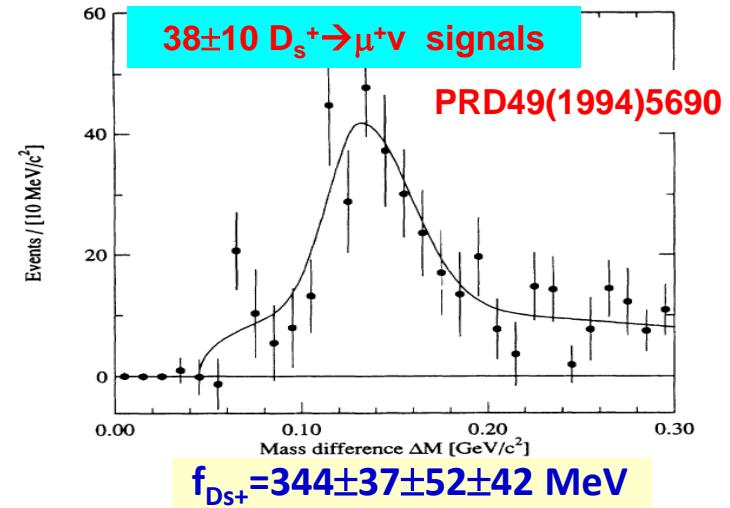
■ WA75, Fixed target experiment



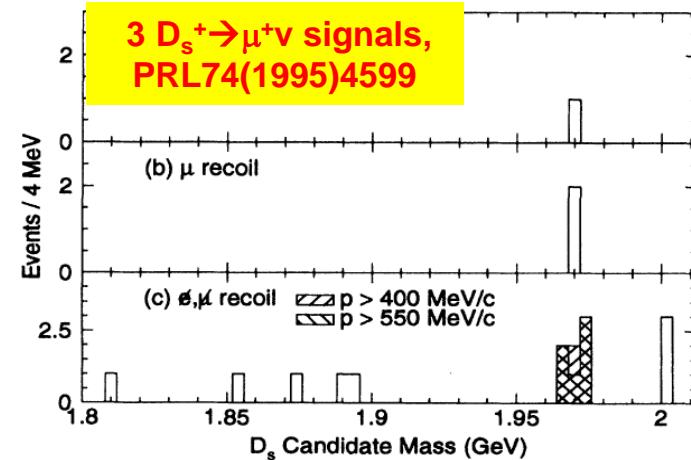
■ E653, Fermilab fixed target experiment



■ CLEOII, 2.13 fb $^{-1}$ at 10.6 GeV

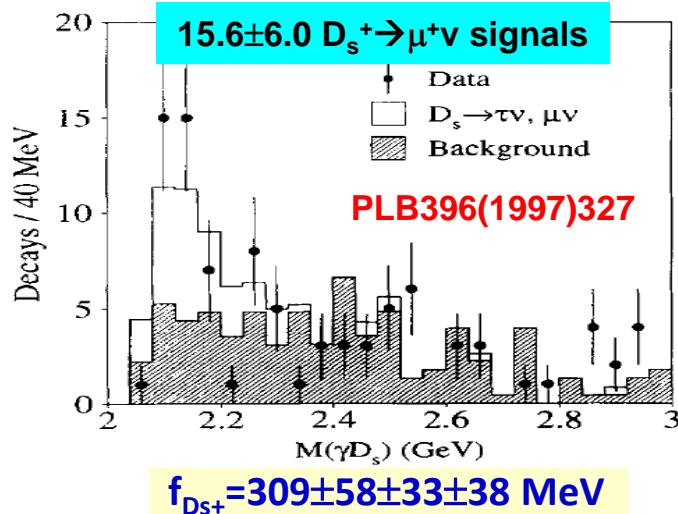


■ BESI, 22.3 pb $^{-1}$ at 4.03 GeV

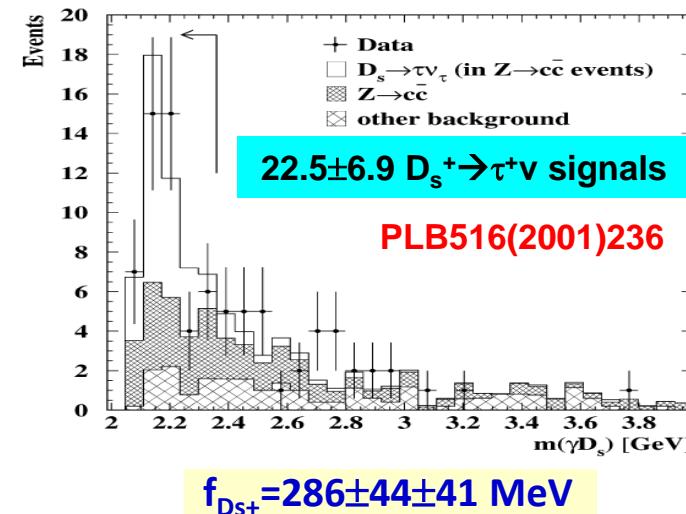


Earlier measurements of $f_{D_{s+}}$

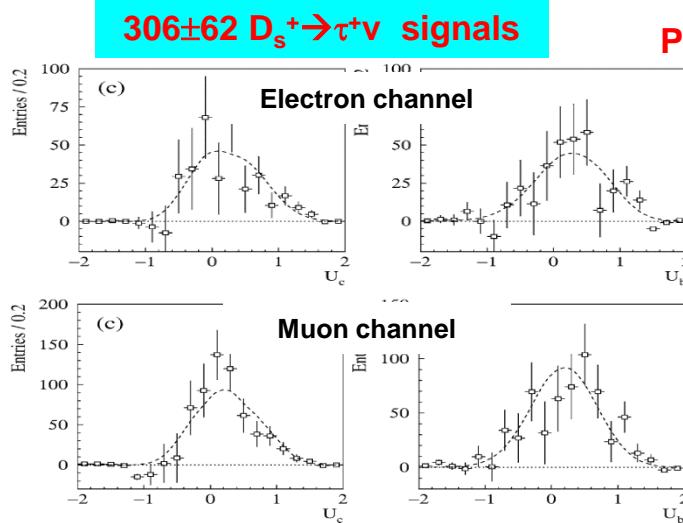
■ L3, $Z \rightarrow q\bar{q}$, 49.6 pb^{-1} at 91.2 GeV



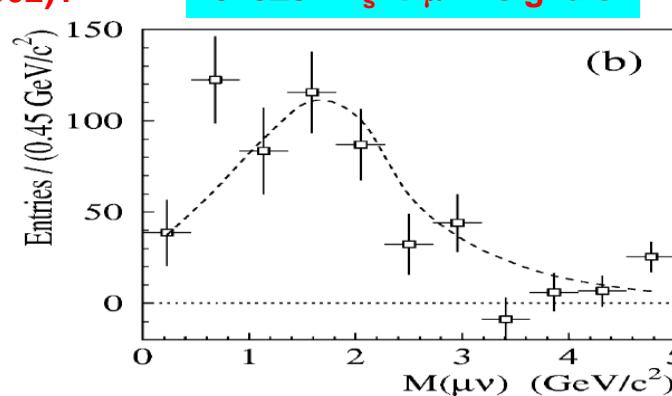
■ OPAL, $3.9 \times 10^6 e^+e^- \rightarrow q\bar{q}$



■ ALPHA, $3.97 \times 10^6 Z$ hadronic decay



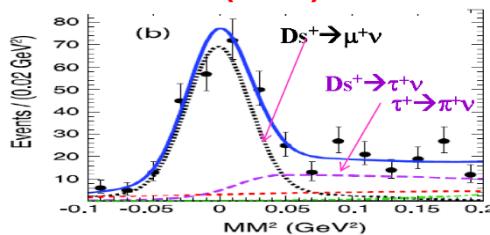
PLB528(2002)1



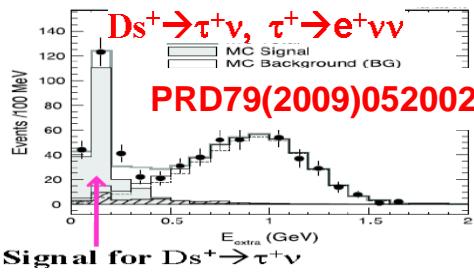
Results of $f_{D_s^+}$ at CLEO/Belle/BaBar

- $D_s^{*+}D_s^-$, 600 pb $^{-1}$
@ 4.17 GeV [697 I+v]

PRD79(2009)052001

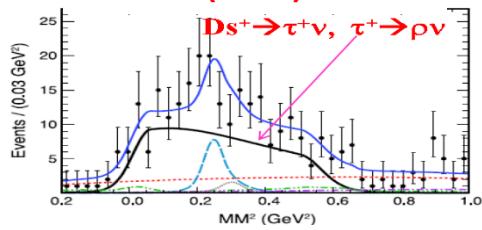


$$f_{D_s^+} = 263.3 \pm 8.2 \pm 1.9 \text{ MeV}$$



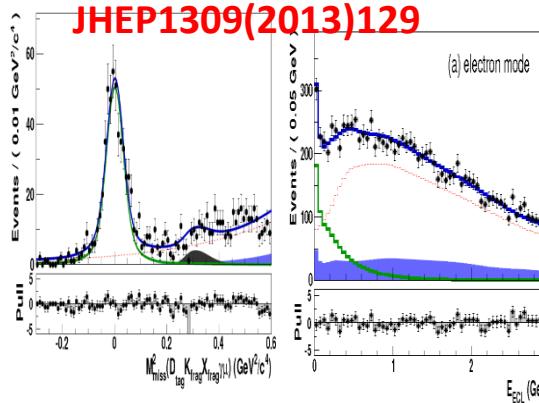
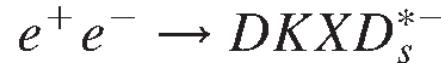
$$f_{D_s^+} = 252.2 \pm 11.1 \pm 5.2 \text{ MeV}$$

PRD80(2009)112004



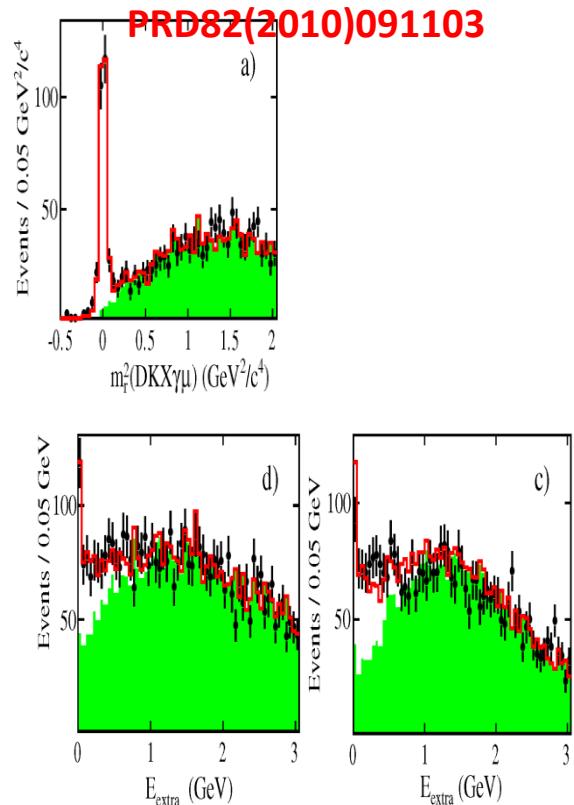
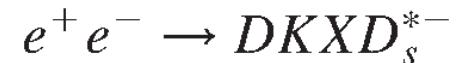
$$f_{D_s^+} = 257.8 \pm 13.3 \pm 5.2 \text{ MeV}$$

- Belle, 913 fb $^{-1}$ at 10.58 GeV [2698 I+v]



$$f_{D_s^+} = 255.5 \pm 4.2 \pm 5.1 \text{ MeV}$$

- Babar, 521 fb $^{-1}$ at 10.58 GeV [1023 I+v]

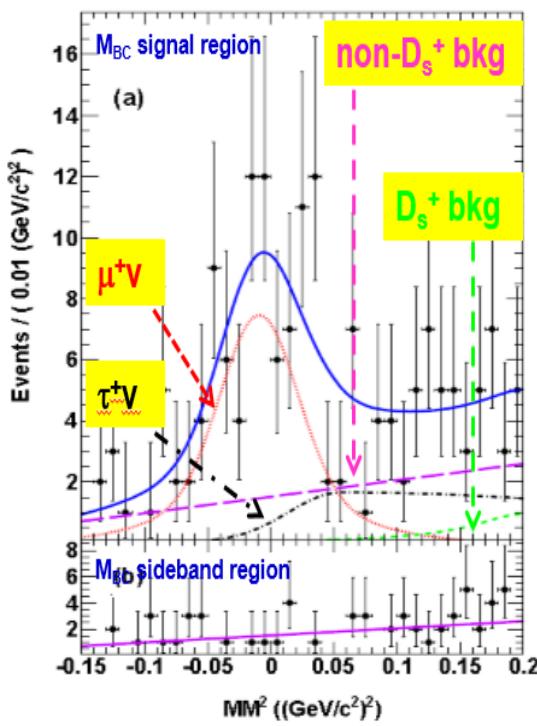


$$f_{D_s^+} = 258.6 \pm 6.4 \pm 7.5 \text{ MeV}$$

Results on $B[D_s^+ \rightarrow \mu^+ v]$, $f_{D_{s+}} |V_{cs}|$ at BESIII

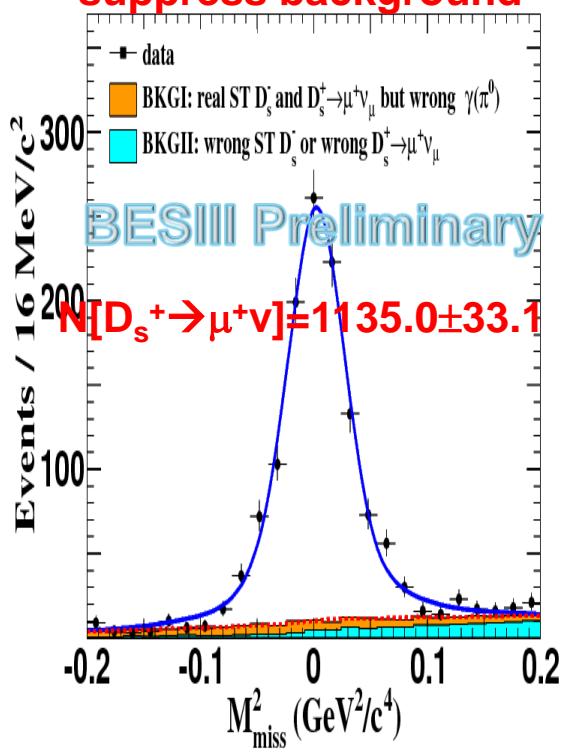
0.48 fb^{-1} data@4.01 GeV

PRD94(2016)072004



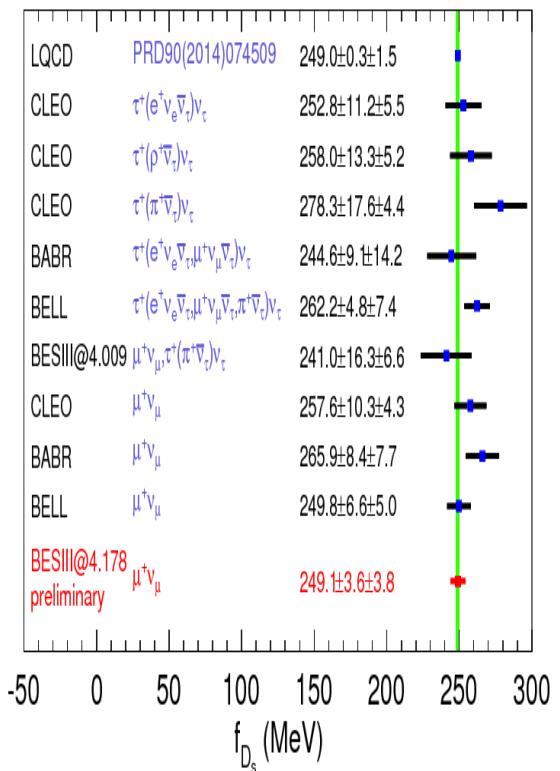
3.19 fb^{-1} data@4.178 GeV

Use μ counter to suppress background



$$f_{D_{s+}} = (241.0 \pm 16.3 \pm 6.6) \text{ MeV}$$

$$f_{D_s} |V_{cs}| = 242.5 \pm 3.5 \pm 3.7 \text{ MeV}$$

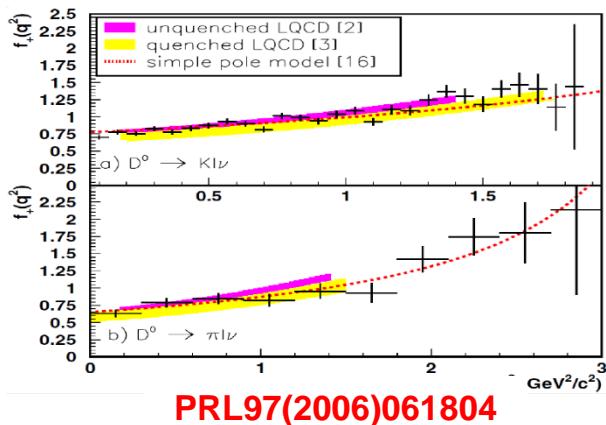


Precision on $f_{D_{s+}}$ reach 2%. Combining $\tau^+ v$ can reduce it to 1.5%

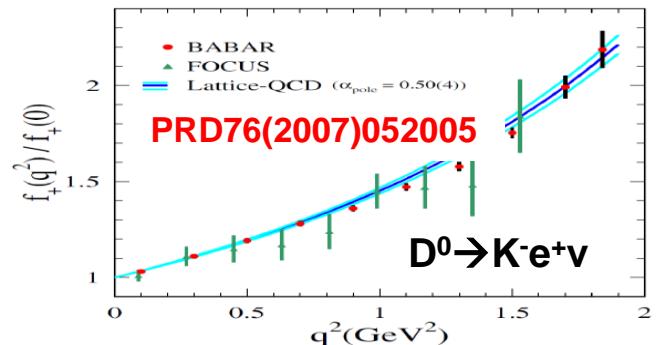
Previous measurements of $f_D^{\pi}(0)|V_{cs(d)}|$

In the past 30 years, studies of $D \rightarrow K(\pi)l^+\nu$ were made by MARKIII, E691, CLEO, CLEOII, BESII, FOCUS, **BELLE**, Babar and CLEO-c

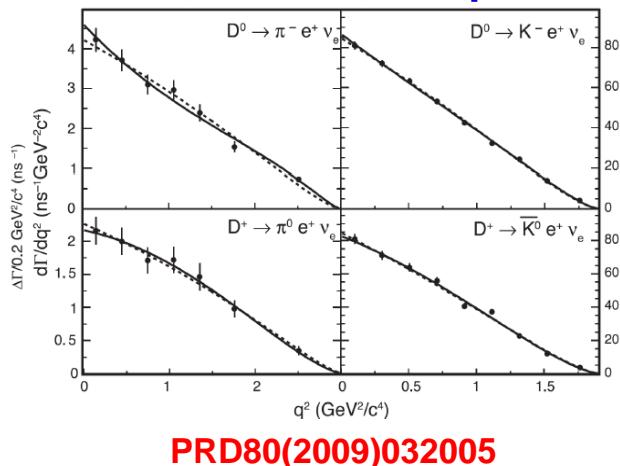
■ BELLE, 282 fb^{-1} at 10.58 GeV



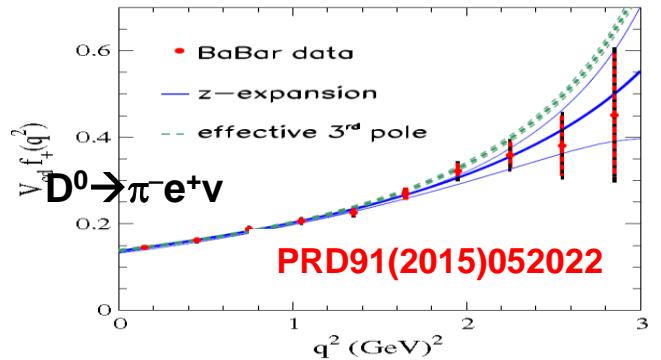
■ Babar, 75 fb^{-1} at 10.58 GeV



■ 2004-2009, CLEO-c, 818 pb^{-1} at ψ''



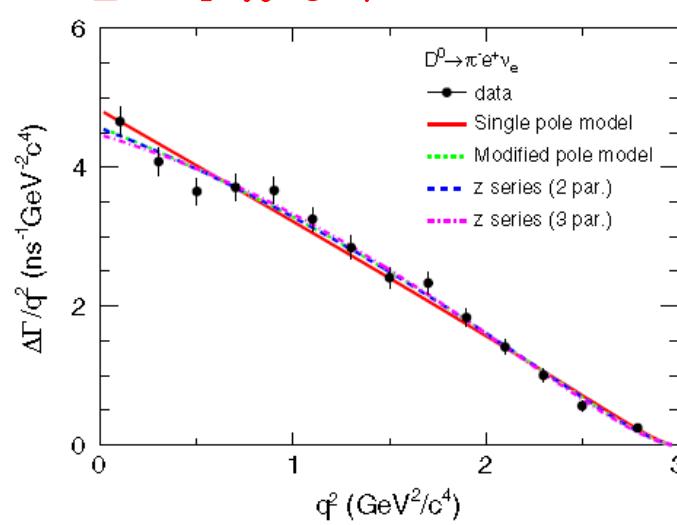
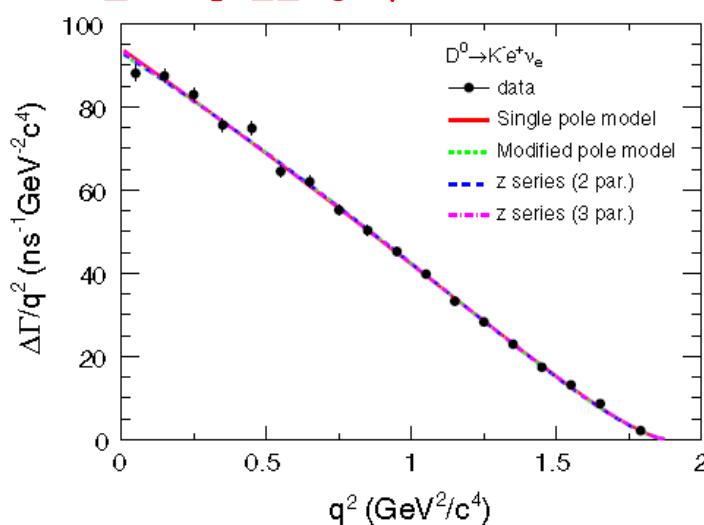
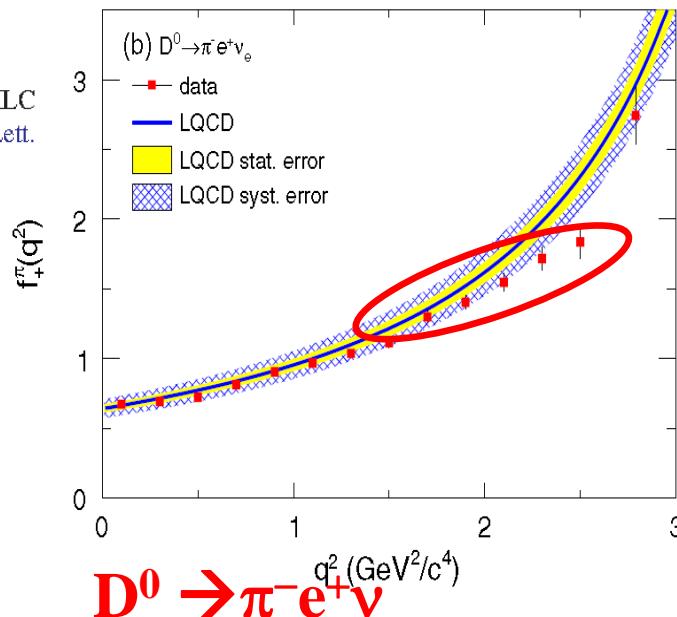
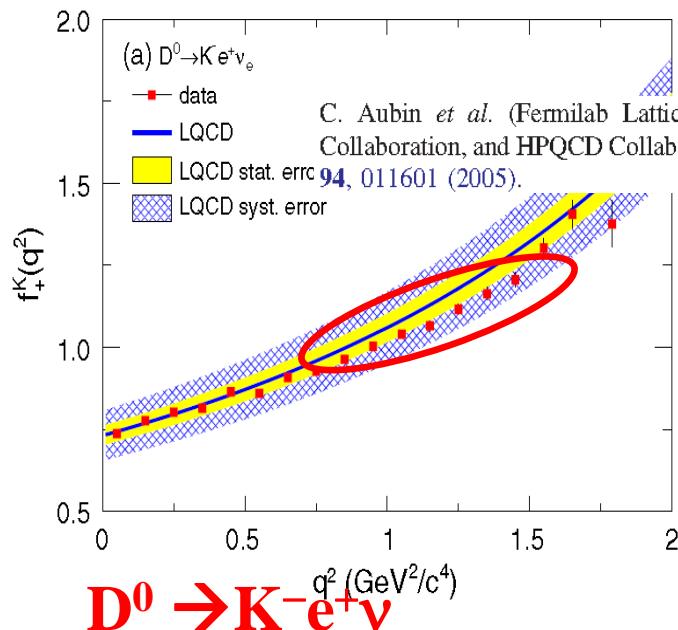
■ Babar, 347.2 fb^{-1} at 10.58 GeV



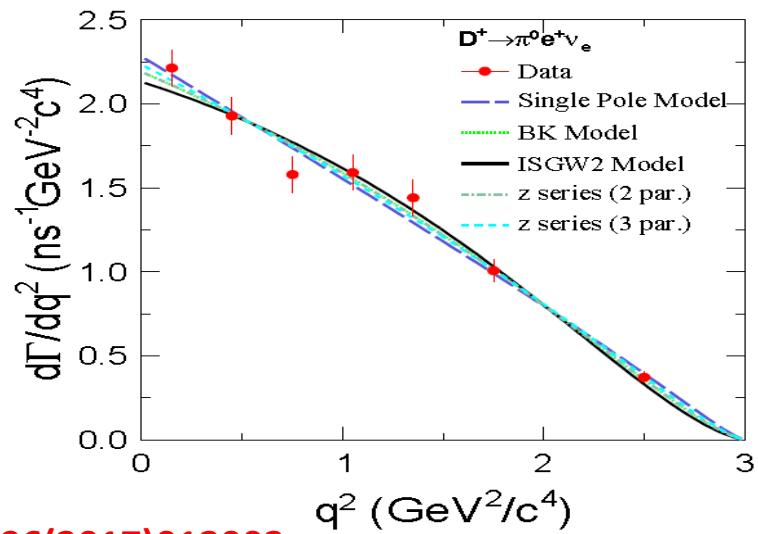
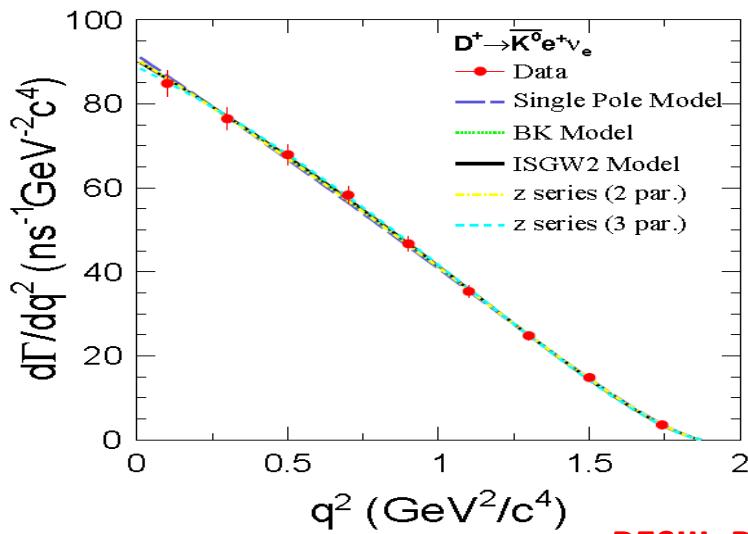
Before 2010, the LQCD calculated $f_D^{\pi}(0)|V_{cs(d)}|$ precision is at 10% level, thus limiting $|V_{cs(d)}|$ measurement

Impact of $f^D \rightarrow K(\pi)(q^2)$ on LQCD

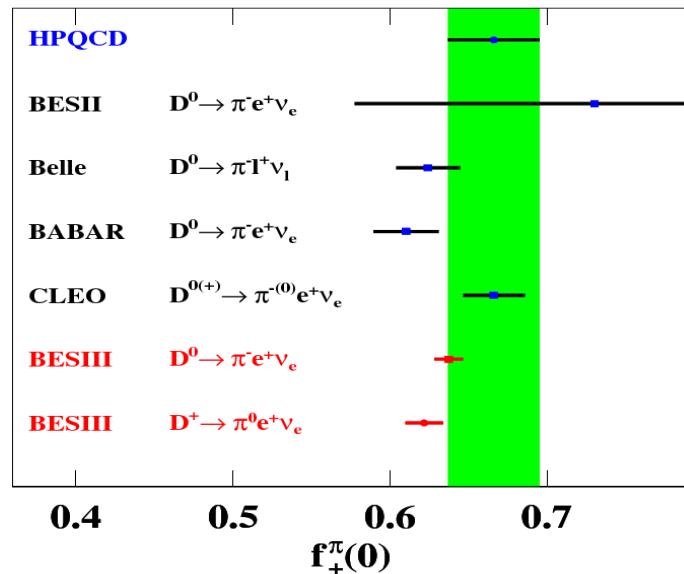
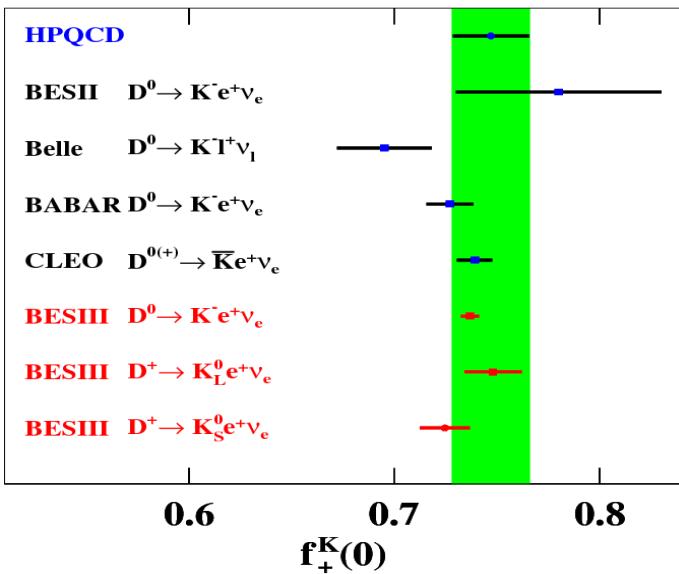
BESIII, PRD92(2015)072012



Comparisons of $f^D \rightarrow K(\pi)(0)$ with LQCD



BESIII, PRD96(2017)012002



Comparisons of the measured $|V_{cs(d)}|$

■ Method 1

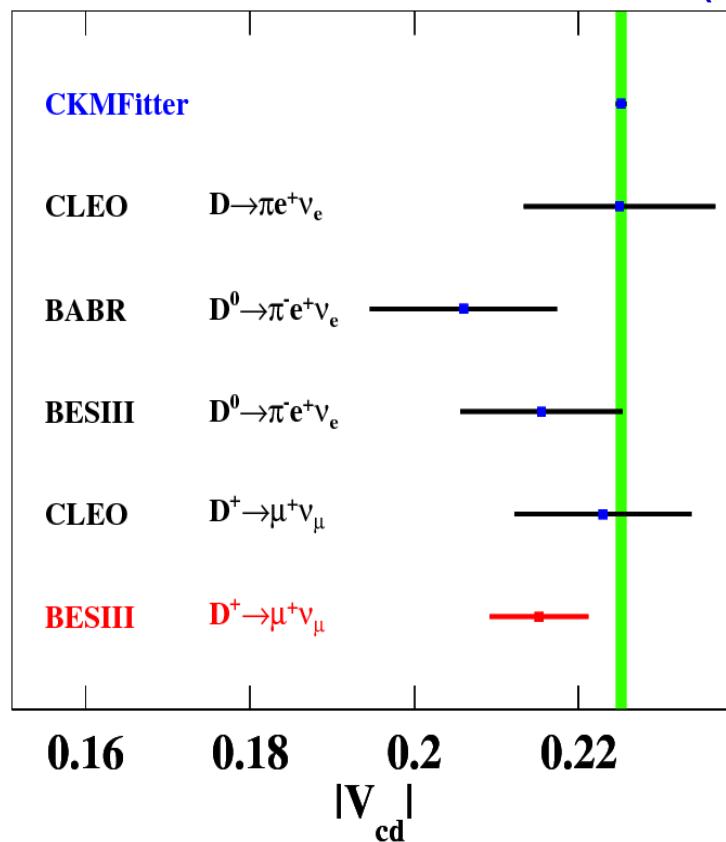
$$f_{D(s)} |V_{cd(s)}|$$

■ Method 2

$$f^{D \rightarrow K(\pi)}(0) |V_{cs(d)}|$$

■ Method 3

$$f^{D(s) \rightarrow \eta}(0) |V_{cd(s)}|$$

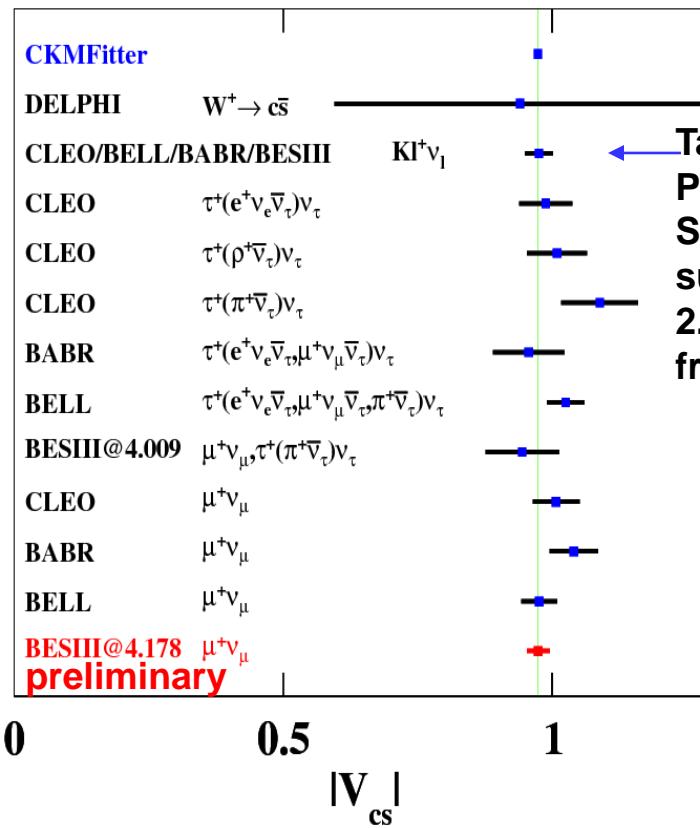


$$|V_{cd(s)}|$$

$$|V_{cs(d)}|$$

$$|V_{cd(s)}|$$

Limited by both statistics and LQCD input



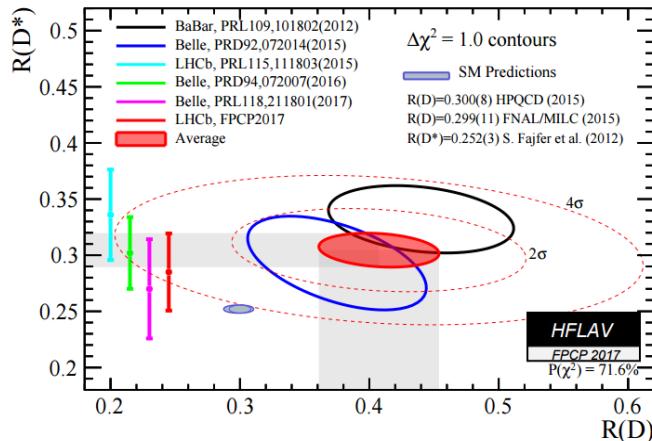
Taken from PDG, and the SL method suffers about 2.4% error from LQCD

Further improved LQCD calculations on $f_{D(s) \rightarrow P}(0)$ will improve the measurement of $|V_{cs(d)}|$ with much improved precision

LFU test in CS decay $D^{0(+)} \rightarrow \pi l^+ \nu$ at BESIII

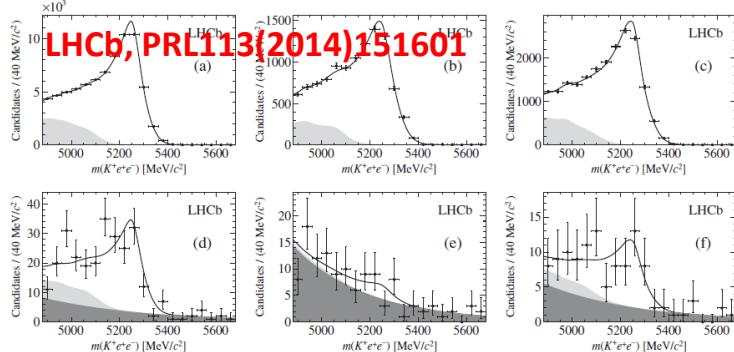
Evidence of violation of LFU at 4σ in

$$R(D^{(*)}) = \frac{B(B \rightarrow D^{(*)} \tau \nu)}{B(B \rightarrow D^{(*)} l \nu)}$$



Evidence at 2.6σ in FCNC decays $B^+ \rightarrow K^+ \mu^+ \mu^- / K^+ e^+ e^-$

$$R_K = \frac{\Gamma(\bar{B} \rightarrow \bar{K} \mu^+ \mu^-)}{\Gamma(\bar{B} \rightarrow \bar{K} e^+ e^-)} = 0.745^{+0.090}_{-0.074} \pm 0.036$$

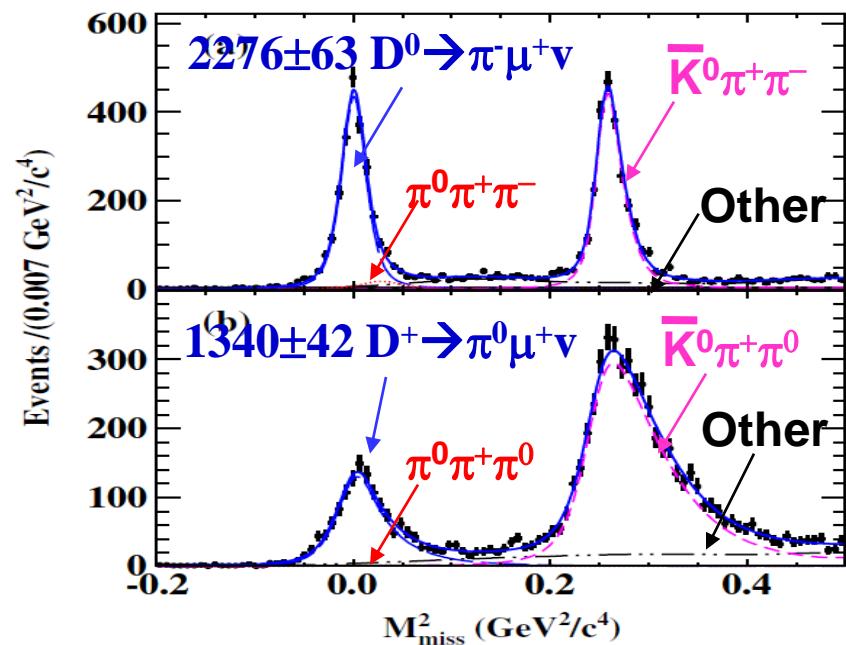


$$R_{LU}^{0(+)} = \frac{B(D^{0(+)} \rightarrow \pi^{-0} \mu^+ \nu)}{B(D^{0(+)} \rightarrow \pi^{-0} e^+ \nu)} \sim 0.97$$

$$\mathbf{B^{PDG16}:} \quad R_{LU}^0 = 0.82 \pm 0.08 \quad (\sim 2.0\sigma)$$

$$B(D^0 \rightarrow \pi^- \mu^+ \nu) = (0.237 \pm 0.024)\%$$

BESIII, arXiv:1802.05492



$$B[D^0 \rightarrow \pi \mu^+ \nu] = (0.267 \pm 0.007 \pm 0.007)\%$$

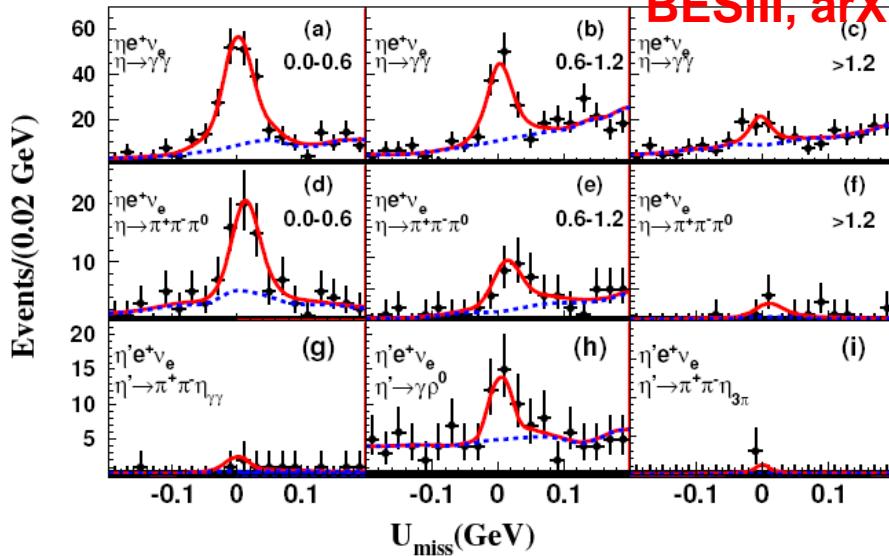
$$B[D^+ \rightarrow \pi^0 \mu^+ \nu] = (0.342 \pm 0.011 \pm 0.010)\%$$

$$\mathcal{R}_{LU}^0 = 0.905 \pm 0.027_{\text{stat.}} \pm 0.023_{\text{syst.}}$$

$$\mathcal{R}_{LU}^+ = 0.942 \pm 0.037_{\text{stat.}} \pm 0.027_{\text{syst.}} \quad 16$$

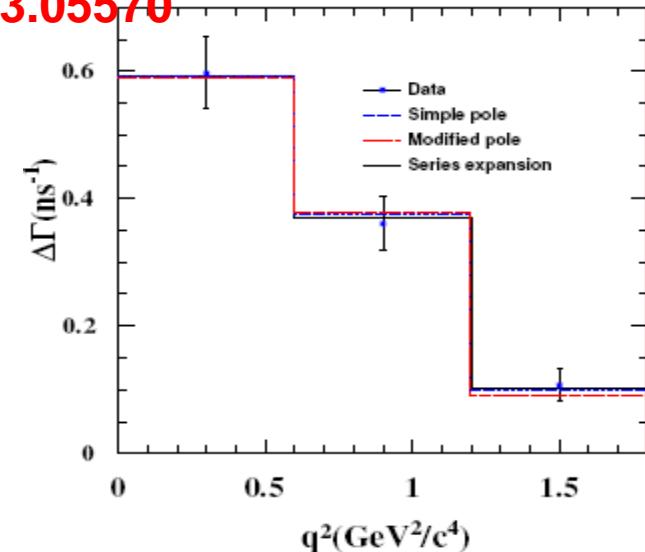
Study of $D^+ \rightarrow \eta(\eta') e^+ \nu_e$ at BESIII

BESIII, arXiv:1803.05570



$$\mathcal{B}_{\eta e^+ \nu_e} = (10.74 \pm 0.81 \pm 0.51) \times 10^{-4}$$

$$\mathcal{B}_{\eta' e^+ \nu_e} = (1.91 \pm 0.51 \pm 0.13) \times 10^{-4}$$



$$\frac{d\Gamma(D^+ \rightarrow \eta e^+ \nu_e)}{dq^2} = \frac{G_F^2 |V_{cd}|^2}{24\pi^3} |\vec{p}_\eta|^3 |f_+(q^2)|^2$$

Fit parameters	Simple pole	Modified pole	Series expansion
$f_+(0) V_{cd} (\times 10^{-2})$	$8.15 \pm 0.45 \pm 0.18$	$8.24 \pm 0.51 \pm 0.22$	$7.86 \pm 0.64 \pm 0.21$
Shape parameter	$1.73 \pm 0.17 \pm 0.03$	$0.50 \pm 0.54 \pm 0.08$	$-7.33 \pm 1.69 \pm 0.40$
ρ	0.80	-0.85	0.90
χ^2/ndf	$0.1/(3-2)$	$0.3/(3-2)$	$0.5/(3-2)$

BFs help to constrain gluon component

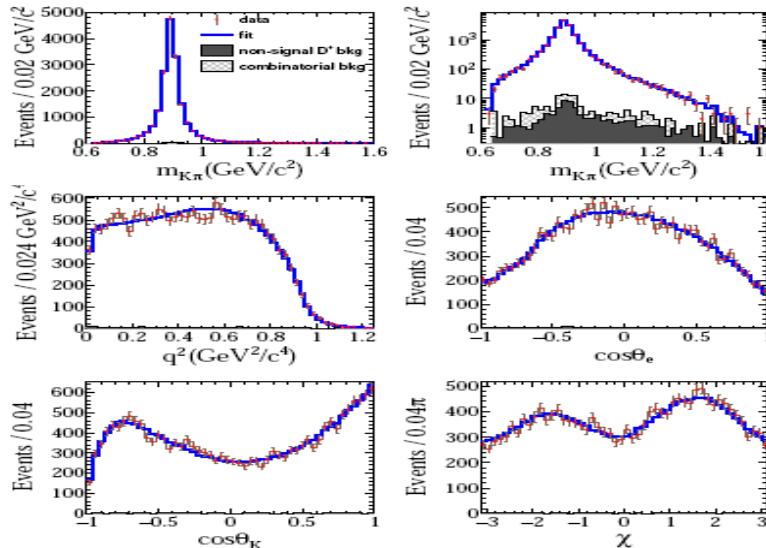
$$\begin{pmatrix} \eta \\ \eta' \\ G \end{pmatrix} = \begin{pmatrix} \cos \phi' & -\sin \phi' & 0 \\ \sin \phi' \cos \phi_G & \cos \phi' \cos \phi_G & \sin \phi_G \\ -\sin \phi' \sin \phi_G & -\cos \phi' \sin \phi_G & \cos \phi_G \end{pmatrix} \begin{pmatrix} \eta_q \\ \eta_s \\ g \end{pmatrix}$$

Combining CLEO's BFs and taking input value by EPJC69,133 and NPPS162, 312, the $\eta-\eta'$ mixing angle is determined to be
 $\phi_P = (40 \pm 3_{\text{experiment}} \pm 3_{\text{theory}})^0$

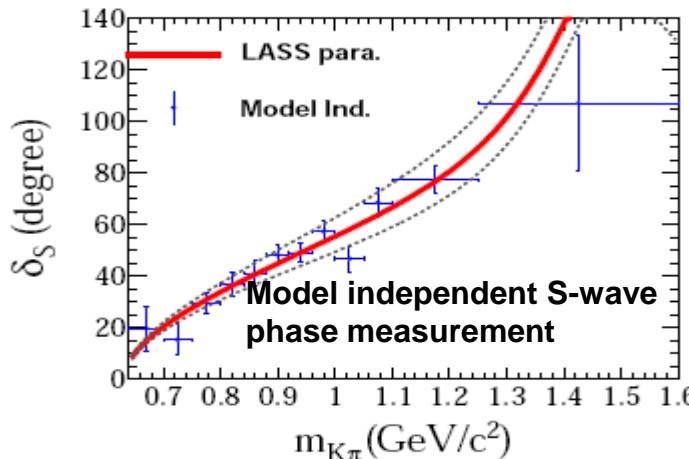
Other topics: D \rightarrow Ve $^+$ v at BESIII

BESIII,PRD94(2016)032001

D $^+$ \rightarrow K $^-\pi^+e^+\nu$

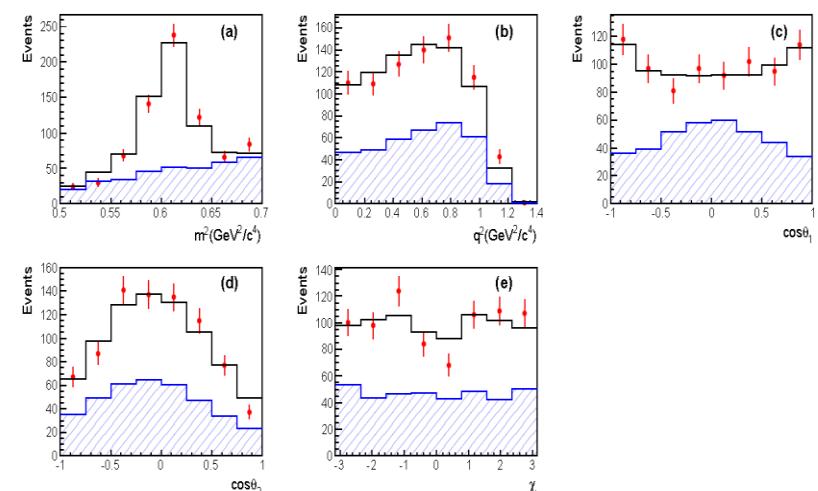
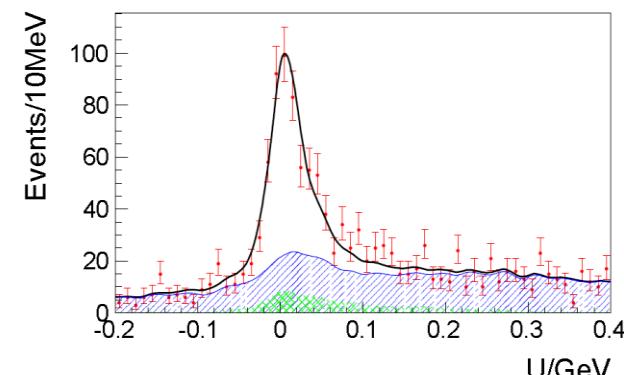


Model independent form factors



BESIII,PRD92(2015)071101(RC)

D $^+$ \rightarrow omega e $^+$ nu



$$r_V = V(0)/A_1(0) = 1.24 \pm 0.09 \pm 0.06$$

$$r_2 = A_2(0)/A_1(0) = 1.06 \pm 0.15 \pm 0.05$$

Observation of $D \rightarrow S e^+ \nu$ at BESIII

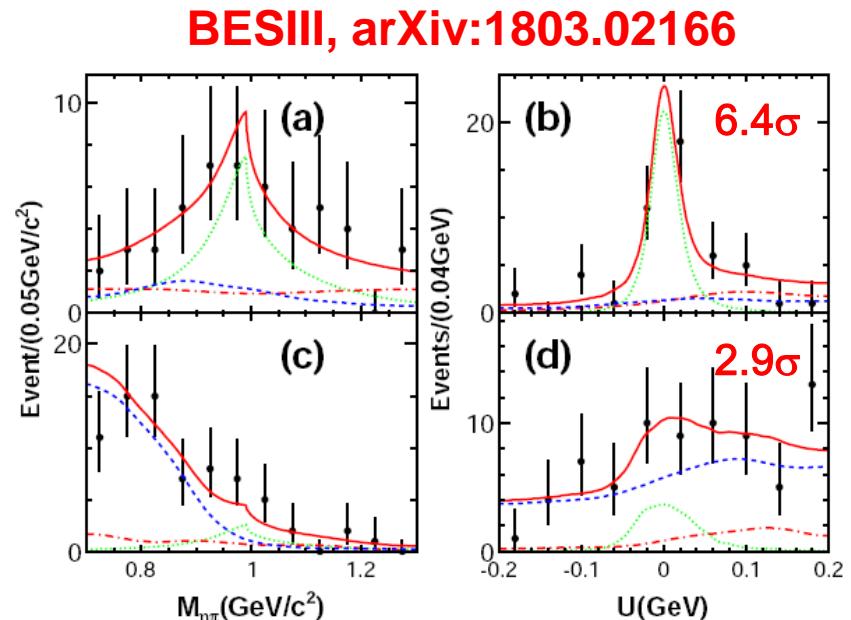
- Explore the nontrivial internal structure of light hadron mesons, traditional $q\bar{q}$ states, tetra quark system.
- With chiral unitarity approach in the coupled channels, BF is predicted to be order of $5(6) \times 10^{-5}$ for $D^0(+) \rightarrow S e^+ \nu$ decays
- Improve understanding of classification of light scalar mesons

$$R \equiv \frac{B(D^+ \rightarrow f_0 l^+ \nu) + B(D^+ \rightarrow \sigma l^+ \nu)}{B(D^+ \rightarrow a_0 l^+ \nu)}$$

$R=1(3)$ if traditional $q\bar{q}$ (tetra quark) system

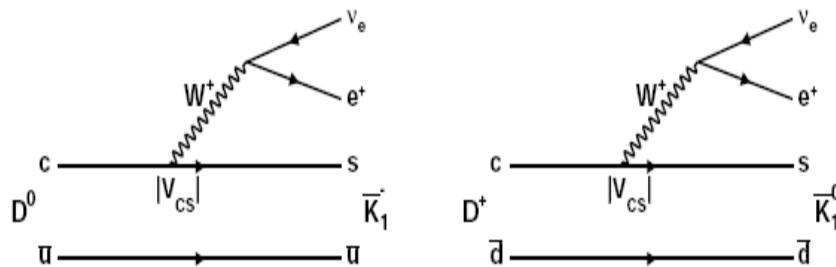
$$\begin{aligned} \mathcal{B}(D^+ \rightarrow a_0(980)^0 e^+ \nu_e) \times \mathcal{B}(a_0(980)^0 \rightarrow \eta \pi^0) \\ = (1.66^{+0.81}_{-0.66} \pm 0.11) \times 10^{-4}, \quad < 3.0 \times 10^{-4} \text{ at the } 90\% \text{ C.L.} \end{aligned}$$

$$\begin{aligned} \mathcal{B}(D^0 \rightarrow a_0(980)^- e^+ \nu_e) \times \mathcal{B}(a_0(980)^- \rightarrow \eta \pi^-) \\ = (1.33^{+0.33}_{-0.29} \pm 0.09) \times 10^{-4} \end{aligned}$$



$$\frac{\Gamma(D^0 \rightarrow a_0(980)^- e^+ \nu_e)}{\Gamma(D^+ \rightarrow a_0(980)^0 e^+ \nu_e)} = 2.03 \pm 0.95 \pm 0.06 \quad 19$$

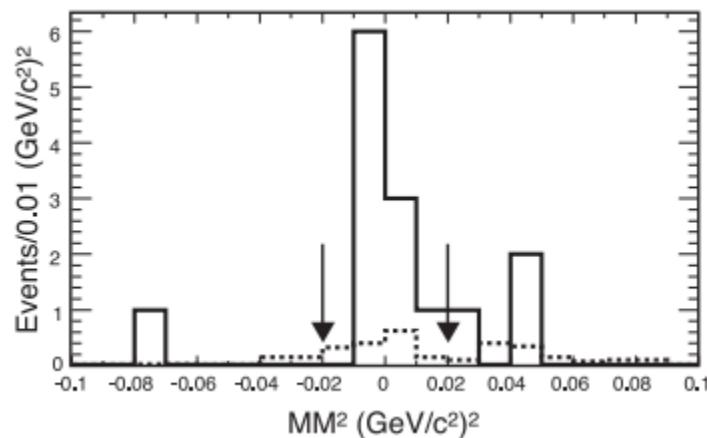
Evidence of $D \rightarrow A e^+ \nu$ at CLEO



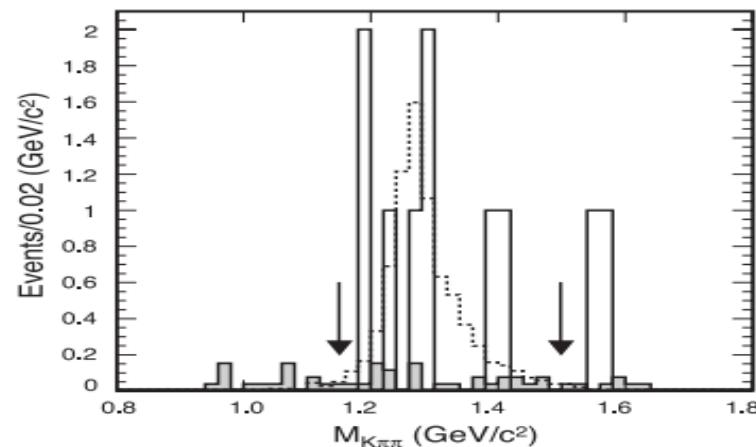
EPJC77(2017)587/863

D^+ decay	$D \rightarrow K_1(1270)$	$D \rightarrow K_1(1400)$
Theory (10^{-5})	320 ± 40	{0.5, 2.0}

CLEO, PRL(2007)191801



with 281 pb⁻¹ data@3.773 GeV



$$\mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^- e^+ \nu_e) = [2.8^{+1.4}_{-1.1}(\text{stat}) \pm 0.3(\text{syst})] \times 10^{-4}$$

$$\mathcal{B}(D^0 \rightarrow K_1^-(1270) e^+ \nu_e) \times \mathcal{B}(K_1^-(1270) \rightarrow K^- \pi^+ \pi^-) = [2.5^{+1.3}_{-1.0}(\text{stat}) \pm 0.2(\text{syst})] \times 10^{-4}$$

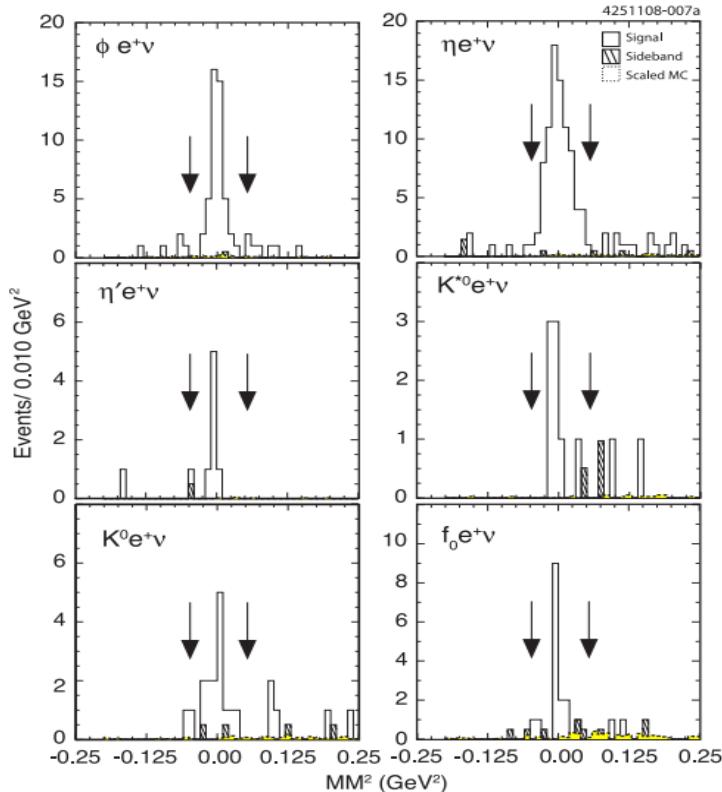
$$\text{Using } \mathcal{B}(K_1^-(1270) \rightarrow K^- \pi^+ \pi^-) = (33 \pm 3)\%$$

$$\mathcal{B}(D^0 \rightarrow K_1^-(1270) e^+ \nu_e) = [7.6^{+4.1}_{-3.0}(\text{stat}) \pm 0.6(\text{syst}) \pm 0.7] \times 10^{-4}$$

BFs of SL D_s^+ decays at CLEO

CLEO, PRD80(2009)052007

with 310 pb^{-1} data@4.17 GeV

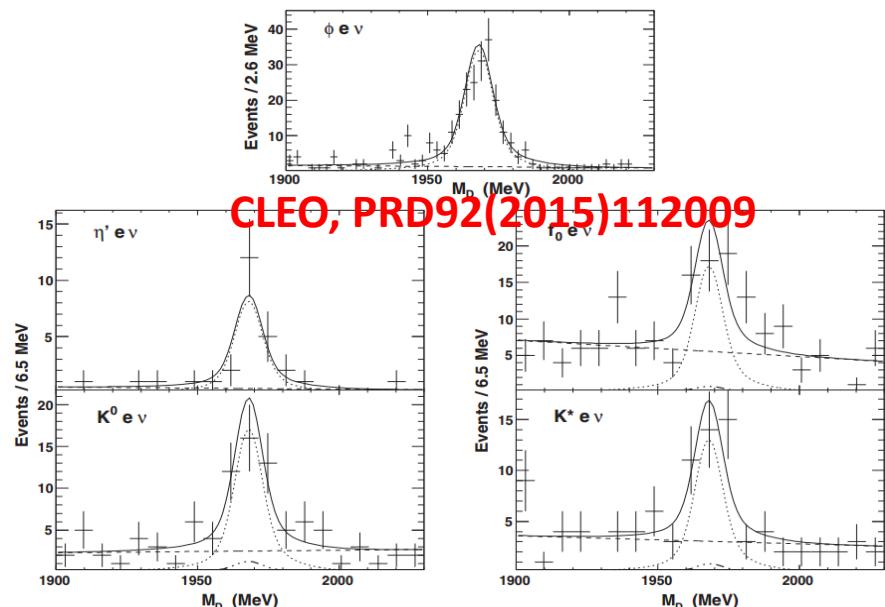


$$\frac{\Gamma(D_s \rightarrow \eta' e\nu)}{\Gamma(D_s \rightarrow \eta e\nu)} = R_D \cot^2 \phi$$

$$\frac{\Gamma(D_s \rightarrow \eta' e\nu)/\Gamma(D_s \rightarrow \eta e\nu)}{\Gamma(D^+ \rightarrow \eta' e\nu)/\Gamma(D^+ \rightarrow \eta e\nu)} = \cot^4 \phi$$

J. Hietala,^{1,*} D. Cronin-Hennessy,^{1,†} T. Pedlar,² and I. Shipsey³

with 600 pb^{-1} data@4.17 GeV



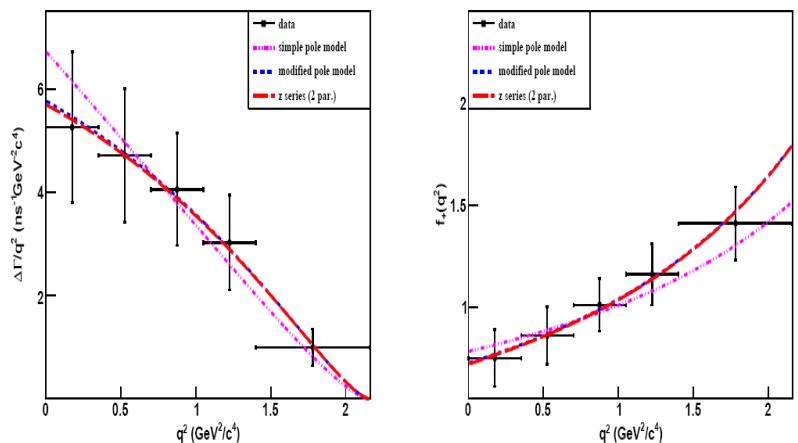
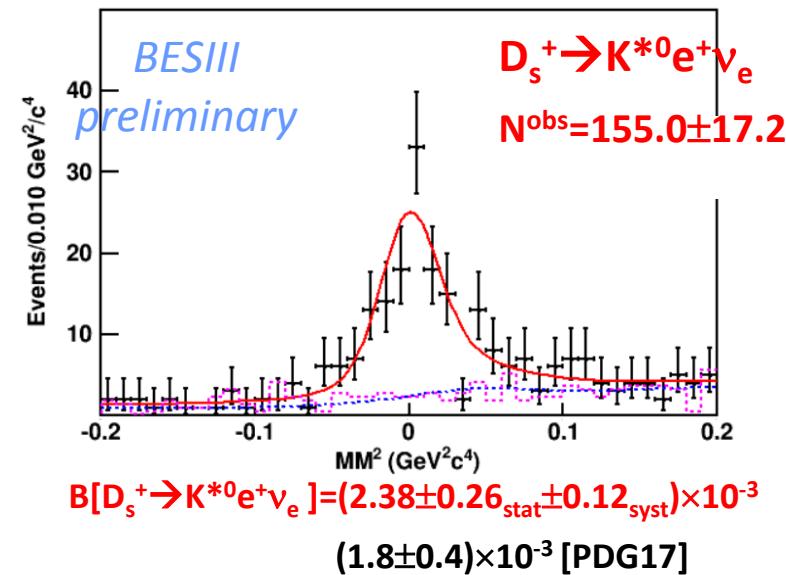
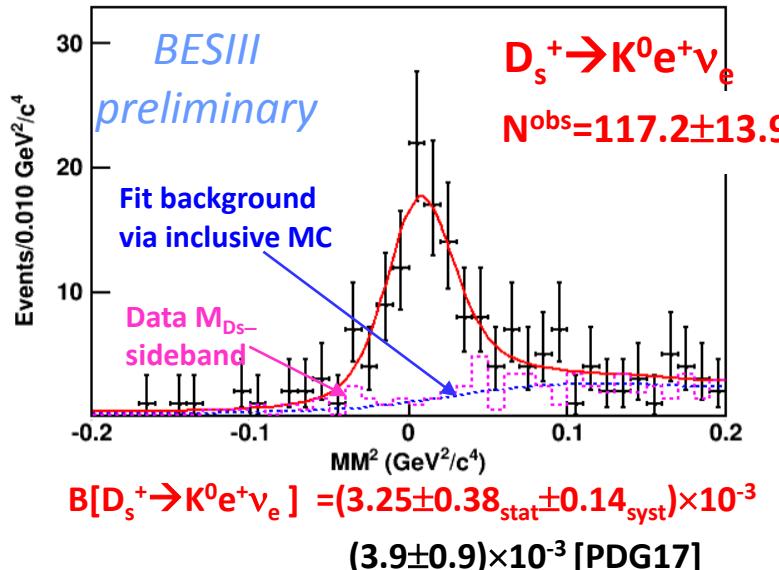
CLEO, PRD92(2015)112009

Signal mode	BABAR (%)	CLEO-c (%)	This analysis (%)
$D_s \rightarrow \phi e\nu$	$2.61 \pm 0.03 \pm 0.08 \pm 0.15$	$2.36 \pm 0.23 \pm 0.13$	$2.14 \pm 0.17 \pm 0.08$
$D_s \rightarrow \eta e\nu$...	$2.48 \pm 0.29 \pm 0.13$	$2.28 \pm 0.14 \pm 0.19$
$D_s \rightarrow \eta' e\nu$...	$0.91 \pm 0.33 \pm 0.05$	$0.68 \pm 0.15 \pm 0.06$
$D_s \rightarrow f_0 e\nu, f_0 \rightarrow \pi\pi$	Seen	$0.20 \pm 0.03 \pm 0.01$	$0.13 \pm 0.03 \pm 0.01$
$D_s \rightarrow K_S e\nu$...	$0.19 \pm 0.05 \pm 0.01$	$0.20 \pm 0.04 \pm 0.01$
$D_s \rightarrow K^* e\nu$...	$0.18 \pm 0.07 \pm 0.01$	$0.18 \pm 0.04 \pm 0.01$

$$\theta(\eta - \eta' \text{ mixing angle}) = (42 \pm 2 \pm 2)^\circ$$

$$\theta(f_0 - \text{ss mixing angle}) = (20^{+32}_{-20})^\circ$$

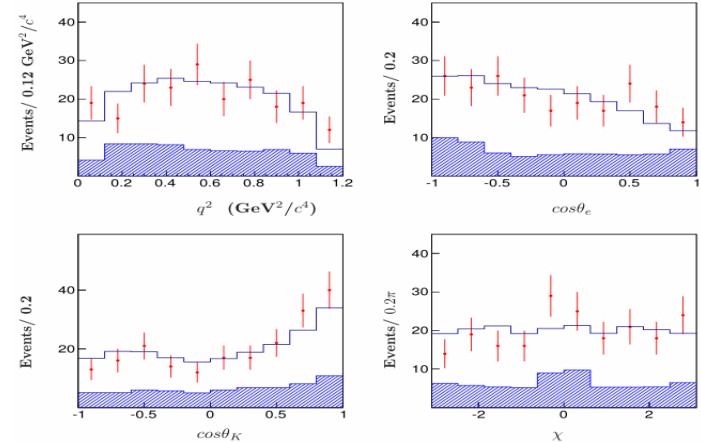
First study of $D_s^+ \rightarrow K^{(*)0} e^+ \nu_e$ dynamics at BESIII



Model	Parameter	Value	$f_+(0)$
Simple pole	$f_+(0) V_{cd} $	$0.175 \pm 0.010 \pm 0.001$	$0.778 \pm 0.044 \pm 0.004$
Modified pole model	$f_+(0) V_{cd} $	$0.163 \pm 0.017 \pm 0.003$	$0.725 \pm 0.076 \pm 0.013$
Series two parameters	α	$0.45 \pm 0.44 \pm 0.02$	
Series two parameters	$f_+(0) V_{cd} $	$0.162 \pm 0.019 \pm 0.003$	$0.720 \pm 0.084 \pm 0.013$
Series two parameters	r_1	$-2.94 \pm 2.32 \pm 0.14$	

Taking $|V_{cd}^{\text{CKMfitter}}$ as input

Four dimensional un-binned likelihood fit is performed. K^* parameters are fixed

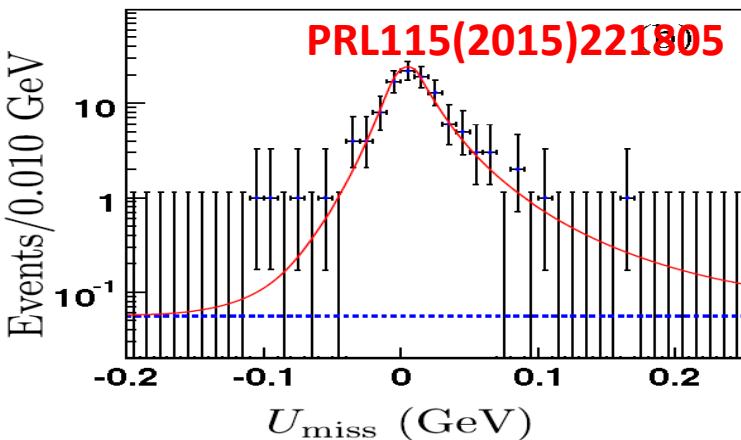


$$r_V = 1.67 \pm 0.34 \pm 0.16$$

$$r_2 = 0.77 \pm 0.28 \pm 0.07$$

First absolute BF of $\Lambda_c^+ \rightarrow \Lambda l^+ \nu$ at BESIII

- Λ_c^+ was observed in 1979
- All decays of Λ_c^+ were measured with high energy data and relative to $pK^-\pi^+$, which suffers an error of 25%. No absolute measurement using threshold Λ_c^+ data before BESIII
- Only about 60% decays are known



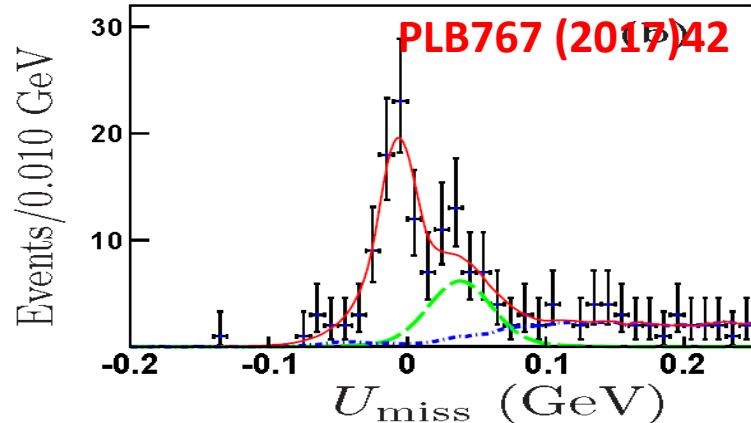
$$B[\Lambda_c^+ \rightarrow \Lambda e^+ \nu] = (3.63 \pm 0.38 \pm 0.20)\%$$

$$\Gamma[\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu] / \Gamma[\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e] = 0.96 \pm 0.16 \pm 0.04$$

Theory: (1.4-9.2)%

Theoretical Models	predicted branching fraction for $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$
MBM [1]	1.9%
NRQM [1]	2.6%
SU(4)-symmetry limit [2]	9.2%
RSQM [3]	4.4%
QCM [4]	5.62%
SQM [5]	1.96%
NRQM2 [6]	2.15%
NRQM3 [7]	1.42%
QCD SR1 [8]	(3.0 ± 0.9)%
QCD SR2 [9]	(2.6 ± 0.4)%
QCD SR3 [9]	(5.8 ± 1.5)%
STSR [10]	2.23% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
STNR [10]	1.58% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
HOSR [10]	4.72% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
HONR [10]	4.2% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
LCSR [11]	(3.0 ± 0.8)% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$ (CZ-type)
PDG 2014 [14]	(2.1 ± 0.6)%
BESIII	(3.63 ± 0.38 ± 0.20)%

3 fb⁻¹ help to explore FF studies



$$B[\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu] = (3.49 \pm 0.46 \pm 0.26)\%$$

Summary

- With $2.9/3.2 \text{ fb}^{-1}$ data taken at $3.773/4.178 \text{ GeV}$, BESIII has obtained the most precise measurements of $D_{(s)}^+ \rightarrow l^+ \nu$, $D \rightarrow \bar{D} l^+ \nu$ and other SL decays

Improved measurements of $f_{D_{(s)}^+}$ and $f_{\pi^+}^{D \rightarrow K(\pi)(q^2)}$, which are important to calibrate LQCD calculations

Improved measurements of $|V_{cs(d)}|$, which is important for unitarity test of the CKM matrix

Other studies of D SL decays (form factor measurements, new decay modes) are ongoing and will be ready soon

- With 0.567 fb^{-1} data taken at 4.6 GeV , BESIII reported the first absolute BFs of $\Lambda_c^+ \rightarrow \Lambda l^+ \nu$

In the near future, more 10 fb^{-1} data at 3.773 GeV and 3 fb^{-1} data at $\sim 4.65 \text{ GeV}$ at BESIII will further benefit all measurements

Prospects at HIEPA

If 300 fb^{-1} data can be collected at 3.773, 4.18 and 4.65 GeV, respectively

	Systematic error	Statistical error		
		$\sim 3 \text{ fb}^{-1}$	12 fb^{-1}	300 fb^{-1}
$\Delta f_{D+}/f_{D+}$	$\sim 0.9\%$	2.6%	1.3%	0.26%
$\Delta f_{D_s+}/f_{D_s+}$	$\sim 1.5\%$	1.1%	0.6%	0.11%
$\Delta f_{D \rightarrow K}/f_{D \rightarrow K}$	$\sim 0.5\%$	0.35%	0.18%	0.04%
$\Delta f_{D \rightarrow \pi}/f_{D \rightarrow \pi}$	$\sim 0.7\%$	1.26%	0.63%	0.13%
$ V_{cs} ^{D_s+ \rightarrow l+\nu}$	$\sim 1.5\%$	1.8%	0.9%	0.18%
$ V_{cs} ^{D^0 \rightarrow K^- e^+ \nu}$	2.5% (2.4% LQCD)	0.35%	0.18%	0.04%
$ V_{cd} ^{D^+ \rightarrow \mu^+ \nu}$	2.1% (1.9 → 0.5% LQCD)	2.6%	1.3%	0.26%
$ V_{cd} ^{D^0 \rightarrow \pi^- e^+ \nu}$	4.5% (4.4% LQCD)	1.26%	0.63%	0.13%

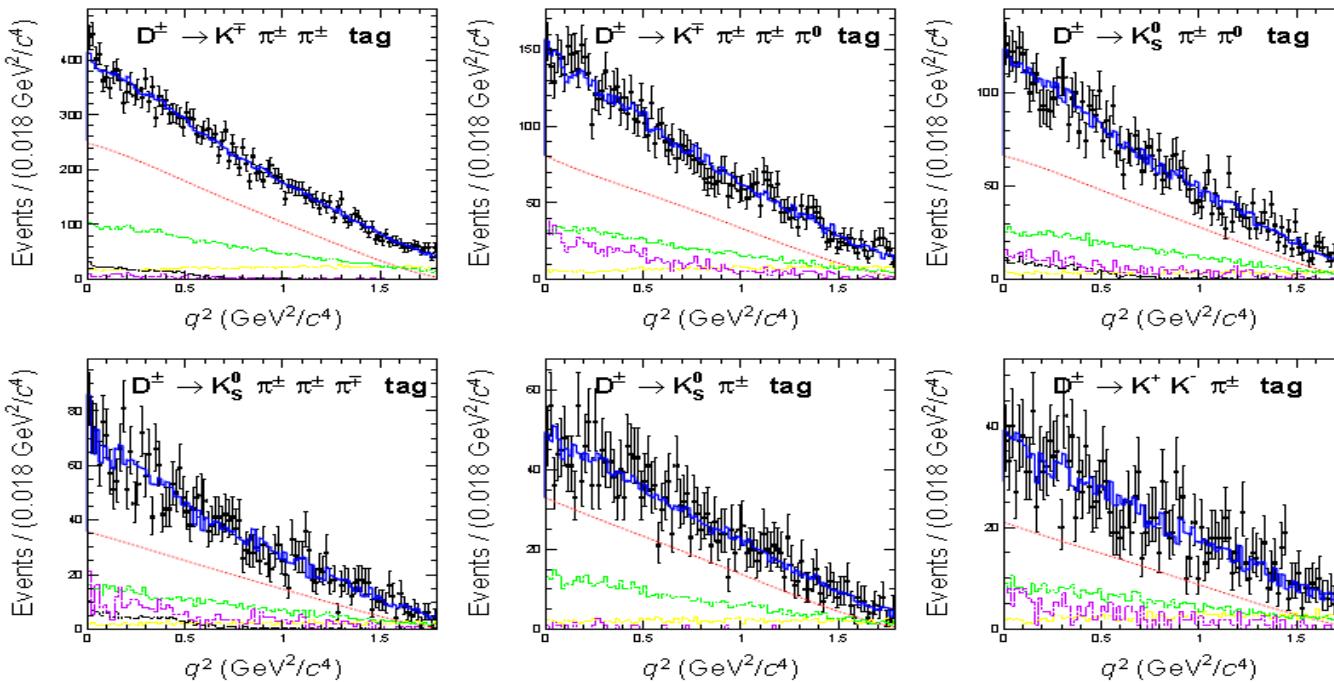
- LQCD calculation uncertainties in the FFs of $D \rightarrow Pl^+\nu$ are expected to reduce to (0.5-1.0)% to better measure $|V_{cs(d)}|$ using D SL decays
- Precise FF studies, especially for $D \rightarrow S/Ae^+\nu$ and $\Lambda_c^+ SL$ decays, as well as other suppressed SL decays

Thank you!

Study of $D^+ \rightarrow K_L e^+ \nu$ at BESIII

- Regardless of long flight distance, K_L interact with EMC and deposit part of energy, thus giving position information
- After reconstructing all other particles, K_L can be inferred with position information and constraint $U_{\text{miss}} \rightarrow 0$

Simultaneous fit to event density $I(q^2)$ with 2-par. series Form Factor



$$\overline{B}(D^+ \rightarrow K_L e^+ \nu) = (4.482 \pm 0.027 \pm 0.103)\%$$

$$A_{CP} \equiv \frac{\mathcal{B}(D^+ \rightarrow K_L^0 e^+ \nu_e) - \mathcal{B}(D^- \rightarrow K_L^0 e^- \bar{\nu}_e)}{\mathcal{B}(D^+ \rightarrow K_L^0 e^+ \nu_e) + \mathcal{B}(D^- \rightarrow K_L^0 e^- \bar{\nu}_e)}$$

$$A_{CP}^{D^+ \rightarrow K_L e^+ \nu} = (-0.59 \pm 0.60 \pm 1.50)\%$$

$D^+ \rightarrow K_L e^+ \nu$ is measured for the first time

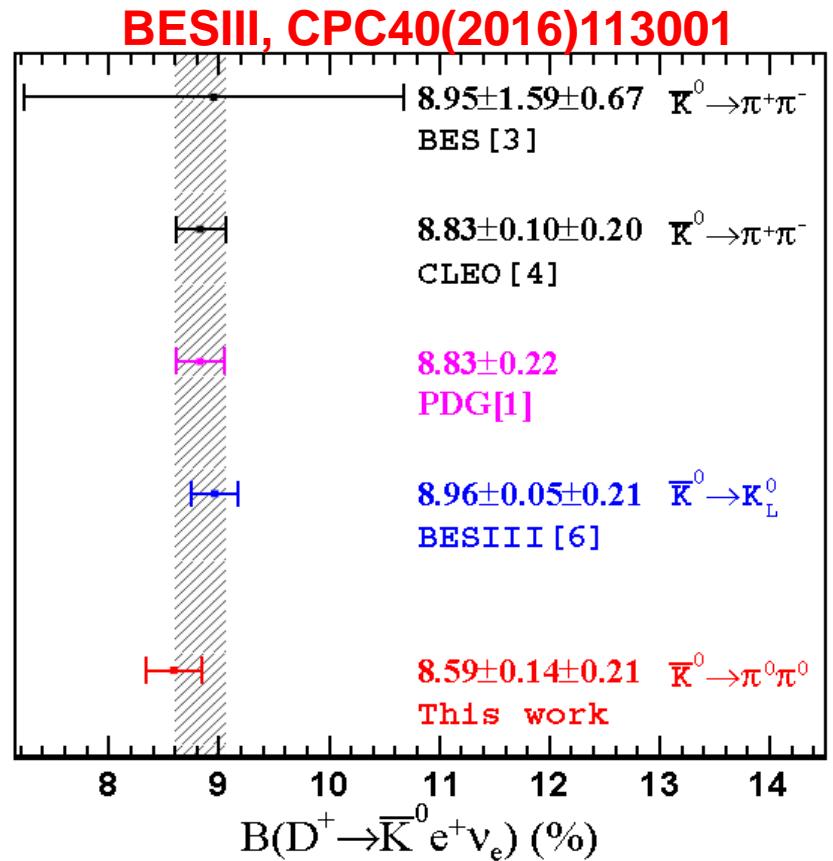
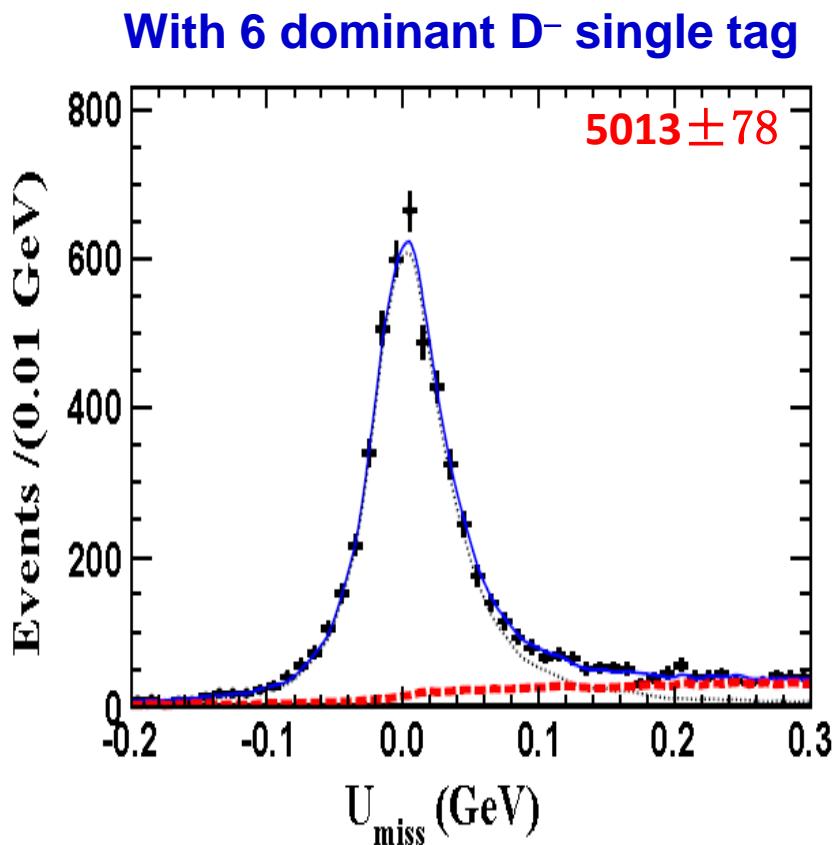
PRD92(2015)112008

With 6 dominant D^- single tag

$$f_{K_+}(0)|V_{cs}| = 0.728 \pm 0.006 \pm 0.011$$

$$r_1 = a_1/a_0 = -1.91 \pm 0.33 \pm 0.24$$

Absolute BF for $D^+ \rightarrow \bar{K}^0 e^+ v$ via $\bar{K}^0 \rightarrow \pi^0 \pi^0$



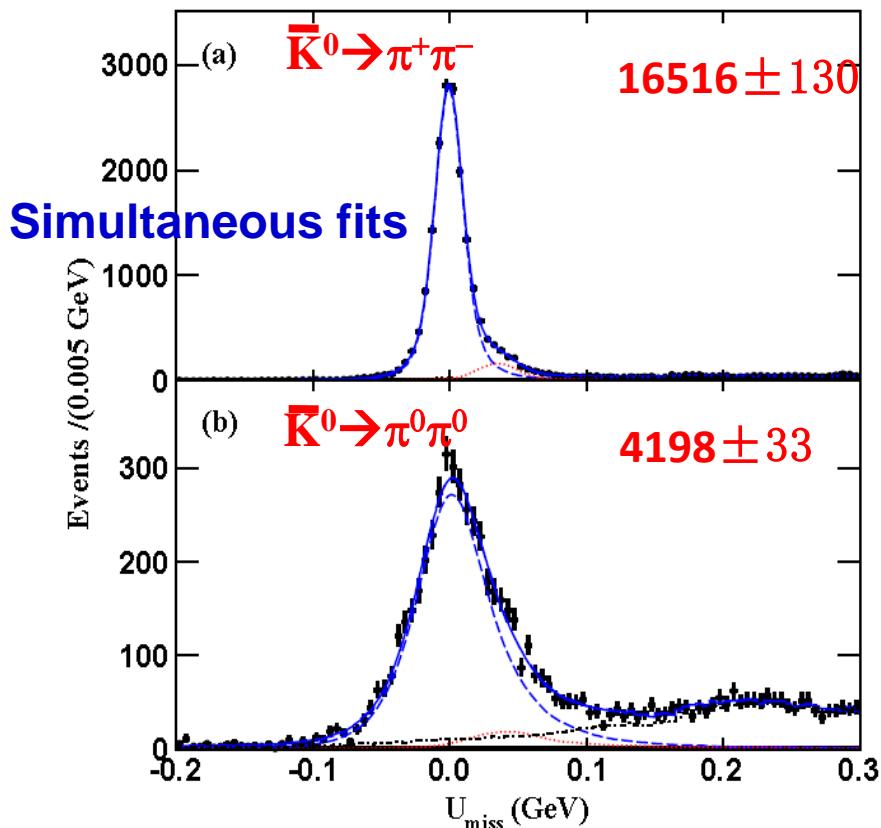
Taking τ_{D^+} , τ_{D0} , $B[D^0 \rightarrow K^- e^+ v]$ and $B[D^+ \rightarrow \bar{K}^0 e^+ v]$ from the PDG as input

$$\frac{\Gamma[D^0 \rightarrow K^- e^+ v]}{\Gamma[D^+ \rightarrow \bar{K}^0 e^+ v]} = 0.969 \pm 0.025$$

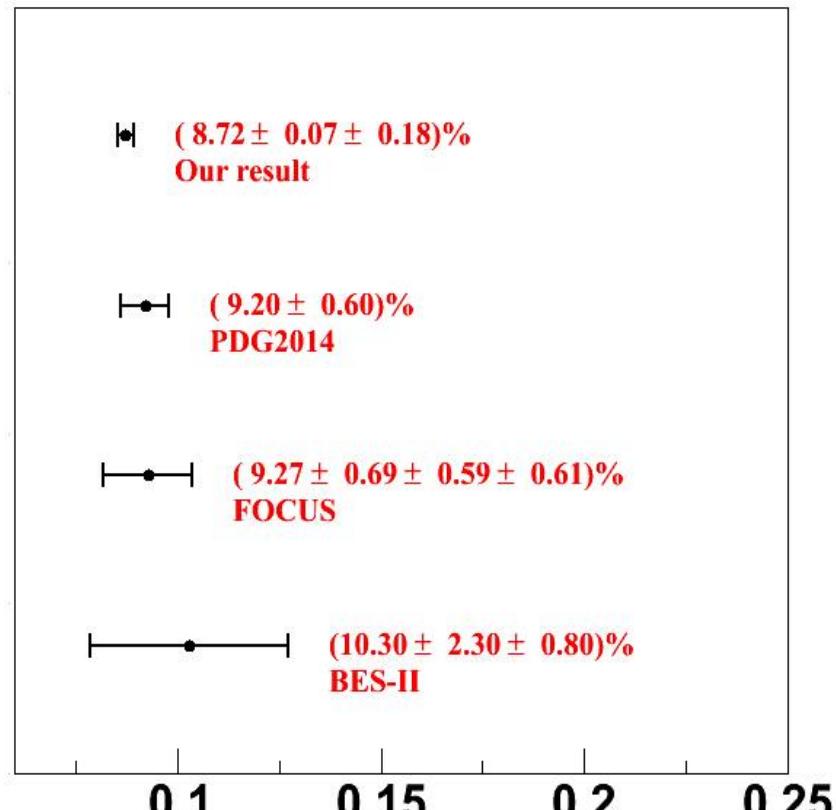
Agrees with isospin conservation within 1.2σ

Improved BF for $D^+ \rightarrow \bar{K}^0 \mu^+ \nu$ at BESIII

With 6 dominant D^- single tag



BESIII, EPJC76(2016)369



Taking $B[D^0 \rightarrow K^- \mu^+ \nu]$
and $B[D^+ \rightarrow \bar{K}^0 e^+ \nu]$
from the PDG as input

$$\frac{\Gamma[D^0 \rightarrow K^- \mu^+ \nu]}{\Gamma[D^+ \rightarrow \bar{K}^0 \mu^+ \nu]} = 0.963 \pm 0.044$$

$$\frac{\Gamma[D^+ \rightarrow \bar{K}^0 \mu^+ \nu]}{\Gamma[D^+ \rightarrow \bar{K}^0 e^+ \nu]} = 0.988 \pm 0.033$$

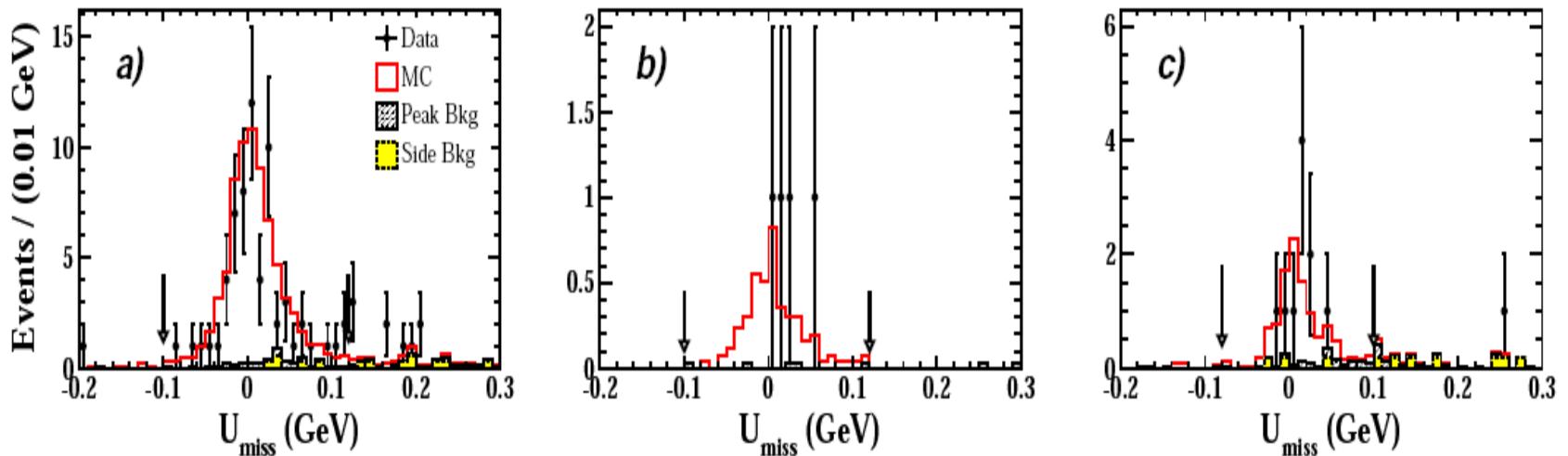
Support isospin conservation in
these two decays within errors

Consistent with theory
prediction 0.97 within error

BFs of $D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu$ at BESIII

- Benefit the understanding of the source of difference of inclusive decay rates of $D^0(+)$ and D_s^+
- Complementary information to understand $\eta - \eta'$ mixing

482 pb⁻¹ data@4.009 GeV, PRD94(2016)112003

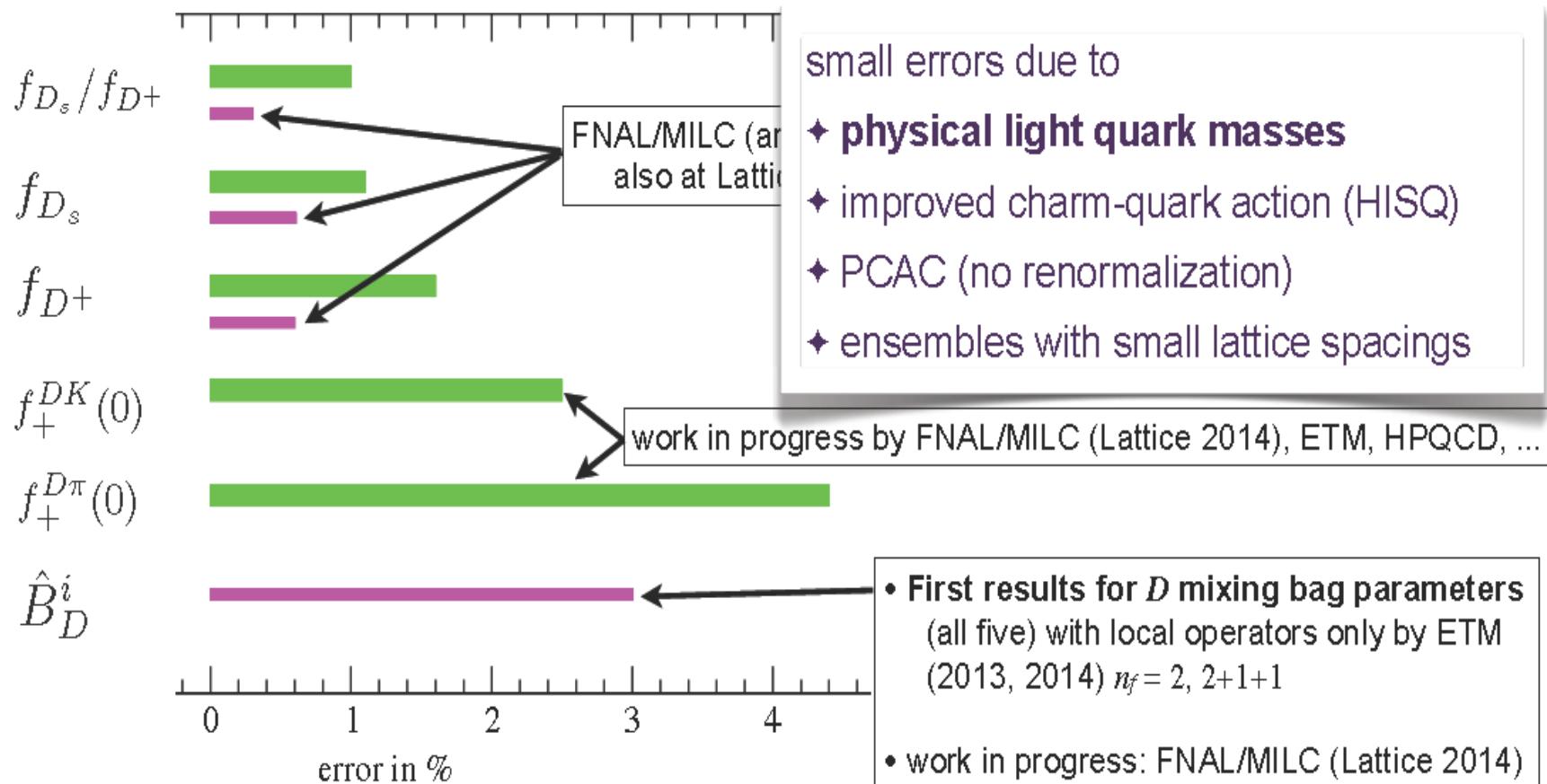


	BESIII	CLEOII 95	= CLEOc09 =	= CLEOc15 =	PDG [4]
$B(D_s^+ \rightarrow \eta e^+ \nu_e)[\%]$	$2.30 \pm 0.31 \pm 0.08$	—	$2.48 \pm 0.29 \pm 0.13$	$2.28 \pm 0.14 \pm 0.20$	2.67 ± 0.29
$B(D_s^+ \rightarrow \eta' e^+ \nu_e)[\%]$	$0.93 \pm 0.30 \pm 0.05$	—	$0.91 \pm 0.33 \pm 0.05$	$0.68 \pm 0.15 \pm 0.06$	0.99 ± 0.23
$\frac{B(D_s^+ \rightarrow \eta' e^+ \nu_e)}{B(D_s^+ \rightarrow \eta e^+ \nu_e)}$	$0.40 \pm 0.14 \pm 0.02$	$0.35 \pm 0.09 \pm 0.07$	—	—	—

Much improved LQCD calculations

Taking from Aida X. El-Khadra's talk at Beauty2014

errors (in %) comparison: **FLAG-2 averages** vs. **new results**



review by C. Bouchard @ Lattice 2014