

Study of Baryon form factors at BESIII

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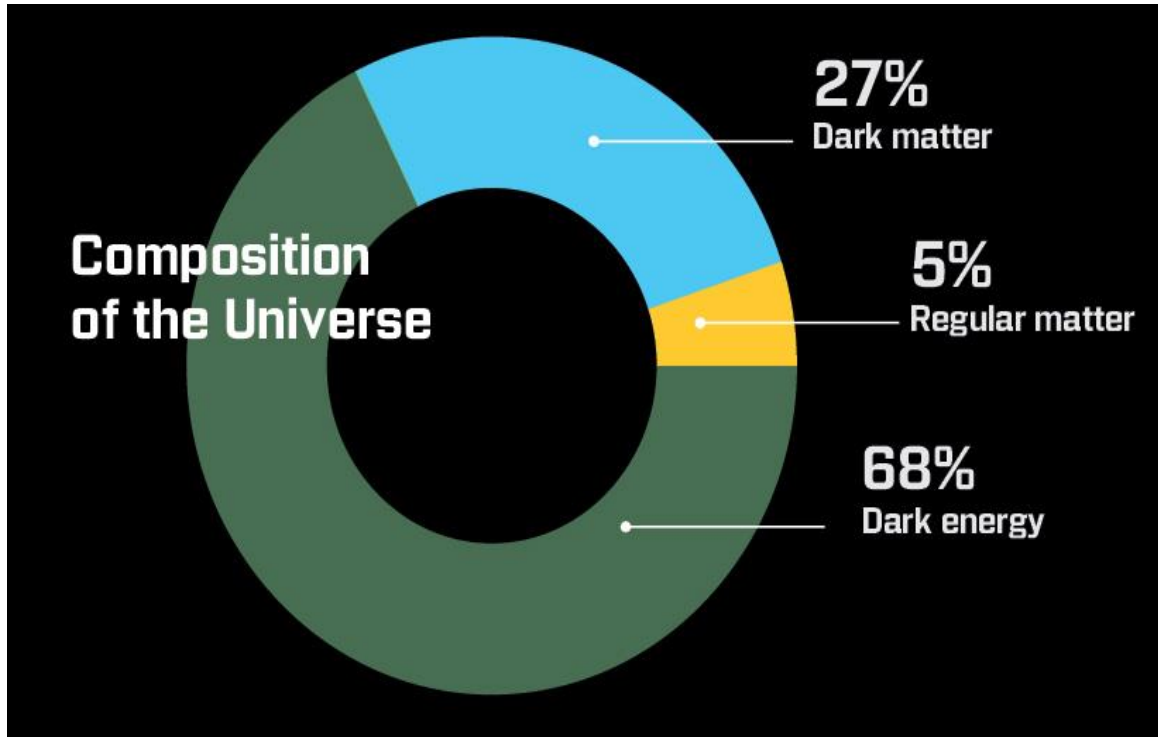
**State Key Laboratory of Particle Detection and Electronics
University of Science and Technology of China**

**Workshop of the Baryon Production at BESIII, Hefei, China
9.15th, 2019**

Outline

- Introduction
- Baryon Form factors
 - Nucleon form factors
 - Hyperon form factors
- Summary and prospect

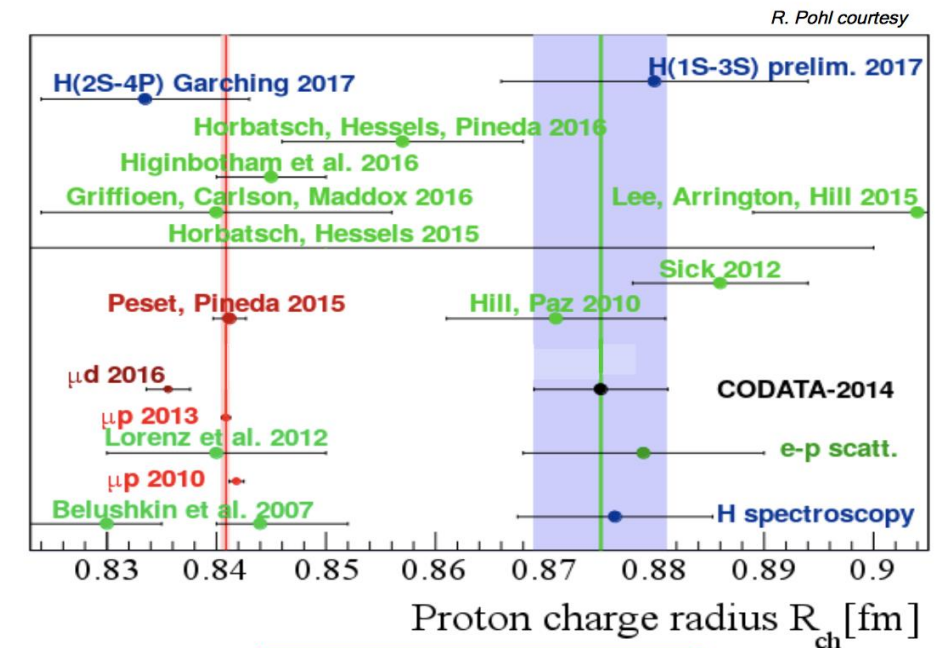
Composition of the Universe



NASA

- Nucleon is the dominant component of visible universe (>99%)

Proton Radius Confusion



Need for more data !!

- Probe nucleon charge radius:

$$G_E(Q^2) = 1 - \frac{1}{6} r_E^2 Q^2 + \dots \quad (Q: \text{four momentum transfer})$$

Nucleon Electromagnetic Form Factor (NEFF)

- Elastic scattering of electron and proton (Hofstadter, Nobel Prize 1961)

- Theoretically, differential cross section is:

$$\left(\frac{d\sigma}{d\Omega}\right)_{ep} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \left(1 + 2\tau \tan^2 \frac{\theta}{2}\right) F(q^2)$$

- The nucleon **electromagnetic vertex** Γ_μ describing the hadron current:

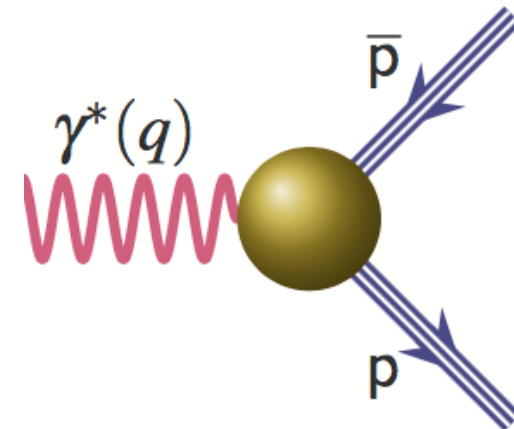
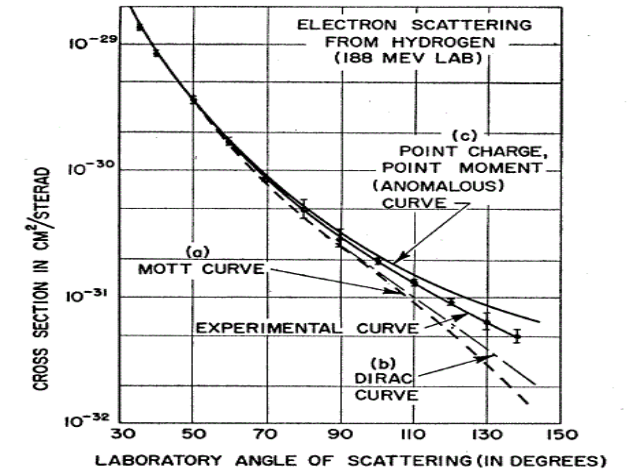
$$\Gamma_\mu(p', p) = \gamma_\mu F_1(q^2) + \frac{i\sigma_{\mu\nu} q^\nu}{2m_p} F_2(q^2)$$

- Sachs FFs:

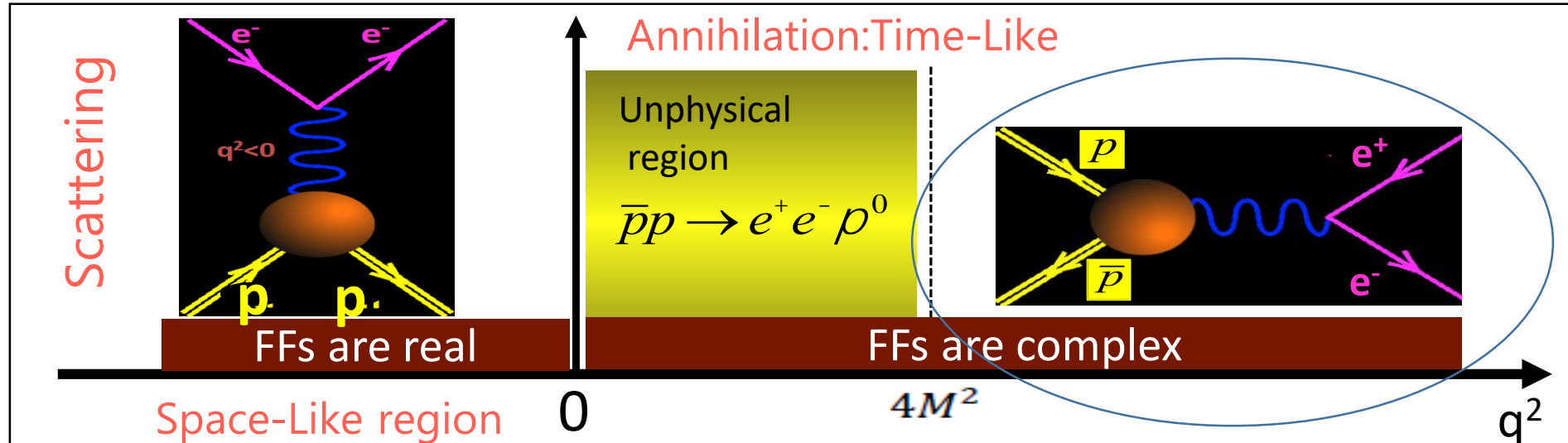
$$\text{Electric FF: } G_E(q^2) = F_1(q^2) + \tau \kappa_p F_2(q^2)$$

$$\text{Magnetic FF: } G_M(q^2) = F_1(q^2) + \kappa_p F_2(q^2)$$

$$\tau = \frac{q^2}{4m^2}, \quad \kappa = \frac{g-2}{2}, \quad g = \frac{\mu}{J}$$



Playground of EMFFs



- **In SL**, FFs are real.
 - Encode information about charge distribution of the nucleon
- **In TL**, FFs are complex, $|G_E/G_M|$ and $\Delta\Phi$.
 - Can be related to the time evolution of the EM charges within the nucleon
- **BESIII has access to the FFs in TL**

Measurement techniques for baryon FF

	Energy Scan	Initial State Radiation
E_{beam}	discrete	fixed
\mathcal{L}	low at each beam energy	high at one beam energy
σ	$\frac{d\sigma_{p\bar{p}}}{d(\cos\theta)} = \frac{\pi\alpha^2\beta C}{2q^2} [G_M ^2(1+\cos^2\theta) + \frac{4m_p^2}{q^2} G_E ^2 \sin^2\theta]$	$\frac{d^2\sigma_{p\bar{p}\gamma}}{dq^2 d\theta_\gamma} = \frac{1}{s} W(s, x, \theta_\gamma) \sigma_{p\bar{p}}(q^2)$ $W(s, x, \theta_\gamma) = \frac{\alpha}{\pi x} \left(\frac{2-2x+x^2}{\sin^2\theta_\gamma} - \frac{x^2}{2} \right)$
q^2	single at each beam energy	from threshold to s

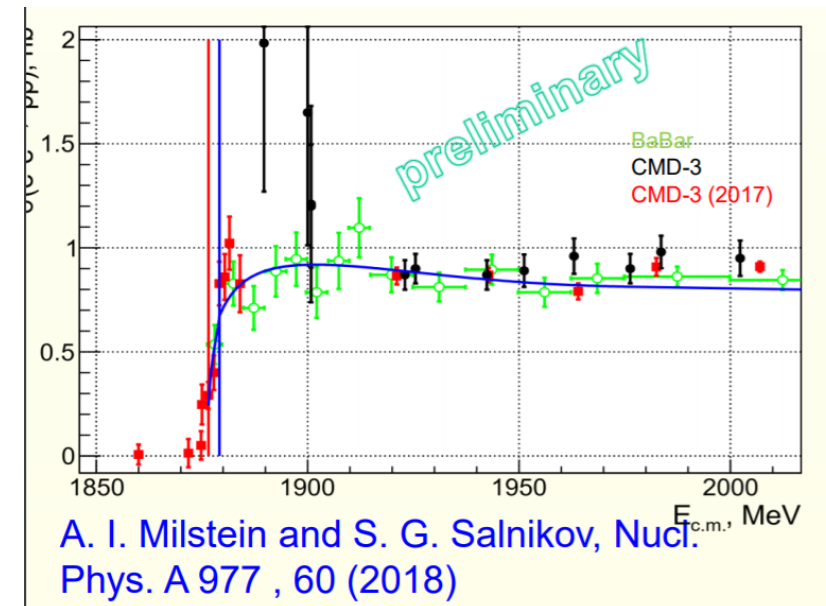
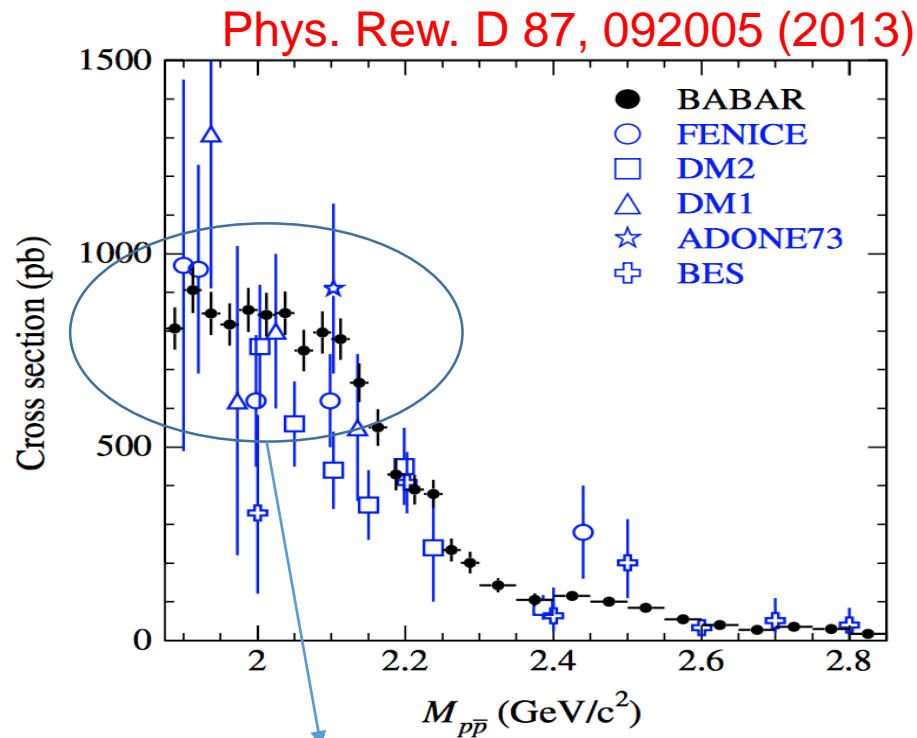
Both techniques, energy scan and initial state radiation, can be used at BESIII



$$\sim \frac{1}{400}$$

Status on proton FFs

- Still mystery on **proton cross section** line-shape

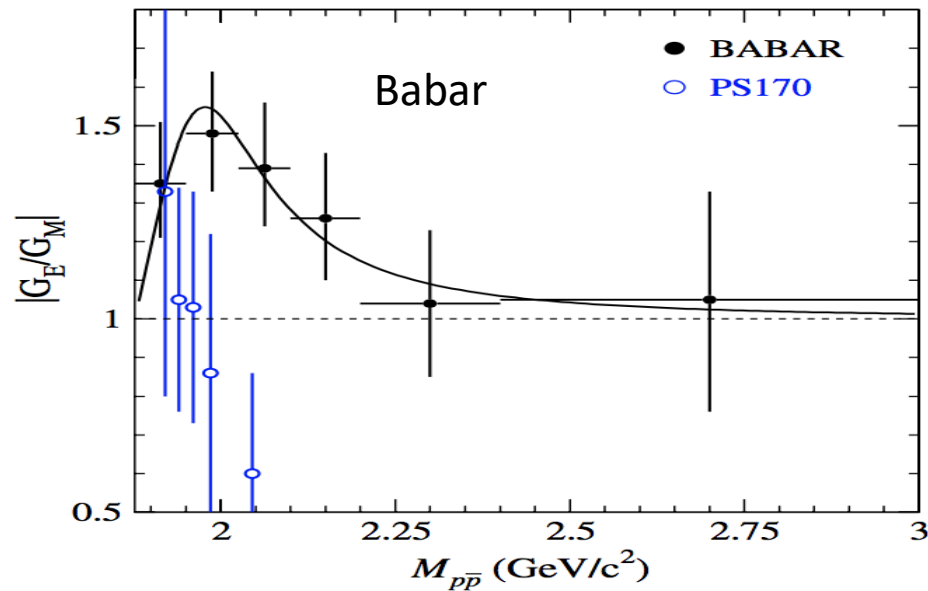


- Point-like cross section near threshold,
- $\sigma_{\text{point}} = \frac{\pi\alpha^2}{3m^2\tau} \left[1 + \frac{1}{2\tau}\right]$
- The $e^+e^- \rightarrow p\bar{p}$ cross section shows an exponential growth in 1 MeV interval above threshold.

Status on proton FFs

- Inconsistence on $|G_E/G_M|$ of proton & poor precision

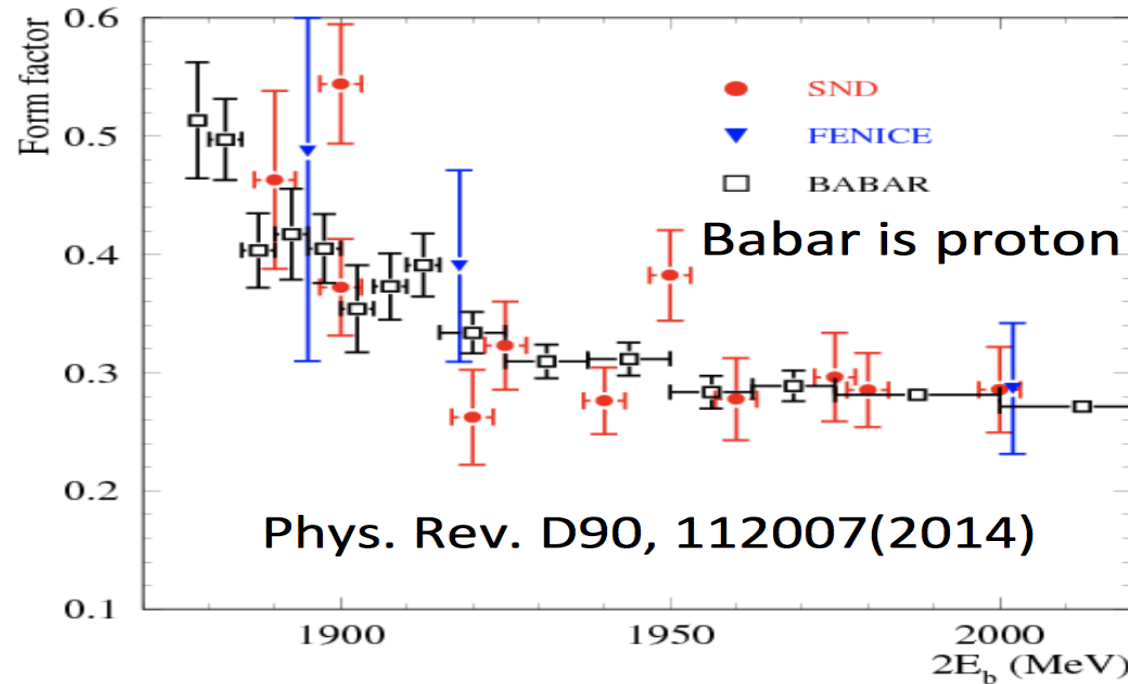
Phys. Rev. D 87, 092005 (2013)



- pQCD predicts a continuous transition and SL-TL equality at high Q^2
- SL best accuracy in $Q^2(0.5, 8.5) \text{ GeV}^2$: 1.7%
- TL accuracy before BESIII: exceeding 20%

Status on neutron FFs

- Poor precision, limited q^2 range in **neutron FF**

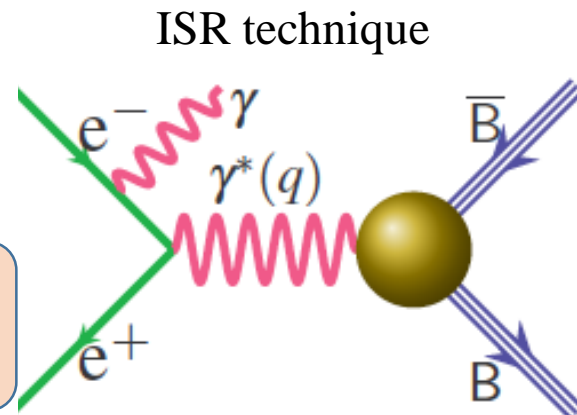
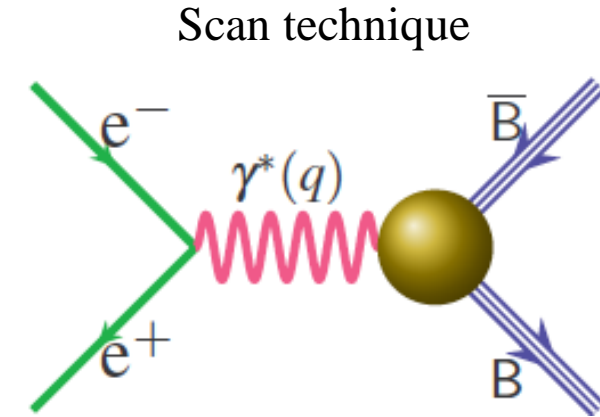
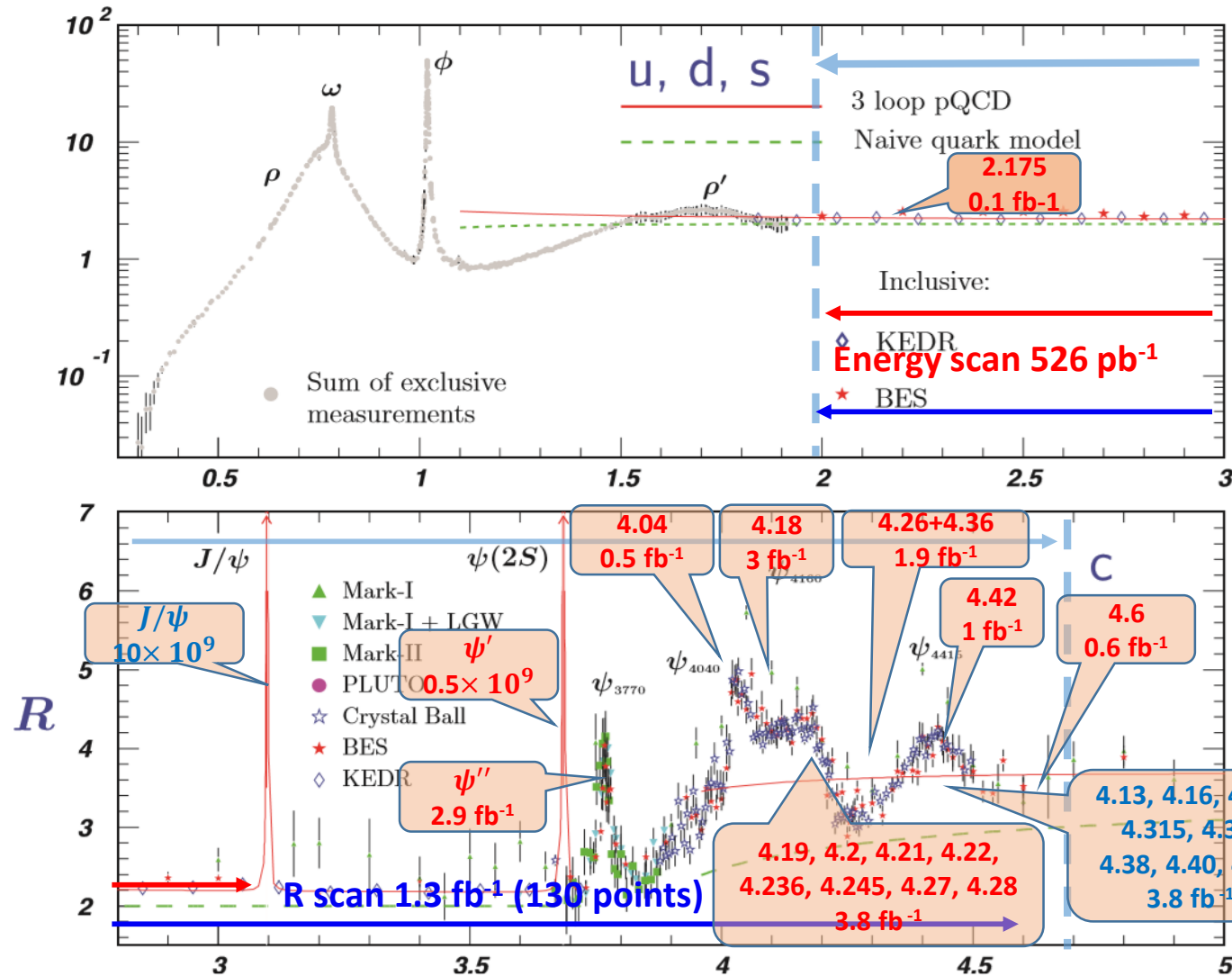


- pQCD prediction^[1]: $|\frac{G_M^n}{G_M^p}|^2 \approx (\frac{q_d}{q_u})^2 = 0.25$
- VMD prediction^[2]: $|\frac{G_M^n}{G_M^p}|^2 \approx 1$

[1] V. L. Chernyak and I. R. Zhitnitsky, Nucl. Phys. B 246 (1984) 52.

[2] J. G. Körner and m. Kuroda, Phys. Rev. D 16 (1988) 2165.

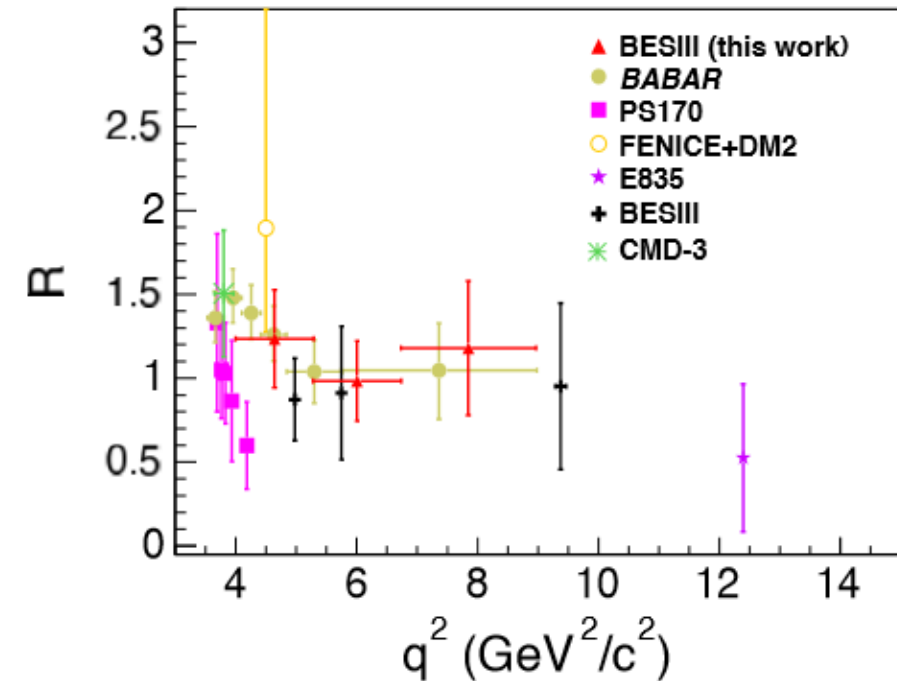
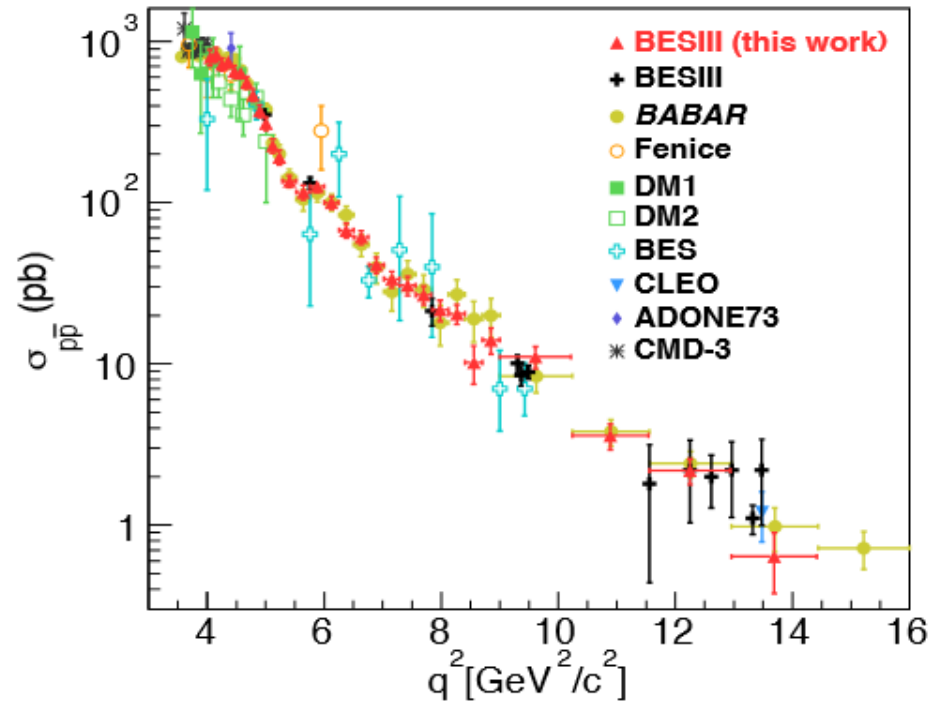
BESIII data samples



Proton FFs with ISR technique

[Phys. Rev. D99, 092002 \(2019\)](#)

- Combined seven data samples (7.4 fb^{-1})

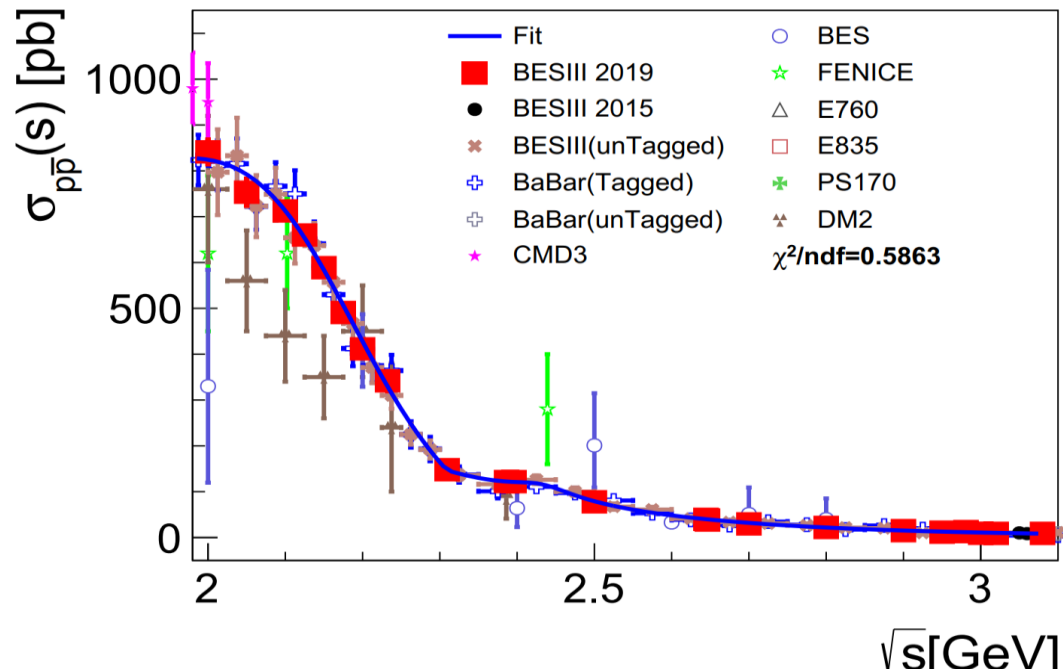


- Precision on $|G_{\text{eff}}|$: 4.1%-28.7%(untagged)
- Precision $|G_E/G_M|$ ratio: 23.0%-31.4%(untagged)
- Confirm Babar's result on $|G_E/G_M|$ above threshold

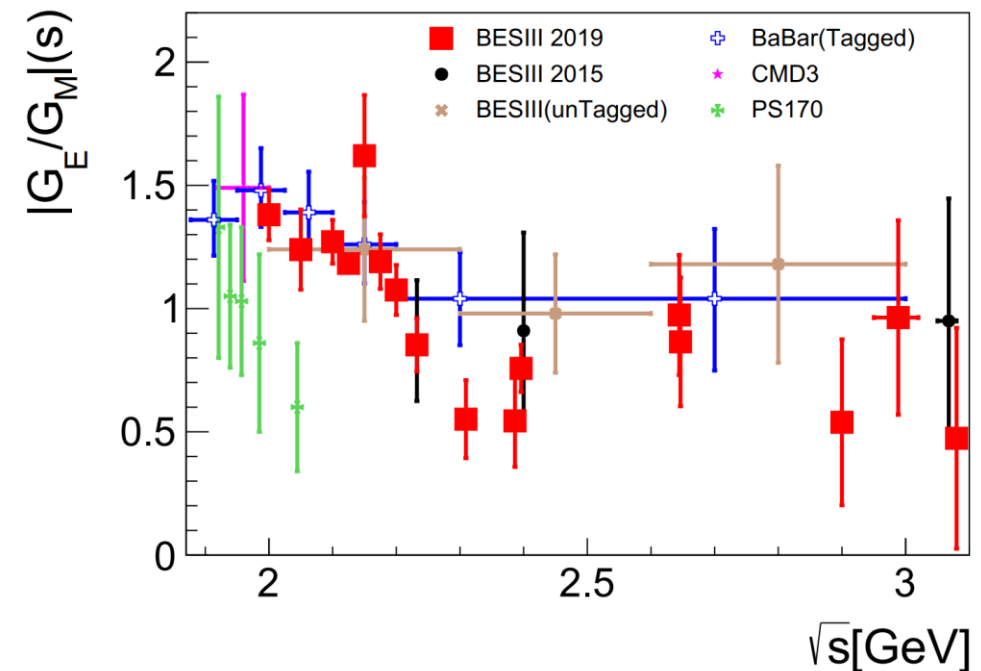
Proton FFs with scan technique

[arxiv:1905.09001](https://arxiv.org/abs/1905.09001)

- Precise measurement of cross section $e^+e^- \rightarrow p\bar{p}$ at 22 points from 2.0 to 3.08 GeV, 688.5 pb⁻¹
- $|G_E/G_M|$, $|G_M|$ are determined with high accuracy, with uncertainty comparable to data in SL
- $|G_E|$ is measured for the first time



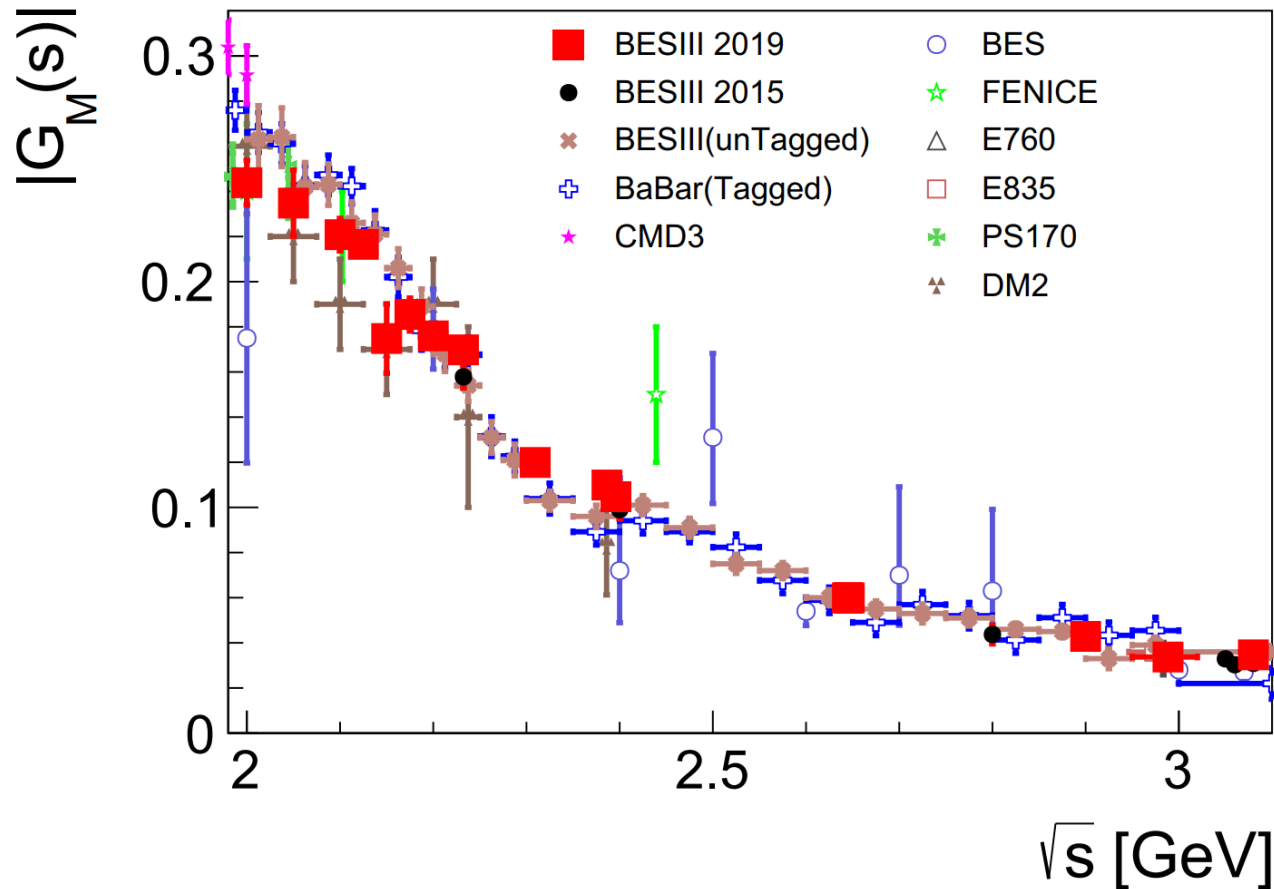
Best precision on σ : 3% (systematic dominant)



Best precision on $|G_E/G_M|$: 3.4% (statistical dominant)

Proton FFs with scan technique

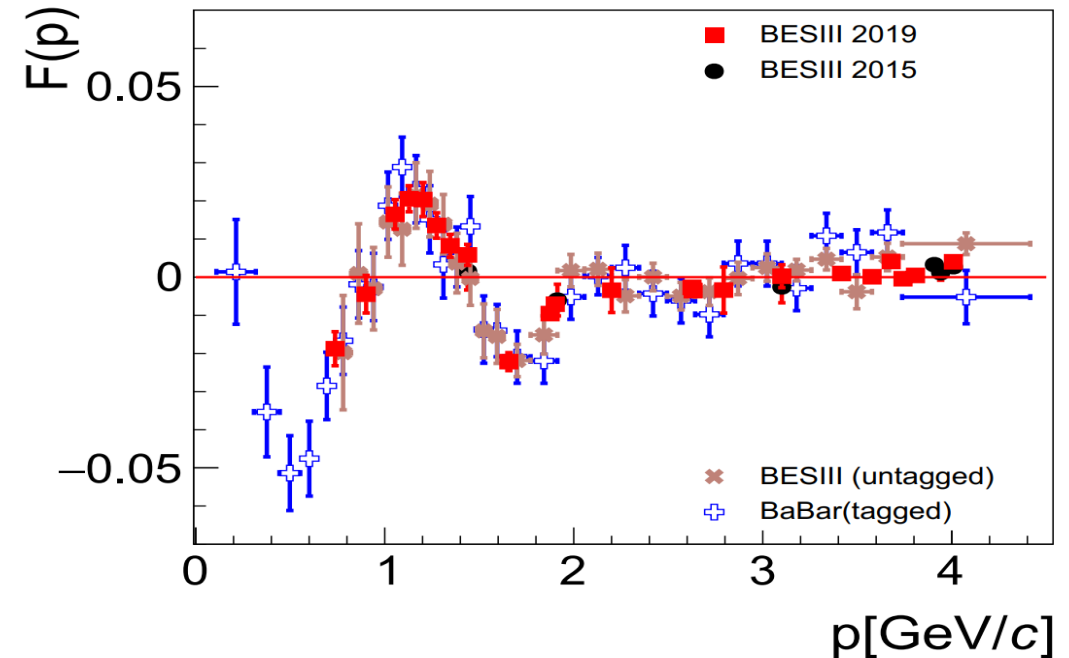
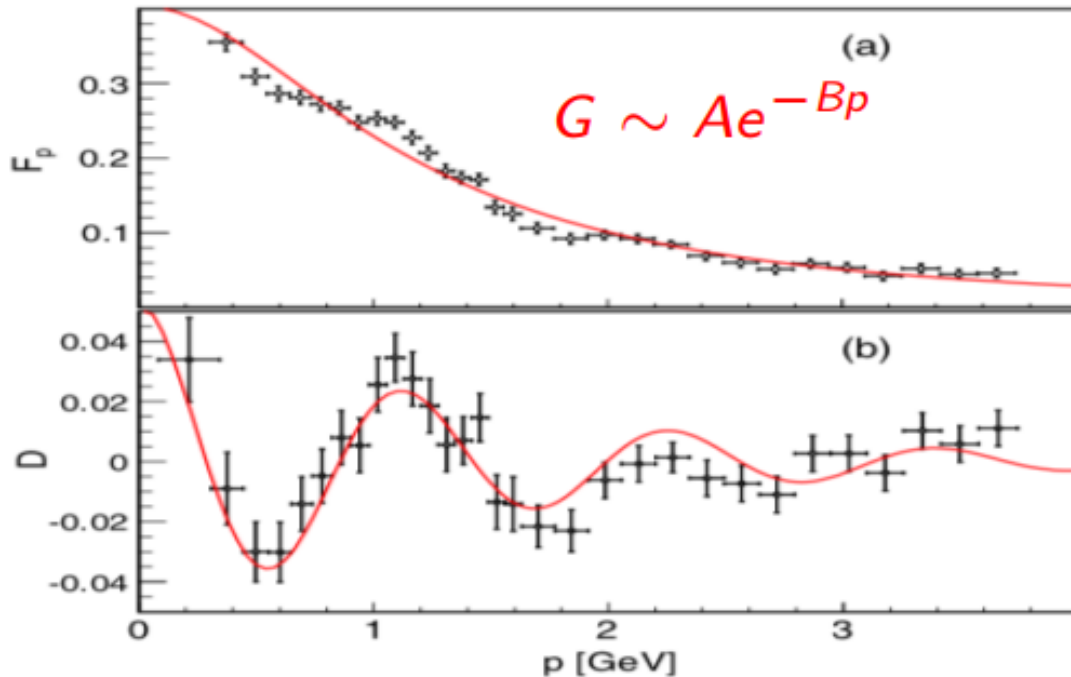
[arxiv:1905.09001](https://arxiv.org/abs/1905.09001)



- Hypothesis on other results:
 $|G_E| = |G_M|$
- First line-shape of $|G_M|$ without hypothesis, achieved by BESIII scan data.

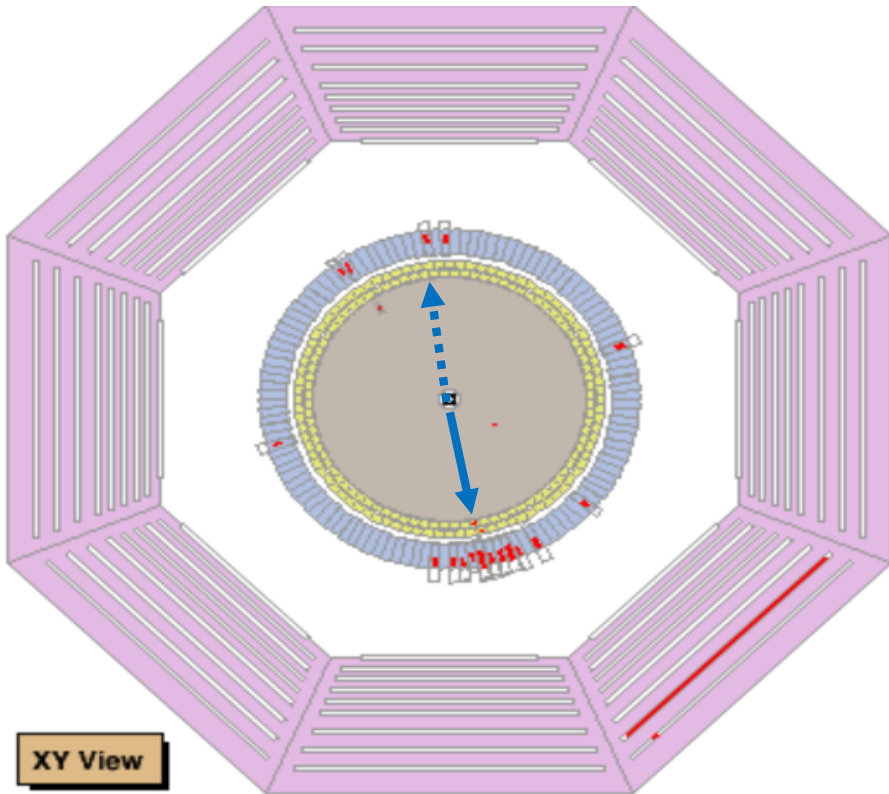
Oscillation structures ?

PRL. 114, 232301 (2015)

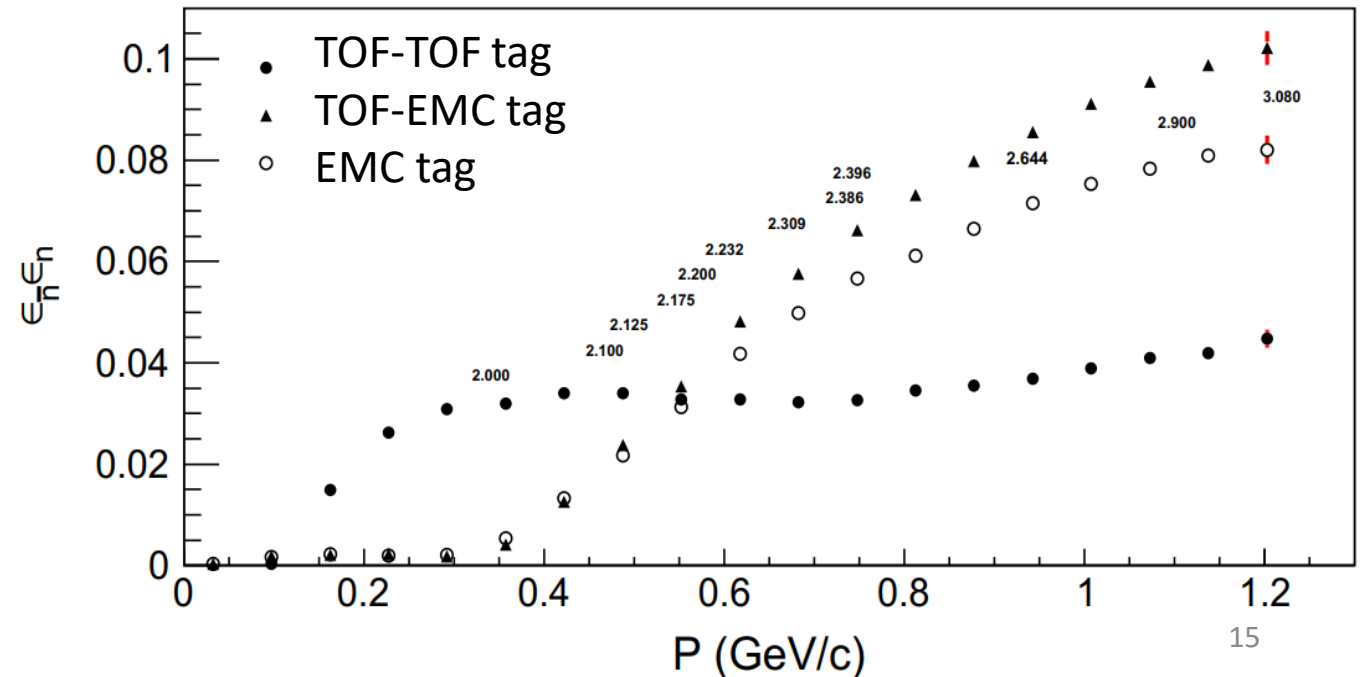


- Oscillating structures observed in the EFF minus modified dipole parameterization in Babar.
 - Rescattering process in final state
 - Independent resonant structure

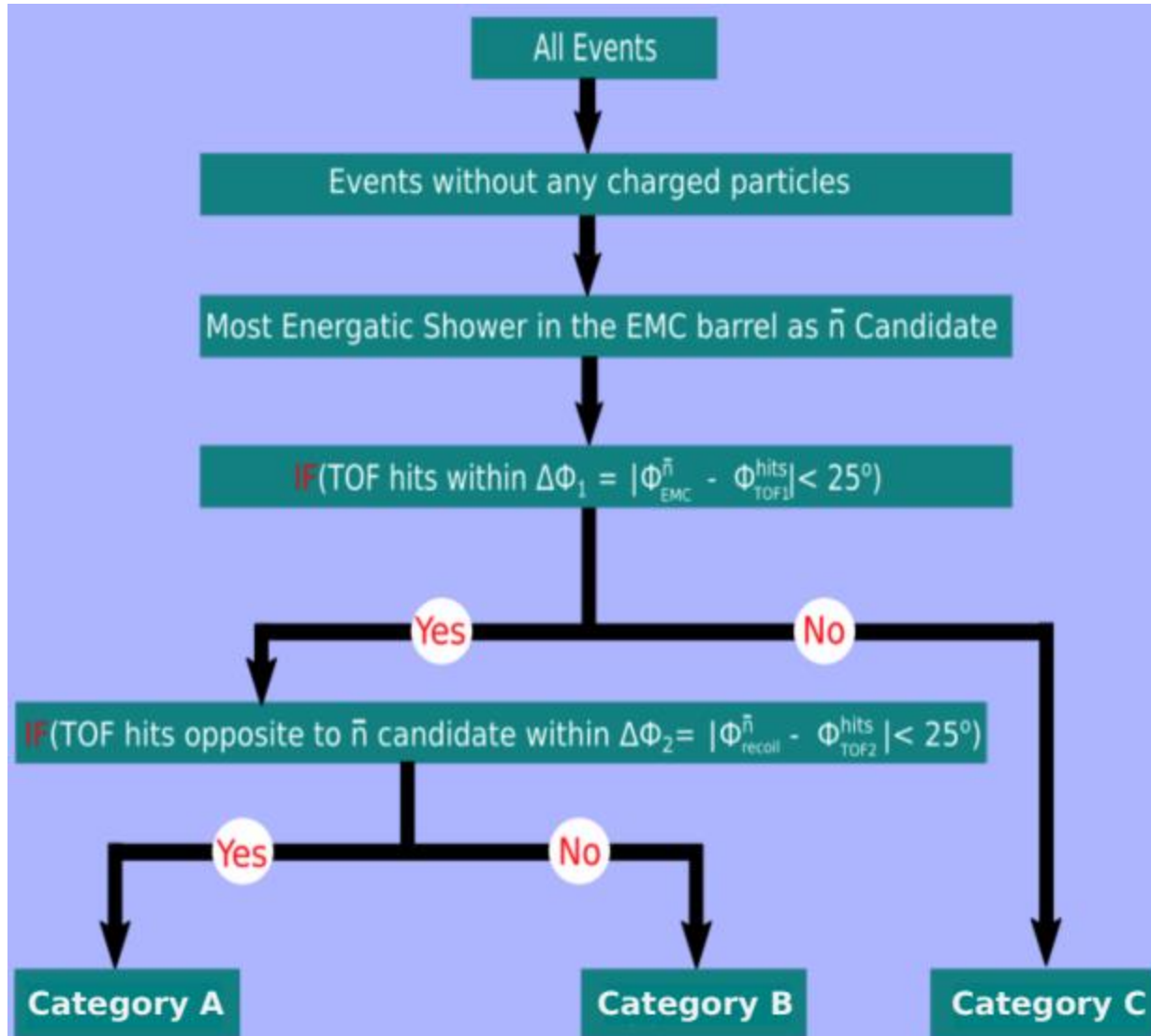
Neutron form factors at BESIII



- Analysis Challenges: Reconstruction of $e^+e^- \rightarrow n\bar{n}$
 - No MDC signal
 - Low EMC efficiency,
 - No TOF reconstruction



Neutron form factors at BESIII

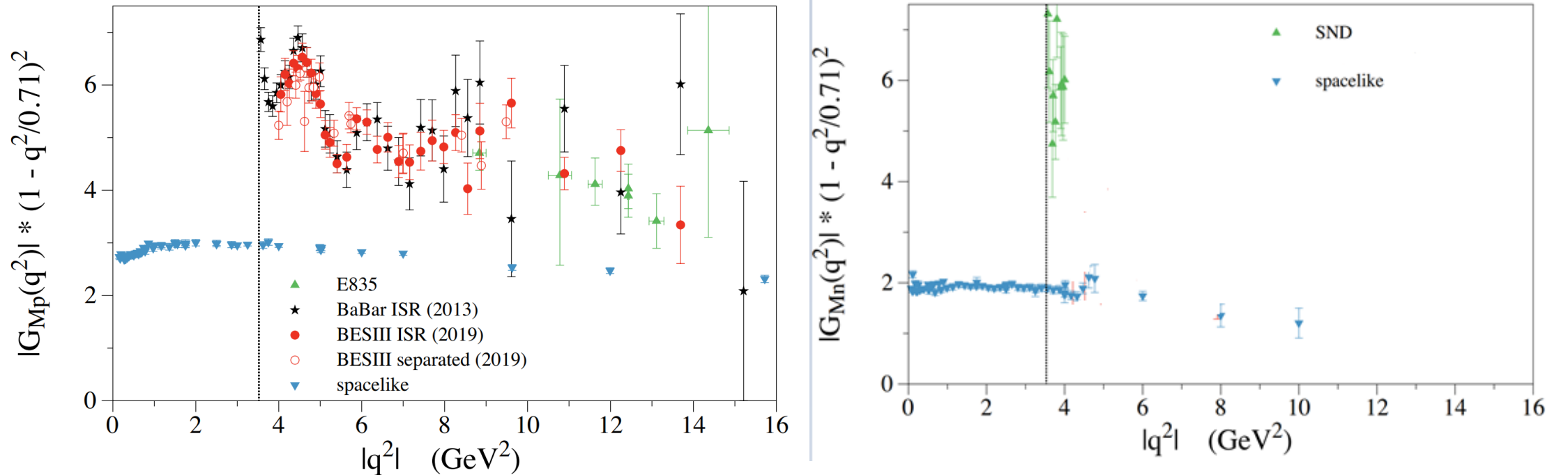


➤ Event must be selected by only one of the three categories.

➤ Events in each of the three categories undergo a complete independent analysis:

- ✓ Selection Criteria
- ✓ Signal yield extraction
- ✓ Efficiency determination
- ✓ Corrections for efficiency
- ✓ Cross section determination

Comparison with Space-Like Results



■ Neutron and Proton Magnetic Form Factors in the SL and TL regions:

- The pQCD predicts an asymptotic behavior of the form factors in the SL and TL regions.
- At high q^2 , the pQCD predicts $G_M(\text{SL})=G_M(\text{TL})$ for neutron and proton form factors.
- The neutron and proton form factors in the TL region are larger than those in the SL region.

Angular Analysis for the Extraction of R_{EM} and $|G_M|$ FFs

The R_{EM} and $|G_M|$ form factors can be extracted by fitting the efficiency corrected angular distribution:

$$\frac{d\sigma_{n\bar{n}}^{Born}}{d\cos\theta_{\bar{n}}} = \frac{d\mathcal{N}/d\cos\theta_{\bar{n}}}{\epsilon_{n\bar{n}}^{MC} \times \mathcal{C}_{dm} \times \mathcal{C}_{trg} \times (1 + \delta) \times \mathcal{L}_{Int}} = A \times |G_M|^2 \left[(1 + \cos^2\theta_{\bar{n}}) + R_{em}^2 \frac{4M_n^2}{s} (1 - \cos^2\theta_{\bar{n}}) \right]$$

- $R_{em}^2 = |G_E/G_M|$ is the form factor ratio, $A = \frac{2\pi\alpha^2\beta}{4s}$ is the normalisation factor.

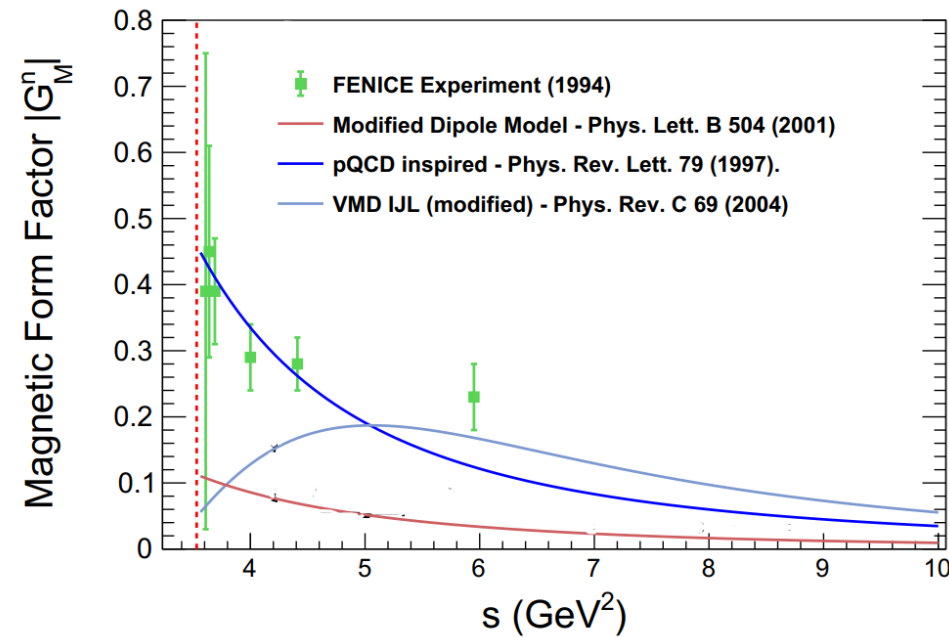
Integration over bin width of the fit function is performed due to the large bin width:

$$\left(\frac{d\sigma_{n\bar{n}}^{Born}}{d\cos\theta_{\bar{n}}} \right)_i = \sum_{bin=1}^{bin=n} \int_{bin} A_i \times |G_M|^2 \left[(1 + \cos^2\theta_{\bar{n}}) + R_{em}^2 \frac{4M_n^2}{s} (1 - \cos^2\theta_{\bar{n}}) \right]$$

- i stands for the three categories, i.e A, B and C.

The neutron form factors are extracted by performing a simultaneous fit to the angular distributions from the three categories where the R_{EM} is shared.

Results of Magnetic Form Factor of the Neutron

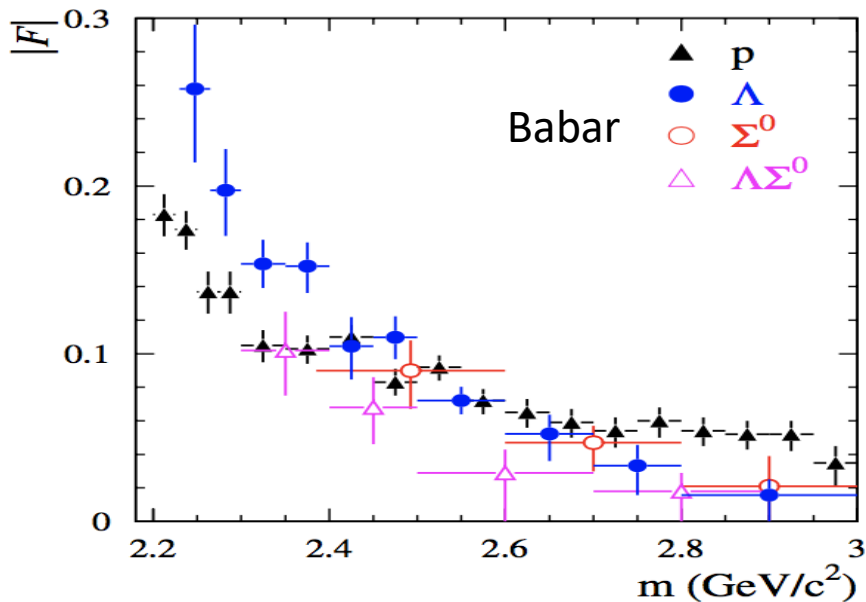


- Comparison of Magnetic Form Factor to the Theoretical Prediction:
 - The only existing results of $|G_M^n|$ are from Fenice, they were determined under the hypothesis $|G_E^n|=0$
 - **A comparison of $|G_M^n|$ results from this analysis to the various theoretical predictions is performed**

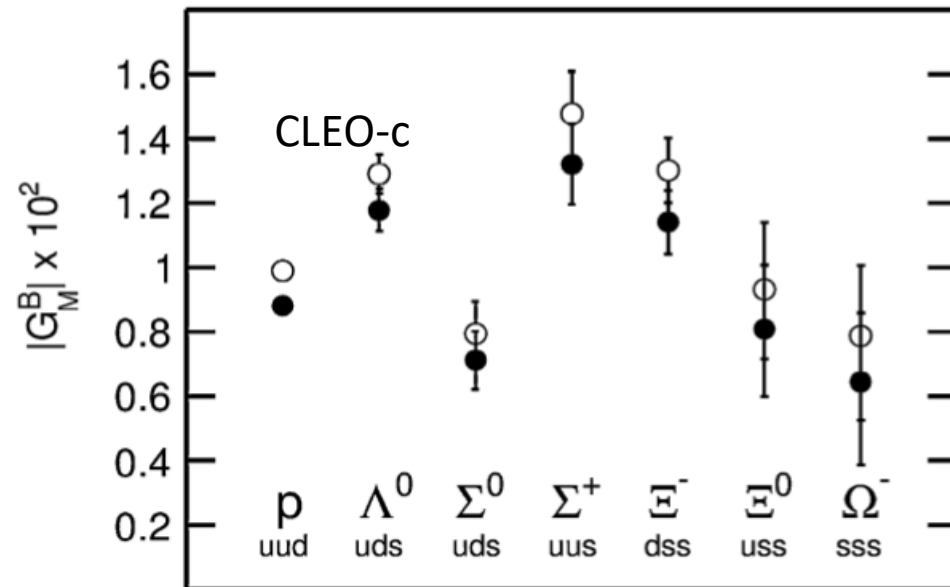
Status on hyperon FFs

- Rare experimental results on **Hyperon FF**

Phys. Rev. D **76**, 092006 (2007)



Phys. Lett. B 739 (2014) 90–94



$q^2 = 14.2$ GeV²

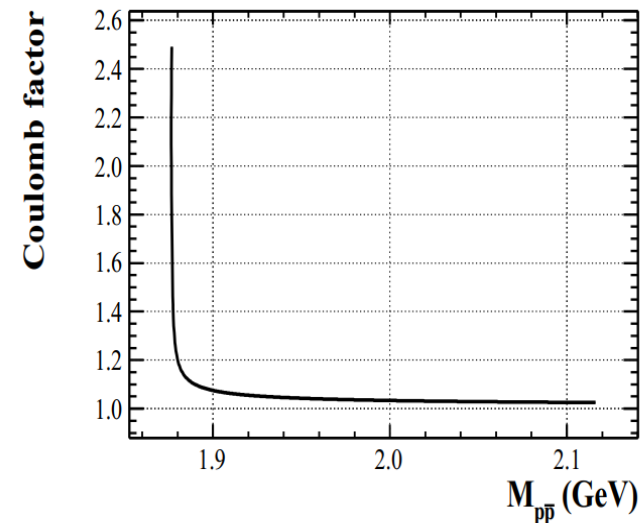
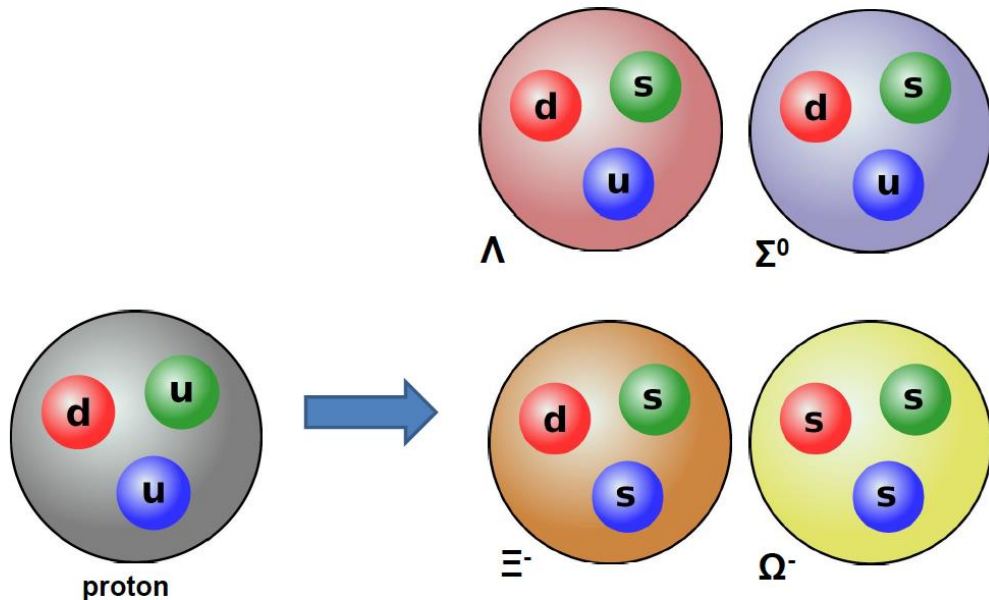
- diquark correlation evidence
- favor spin–isospin singlet

Measurement of Hyperon FFs near threshold

- The Born cross section for $e^+e^- \rightarrow \gamma^* \rightarrow B\bar{B}$, can be expressed in terms of electromagnetic form factor G_E and G_M :

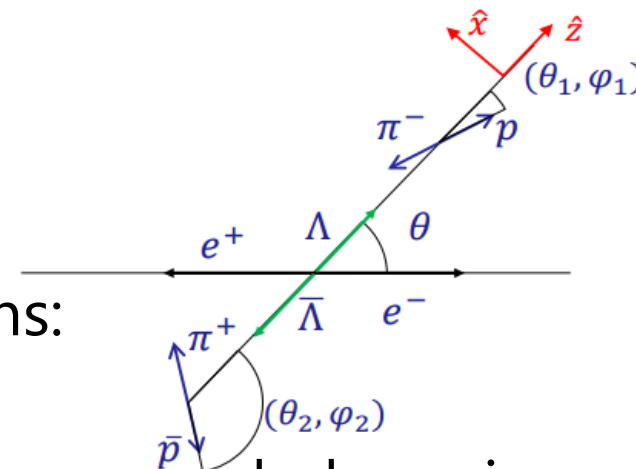
$$\sigma_{B\bar{B}}(q) = \frac{4\pi\alpha^2 C\beta}{3q^2} [|G_M(q)|^2 + \frac{1}{2\tau} |G_E(q)|^2]$$

- The **Coulomb factor** $C = \frac{\pi\alpha}{\beta} \frac{1}{1 - \exp(-\frac{\pi\alpha}{\beta})}$ for a charged $B\bar{B}$ pair, and equals to 1 for a neutral $B\bar{B}$ pair
- Complex form of FFs: $G_E = |G_E|e^{i\Phi_E}$, $G_M = |G_M|e^{i\Phi_M}$; **Relative phase**: $\Delta\Phi = \Phi_E - \Phi_M$



Determination of the Relative phase of FFs

- Complex form of FFs:
 - $G_E = |G_E|e^{i\Phi_E}$, $G_M = |G_M|e^{i\Phi_M}$
 - Relative phase: $\Delta\Phi = \Phi_E - \Phi_M$
- A non-zero phase has polarization effect on the Baryons:
 - $P_y \propto \sin \Delta\Phi$
- The angular distribution of daughter baryon from Hyperon weak decay is:
 - $\frac{d\sigma}{d\Omega} \propto 1 + \alpha_\Lambda \mathbf{P}_y \cdot \hat{\mathbf{q}}$
 - α_Λ : asymmetry parameter
 - $\hat{\mathbf{q}}$: unit vector along the daughter baryon in hyperon rest frame



With hyperon weak decay to B+P, the polarization of hyperon can be measurement, so does the relative phase between G_E and G_M !

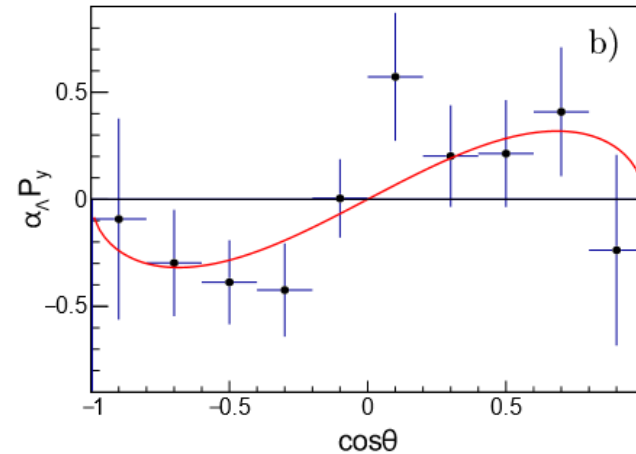
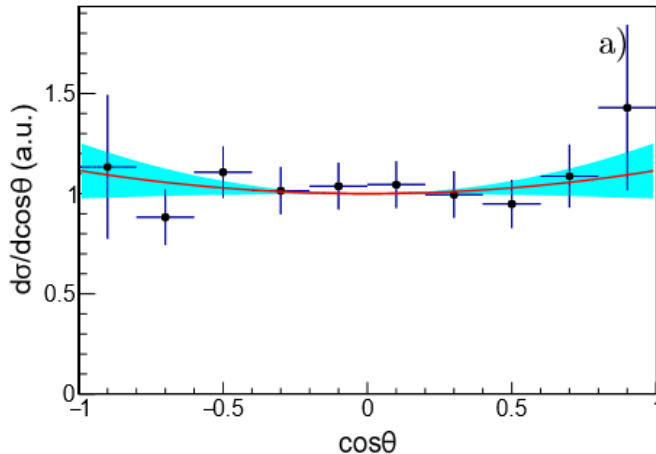
Complete measurement of Λ EMFFs

[arXiv: 1903.09421](https://arxiv.org/abs/1903.09421)

- An event of the reaction $e^+e^- \rightarrow \Lambda(\rightarrow p\pi^-)\bar{\Lambda}(\rightarrow \bar{p}\pi^+)$ is specified by the five dimensional vector $\xi = (\theta, \Omega_1, \Omega_2)$, the differential cross section is:

$$\begin{aligned} \mathcal{W}(\xi) = & \mathcal{T}_0(\xi) + \eta \mathcal{T}_5(\xi) \\ & - \alpha_\Lambda^2 \left(\mathcal{T}_1(\xi) + \sqrt{1 - \eta^2} \cos(\Delta\Phi) \mathcal{T}_2(\xi) + \eta \mathcal{T}_6(\xi) \right) \\ & + \alpha_\Lambda \sqrt{1 - \eta^2} \sin(\Delta\Phi) (\mathcal{T}_3(\xi) - \mathcal{T}_4(\xi)). \end{aligned}$$

Phys.Lett. B772 (2017) 16-20



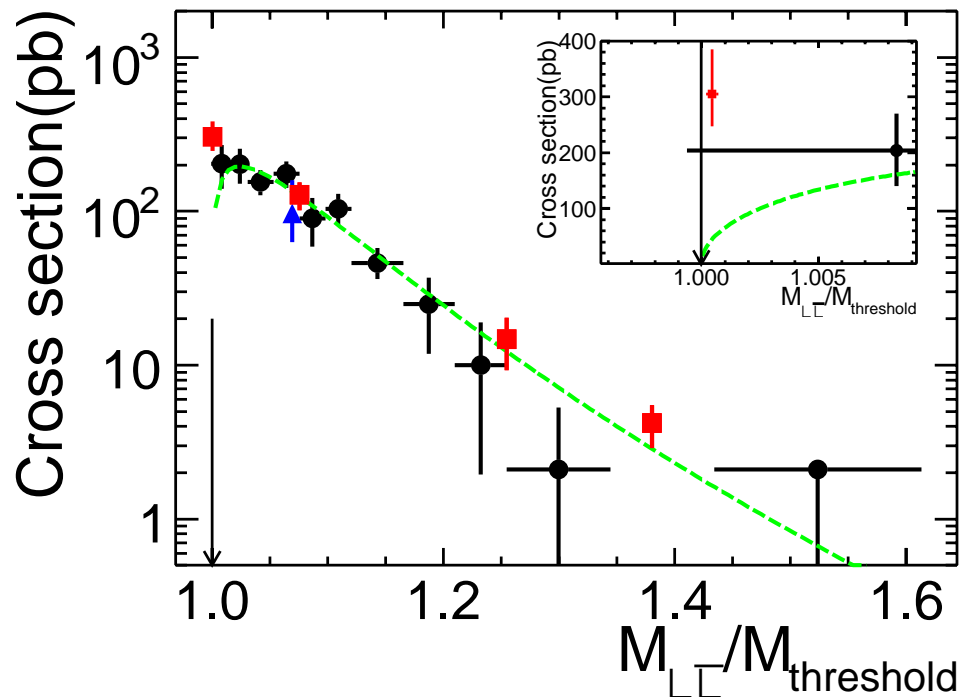
Fit data by Maximum Log Likelihood

$$\begin{aligned} \left| \frac{G_E}{G_M} \right| &= 0.96 \pm 0.14(stat.) \pm 0.02(sys.) \\ \Delta\Phi &= 37^\circ \pm 12^\circ(stat.) \pm 6^\circ(sys.) \end{aligned}$$

Measurement of $e^+e^- \rightarrow \Lambda\bar{\Lambda}$ at $\sqrt{s} = 2.2324$ GeV

Phys. Rev. D 97, 032013 (2018)

- Near threshold production ($2M_\Lambda + 1.0$ MeV) and small PHSP in $\Lambda/\bar{\Lambda}$ decays
- Indirect search for antiproton in $\Lambda \rightarrow p\pi^-$, $\bar{\Lambda} \rightarrow \bar{p}\pi^+$
- Search for mono-energetic π^0 in $\bar{\Lambda} \rightarrow \bar{n}\pi^0$



- The anomalous behavior differing from the pQCD prediction at threshold is observed.

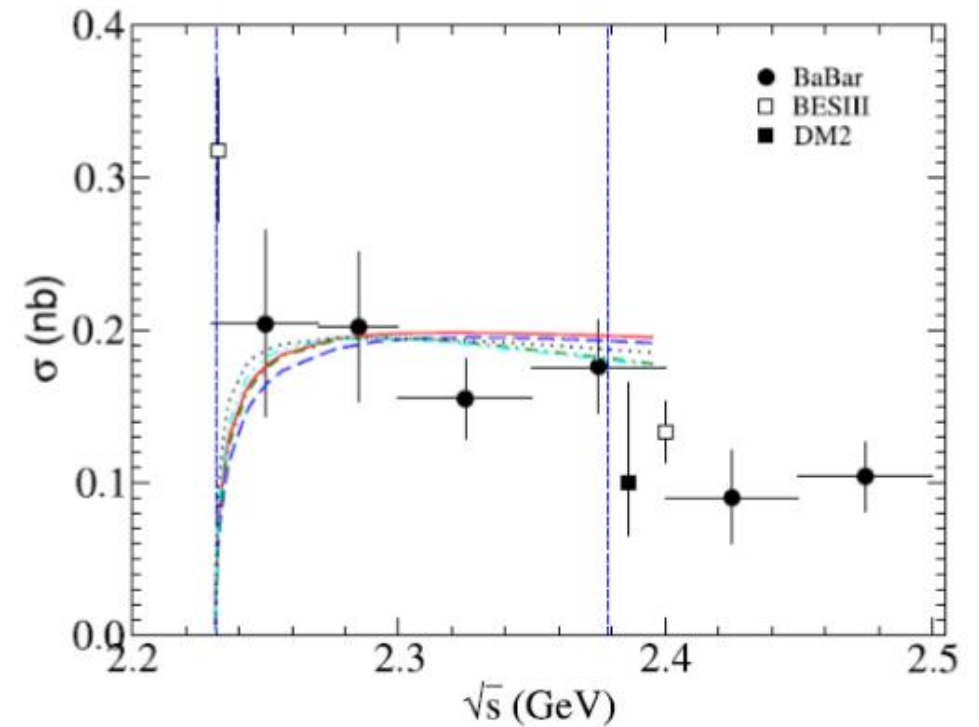
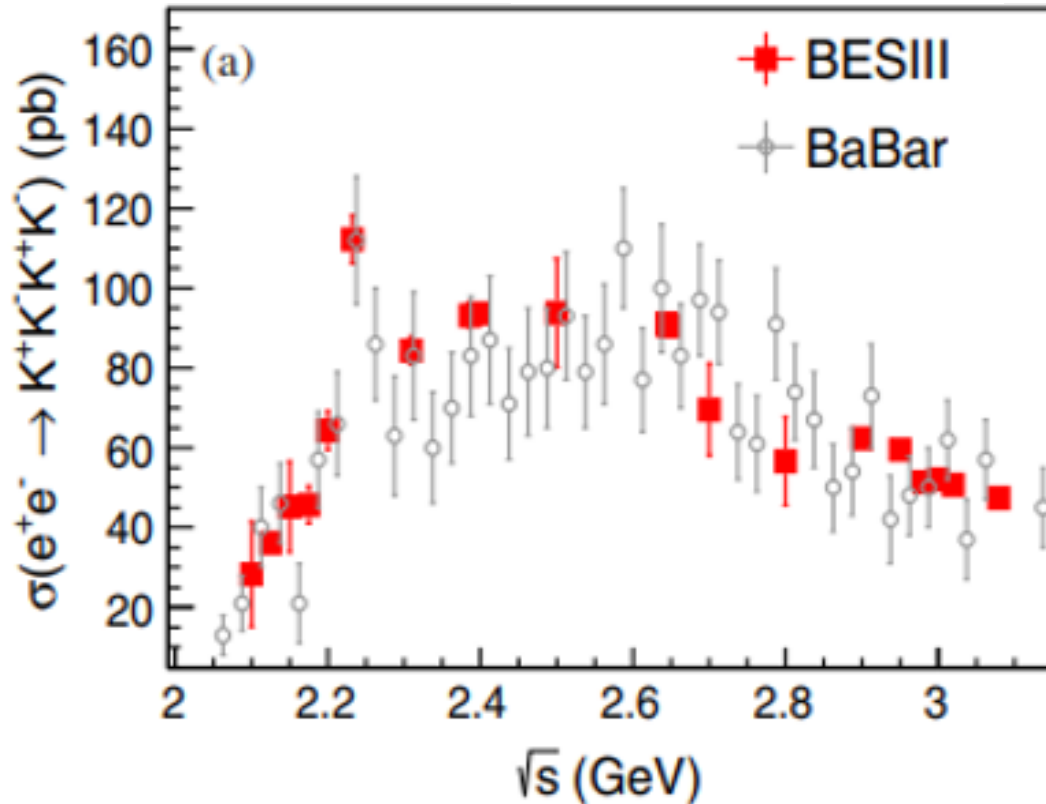
• Recalling the baryon pair production cross section:

$$\sigma_{B\bar{B}}(q) = \frac{4\pi\alpha^2 C \beta}{3q^2} [|G_M(q)|^2 + \frac{1}{2\tau} |G_E(q)|^2]$$

• The Columb correction factor $C = \frac{\pi\alpha}{\beta} \frac{1}{1 - \exp(-\frac{\pi\alpha}{\beta})}(Q)$, cancel the β for a charged $B\bar{B}$ pair, equals to 1 for a neutral $B\bar{B}$ pair

A possible resonance around $\Lambda\bar{\Lambda}$ resonance?

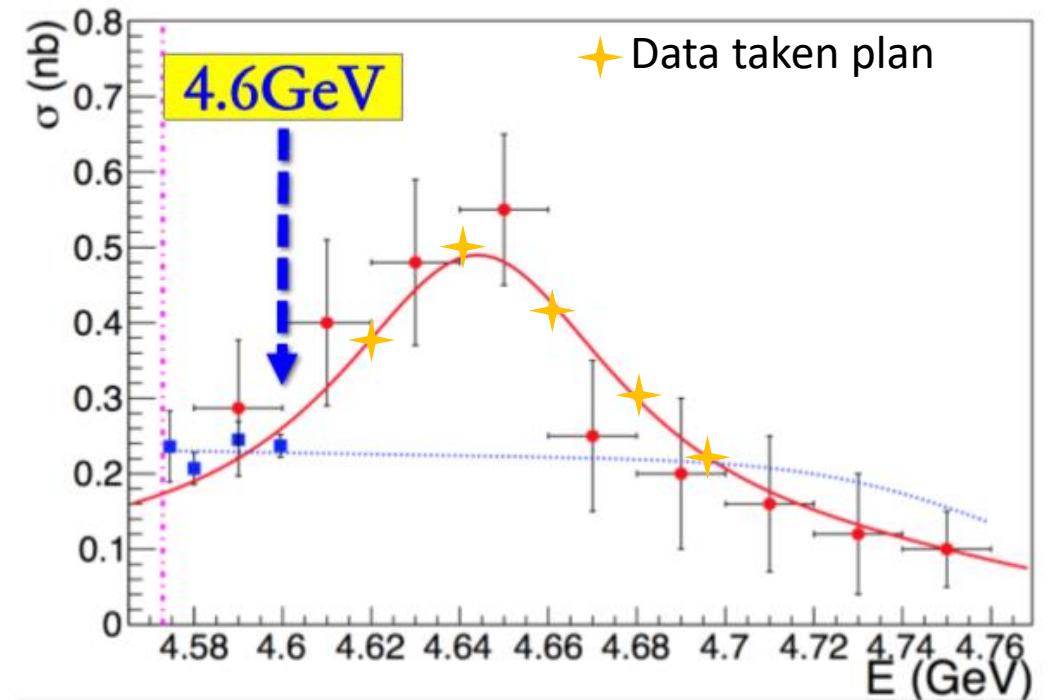
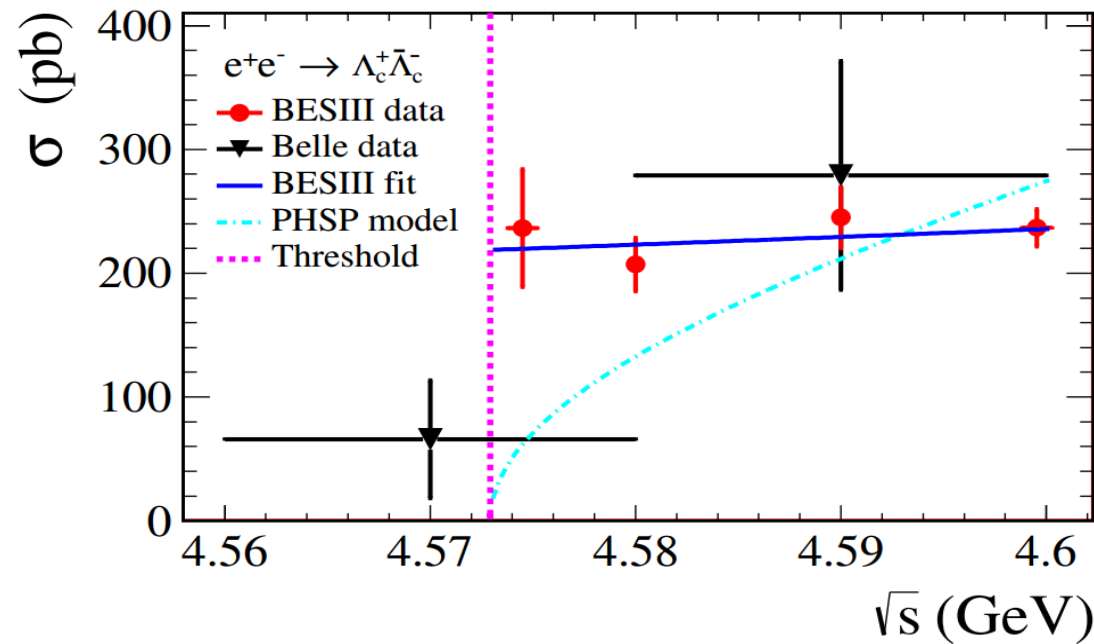
Phys. Rev. D 100, 032009



- A hint for resonance around $\Lambda\bar{\Lambda}$ threshold in $e^+e^- \rightarrow KKKK$ cross section
 - Mass= 2232 ± 3.5 MeV, width ≈ 20 MeV

$e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$ near kinematic threshold

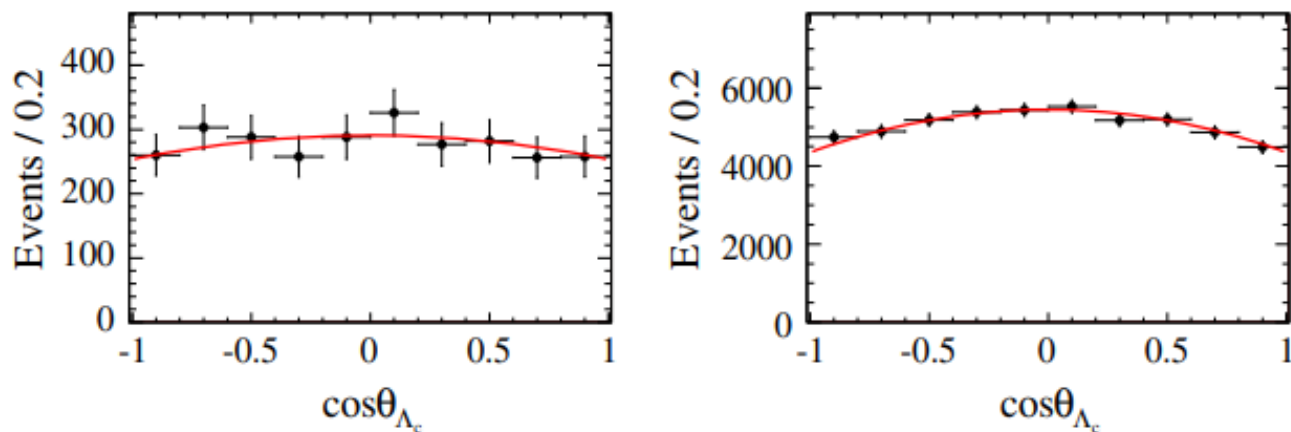
Phys. Rev. Lett. 120, 132001 (2018)



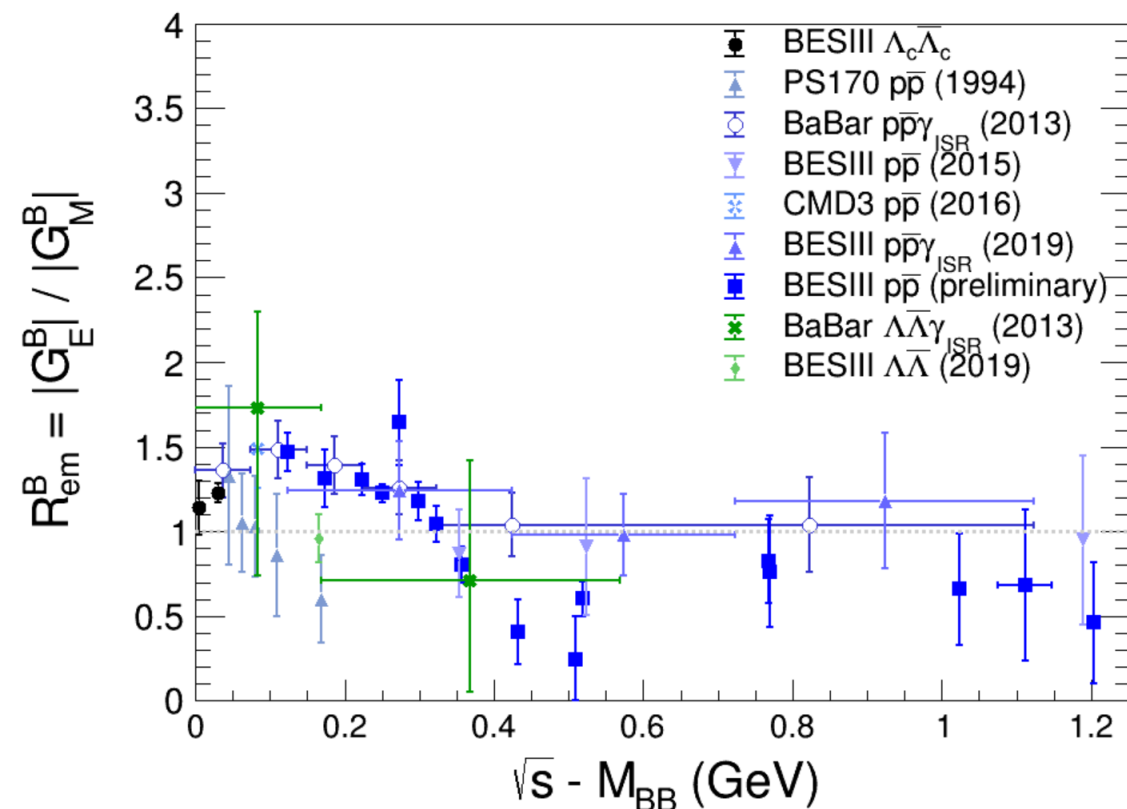
- Ten modes of Λ_c^+ ($\bar{\Lambda}_c^-$) are reconstructed
- Measurement of the Born cross section at 4 energy points below 4.6 GeV with **unprecedented statistical accuracy** ($\sim 1.3\%$ at 4.6 GeV)

$e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$ near kinematic threshold

- Angular distribution study



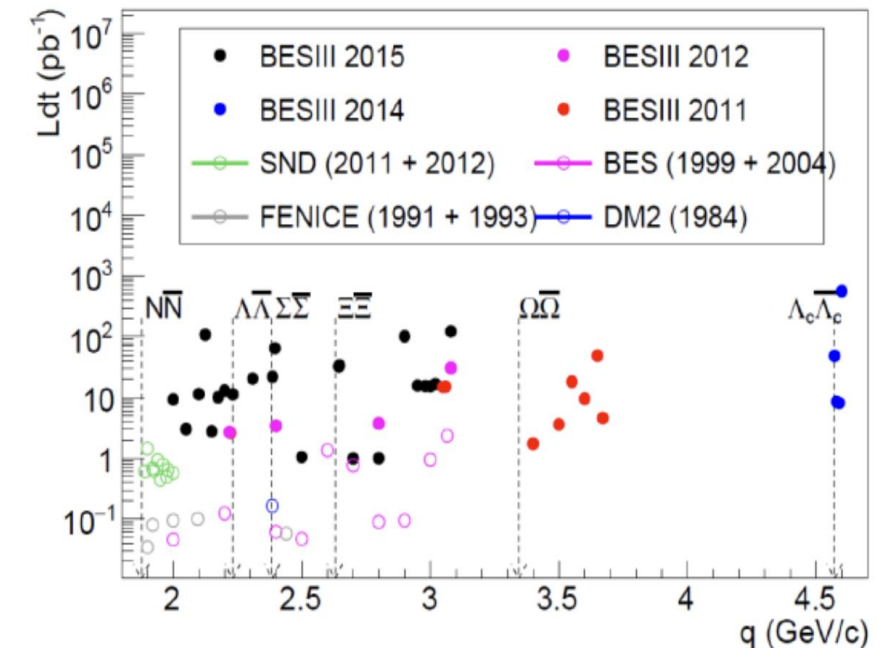
\sqrt{s} (MeV)	α_{Λ_c}	$ G_E/G_M $
4574.5	$-0.13 \pm 0.12 \pm 0.08$	$1.14 \pm 0.14 \pm 0.07$
4599.5	$-0.20 \pm 0.04 \pm 0.02$	$1.23 \pm 0.05 \pm 0.03$



A summary of $|R_{\text{EM}}|$ for measured Baryons

Summary and discussion

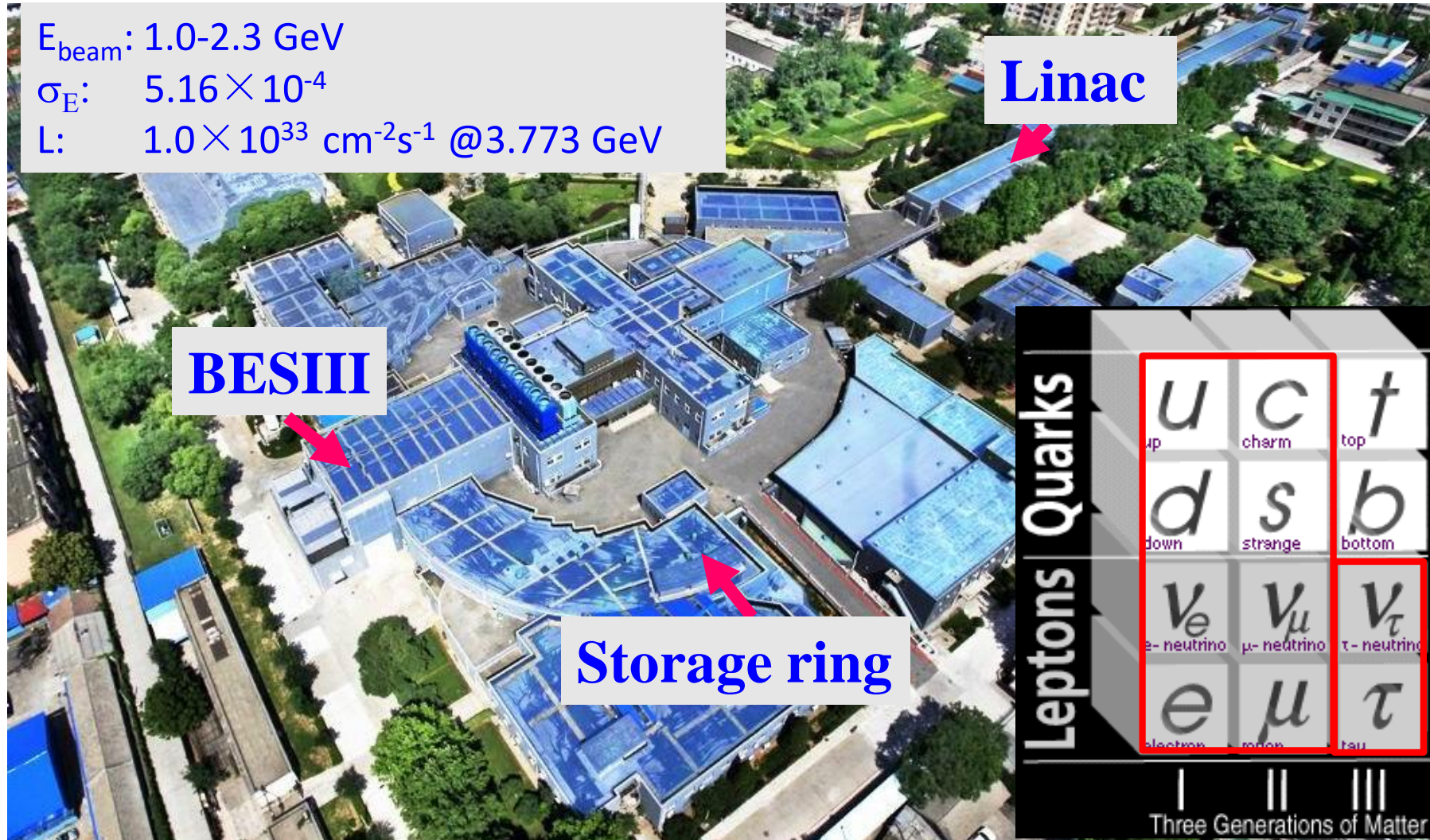
- Nucleon FFs is measured with scan and ISR techniques at BESIII
 - Answered the remaining questions on proton FFs
 - Precise measurement on neutron FFs is ongoing
- With the large data set, more precise results on Hyperon FFs are expected on BESIII.
 - More precise cross section line-shape
 - Search for resonant structure and test di-quark correlation
 - Test on threshold effect
 - Complete determination of G_E and G_M



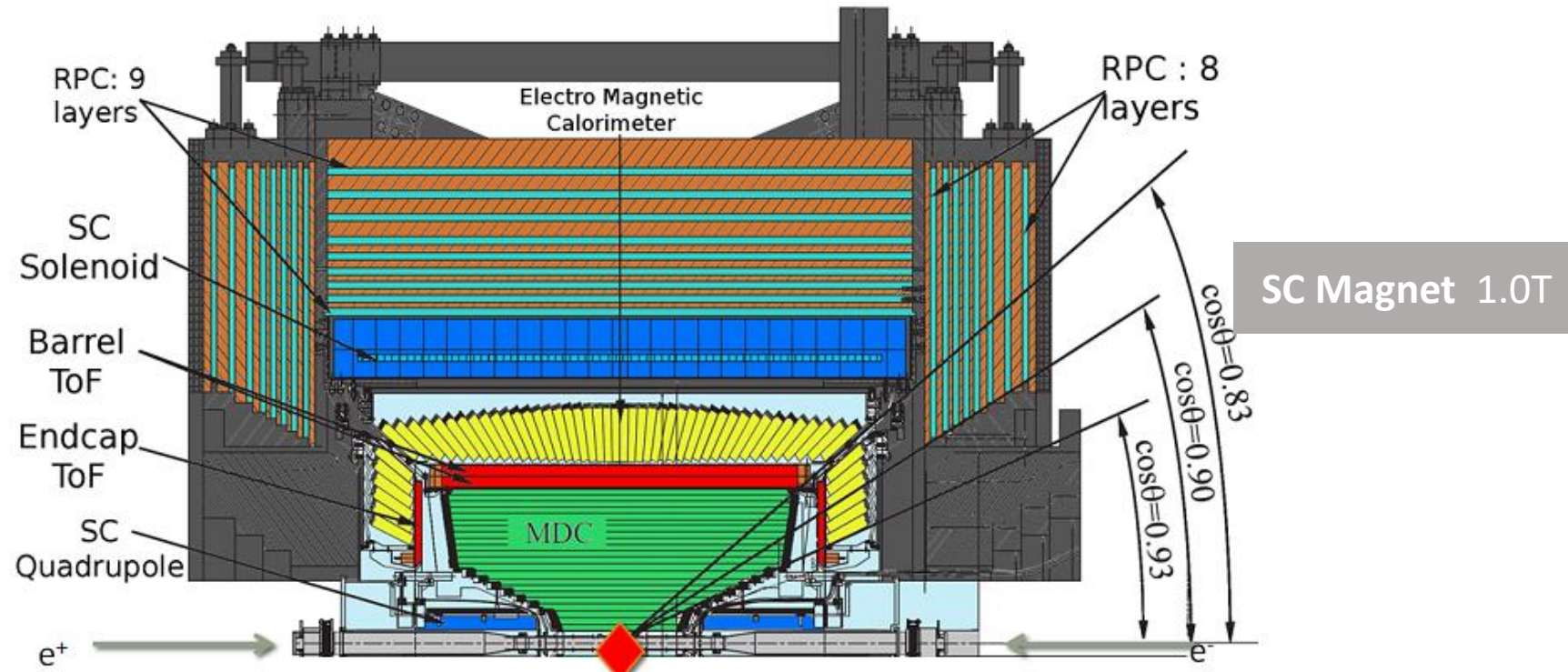
Energy scan in 2014-2015 at BESIII

Thank you for your attention!

Beijing Electron Positron Collider (BEPCII)



BESIII detector



Main Drift Chamber

Small cell, 43 layer

$\sigma_{xy}=130 \mu\text{m}$, $dE/dx \sim 6\%$

$\sigma_p/p = 0.5\%$ at 1 GeV

Time Of Flight

Plastic scintillator

$\sigma_T(\text{barrel}): 80 \text{ ps}$

$\sigma_T(\text{endcap}): 110 \text{ ps}$

(endcap update with MRPC $\sigma_T: 65 \text{ ps}$)

Electromagnetic Calorimeter

CsI(Tl): $L=28 \text{ cm}$ ($15X_0$)

Energy range: 0.02-2GeV

Barrel σ_E 2.5%, σ_l 6mm

Endcap σ_E 5.0%, σ_l 9mm

Muon Counter

Resistive plate chamber

Barrel: 9 layers

Endcaps: 8 layers

$\sigma_{\text{spatial}}: 1.48 \text{ cm}$