



Study of the light baryon states in Λ_c^+ decays

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Workshop of the Baryon Production at BESIII

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Outline

Introduction

Possible $\Sigma_{1/2^-}^(1380)$ state in $\Lambda_c^+ \rightarrow \eta\pi^+\Lambda$ decay*

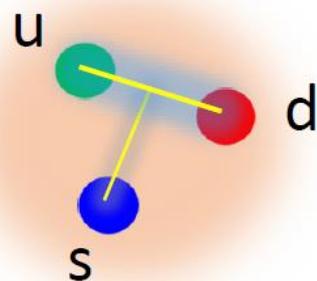
Study of $N^(1535)$ in the $\Lambda_c^+ \rightarrow \bar{K}^0\eta p$ decay*

Possible ϕp state in $\Lambda_c^+ \rightarrow \pi^0\phi p$ decay

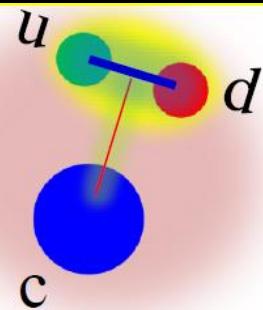
Summary

Λ_c^+

The lightest charmed baryon

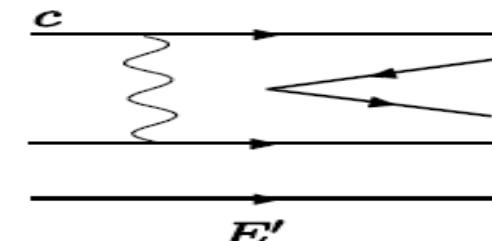
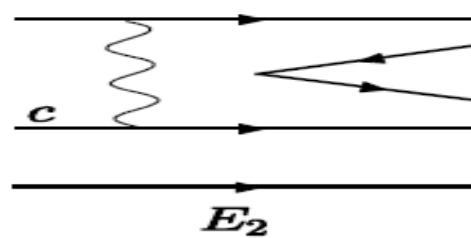
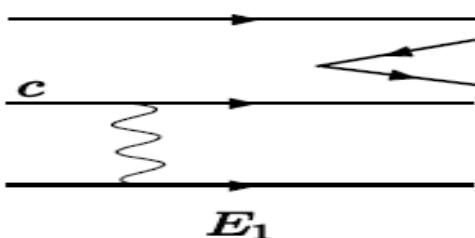
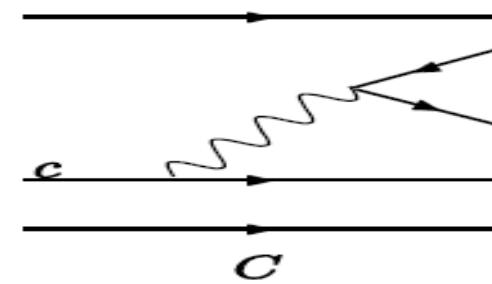
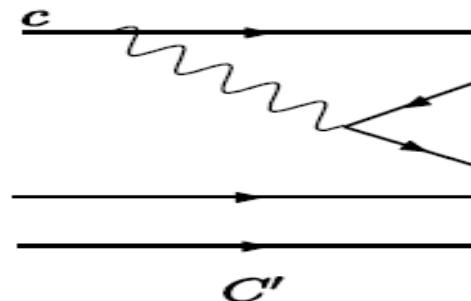
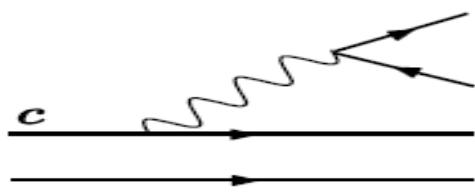
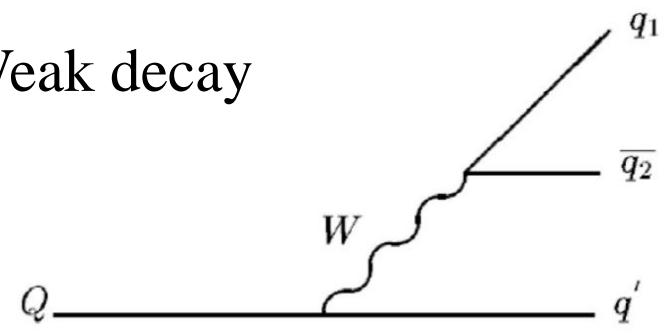


Strange baryons ($\Lambda[\text{uds}]$)
 $m_u, m_d \approx m_s \rightarrow (\text{qqq})$ uniform

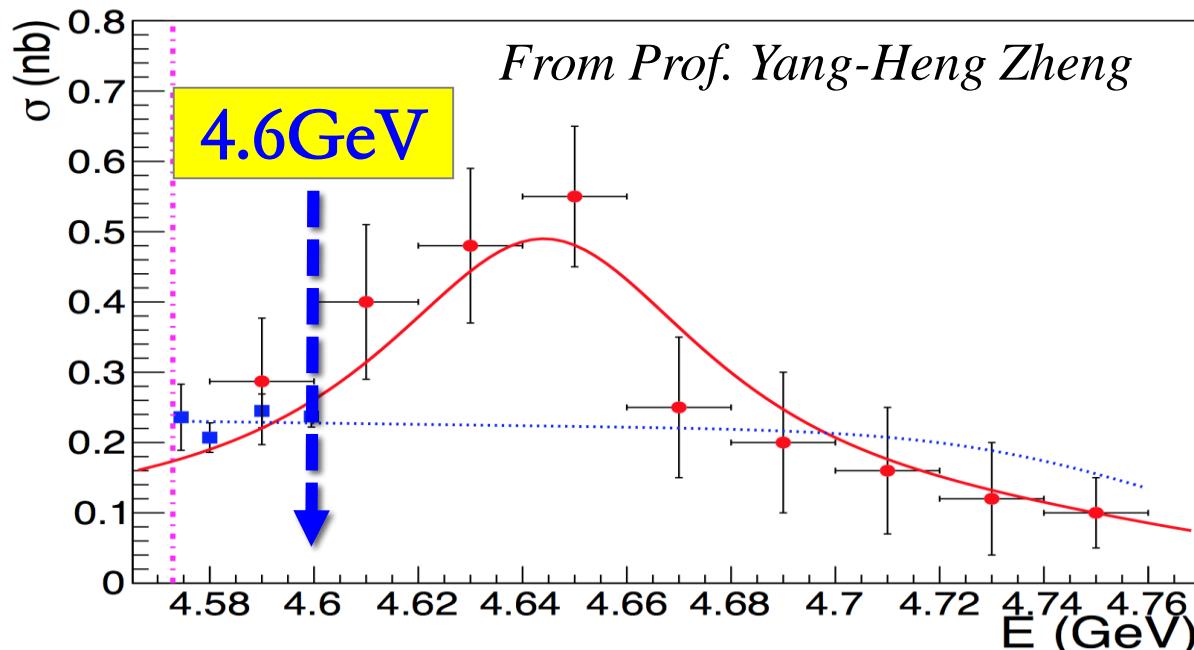
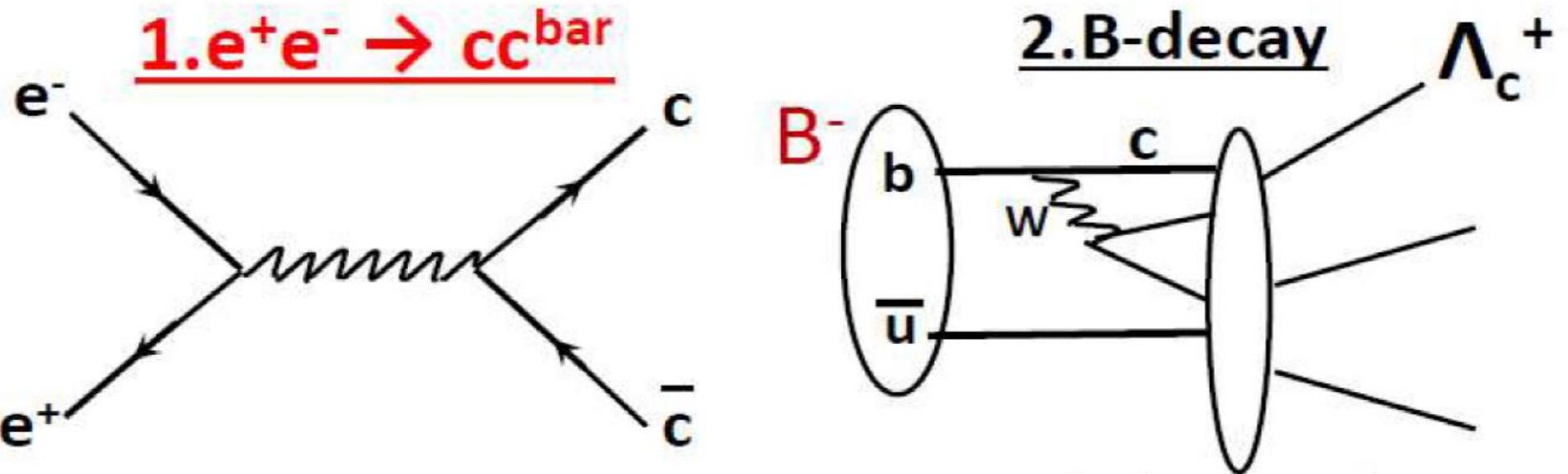


Charmed baryon ($\Lambda_c[\text{udc}]$)
 $m_u, m_d \ll m_c \rightarrow \text{diquark} + \text{quark}$
 $(\text{qq}) \quad (\text{Q})$

Weak decay



Λ_c^+ : production



BESIII data taking
@ $\Lambda_c^+\Lambda_c^-$ threshold

BF precisions improved significantly

PDG2014

$\Gamma(p\bar{K}^0\pi^0)/\Gamma(pK^-\pi^+)$	PDG2014				Γ_7/Γ_2
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	
$0.66 \pm 0.05 \pm 0.07$	774	ALAM	98	CLE2 $e^+e^- \approx \gamma(4S)$	
$\Gamma(p\bar{K}^0\eta)/\Gamma(pK^-\pi^+)$					
Unseen decay modes of the η are included.				Γ_8/Γ_2	
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	
$0.25 \pm 0.04 \pm 0.04$	57	AMMAR	95	CLE2 $e^+e^- \approx \gamma(4S)$	
$\Gamma(p\bar{K}^0\pi^+\pi^-)/\Gamma(pK^-\pi^+)$					
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	Γ_9/Γ_2
0.51 ± 0.06 OUR AVERAGE					
0.52 $\pm 0.04 \pm 0.05$	985	ALAM	98	CLE2 $e^+e^- \approx \gamma(4S)$	
0.43 $\pm 0.12 \pm 0.04$	83	AVERY	91	CLEO $e^+e^- 10.5$ GeV	
0.98 $\pm 0.36 \pm 0.08$	12	BARLAG	90D	NA32 $\pi^- 230$ GeV	
$\Gamma(pK^-\pi^+\pi^0)/\Gamma(pK^-\pi^+)$					
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	Γ_{10}/Γ_2
$0.67 \pm 0.04 \pm 0.11$	2606	ALAM	98	CLE2 $e^+e^- \approx \gamma(4S)$	
$\Gamma(pK^*(892)^-\pi^+)/\Gamma(p\bar{K}^0\pi^+\pi^-)$					
Unseen decay modes of the $K^*(892)^-$ are included.				Γ_{11}/Γ_9	
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	
0.44 ± 0.14	17	ALEEV	94	BIS2 $nN 20-70$ GeV	
$\Gamma(p(K^-\pi^+)_{\text{nonresonant}}\pi^0)/\Gamma(pK^-\pi^+)$					
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	Γ_{12}/Γ_2
$0.73 \pm 0.12 \pm 0.05$	67	BOZEK	93	NA32 $\pi^- Cu 230$ GeV	

PDG2019

$\Gamma(pK_S^0\pi^0)/\Gamma_{\text{total}}$	EVTS	DOCUMENT ID	TECN	COMMENT	Γ_7/Γ
1.96 ± 0.13 OUR FIT				Error includes scale factor of 1.1	
$1.87 \pm 0.13 \pm 0.05$	558	ABLIKIM	16	BES3 $e^+e^- \rightarrow \Lambda_c\bar{\Lambda}_c$, 4.599 GeV	
$\Gamma(pK_S^0\pi^0)/\Gamma(pK^-\pi^+)$					
Measurements given as a \bar{K}^0 ratio have been divided by 2 to convert to a K_S^0 ratio.				Γ_7/Γ_2	
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	
0.314 ± 0.018 OUR FIT					
$0.33 \pm 0.03 \pm 0.04$	774	ALAM	98	CLE2 $e^+e^- \approx \gamma(4S)$	
$\Gamma(nK_S^0\pi^+)/\Gamma_{\text{total}}$					
VALUE (%)	EVTS	DOCUMENT ID	TECN	COMMENT	Γ_8/Γ
$1.82 \pm 0.23 \pm 0.11$	83	ABLIKIM	17H	BES3 e^+e^- at 4.6 GeV	
$\Gamma(p\bar{K}^0\eta)/\Gamma(pK^-\pi^+)$					
Unseen decay modes of the η are included.				Γ_9/Γ_2	
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	
$0.25 \pm 0.04 \pm 0.04$	57	AMMAR	95	CLE2 $e^+e^- \approx \gamma(4S)$	
$\Gamma(pK_S^0\pi^+\pi^-)/\Gamma_{\text{total}}$					
VALUE (%)	EVTS	DOCUMENT ID	TECN	COMMENT	Γ_{10}/Γ
1.59 ± 0.12 OUR FIT				Error includes scale factor of 1.2	
$1.53 \pm 0.11 \pm 0.09$	485	ABLIKIM	16	BES3 $e^+e^- \rightarrow \Lambda_c\bar{\Lambda}_c$, 4.599 GeV	
$\Gamma(pK_S^0\pi^+\pi^-)/\Gamma(pK^-\pi^+)$					
Measurements given as a \bar{K}^0 ratio have been divided by 2 to convert to a K_S^0 ratio.				Γ_{10}/Γ_2	
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	
0.255 ± 0.015 OUR FIT				Error includes scale factor of 1.1.	
0.257 ± 0.031 OUR AVERAGE					
0.26 $\pm 0.02 \pm 0.03$	985	ALAM	98	CLE2 $e^+e^- \approx \gamma(4S)$	
0.22 $\pm 0.06 \pm 0.02$	83	AVERY	91	CLEO $e^+e^- 10.5$ GeV	
0.49 $\pm 0.18 \pm 0.04$	12	BARLAG	90D	NA32 $\pi^- 230$ GeV	
$\Gamma(pK^-\pi^+\pi^0)/\Gamma_{\text{total}}$					
VALUE (%)	EVTS	DOCUMENT ID	TECN	COMMENT	Γ_{11}/Γ
4.42 ± 0.31 OUR FIT				Error includes scale factor of 1.5	
$4.53 \pm 0.23 \pm 0.30$	1849	ABLIKIM	16	BES3 $e^+e^- \rightarrow \Lambda_c\bar{\Lambda}_c$, 4.599 GeV	
$\Gamma(pK^-\pi^+\pi^0)/\Gamma(pK^-\pi^+)$					
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	Γ_{11}/Γ_2

- BFs of many Λ_c decays: improved significantly
- $\text{BF}(\Lambda_c^+ \rightarrow pK\pi)$: model dependent \Rightarrow model independent
- New decay channels observed: i.e. Λ_c^+ decay involving the neutron in the final state; more SCS decays

From Prof. Yang-Heng Zheng

Introduction

Λ_c^+ two body decays

Non-leptonic two-body weak decays of $\Lambda_c(2286)$

Physics Letters B 776 (2018) 265–269

C.Q. Geng^{a,b,*}, Y.K. Hsiao^{a,b}, Yu-Heng Lin^b, Liang-Liang Liu^a

The branching ratios of the $\Lambda_b \rightarrow B_n M$ decays, where the 2nd column is for our results, where the errors come from the parameters in Eq. (18), while 3, 4, ..., 7 ones correspond to the studies by the heavy quark effective theory (HQET) [24], Sharma and Verma (SV) in Ref. [23], pole model (PM) [11], current algebra (CA) [11] and data [1–3], respectively.

Branching ratios	Our results	HQET [24]	SV [23]	PM [11]	CA [11]	Data [1–3]
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow p \bar{K}^0)$	3.3 ± 0.2	1.23	2.67 ± 0.74	1.20	3.46	3.16 ± 0.16
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda \pi^+)$	1.3 ± 0.2	1.17	–	0.84	1.39	1.30 ± 0.07
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)$	1.3 ± 0.2	0.69	–	0.68	1.67	1.24 ± 0.10
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+)$	1.3 ± 0.2	0.69	0.87 ± 0.20	0.68	1.67	1.29 ± 0.07
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Xi^0 K^+)$	0.5 ± 0.1	0.07	–	–	–	0.50 ± 0.12
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \pi^0)$	5.6 ± 1.5	–	2	–	–	–
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda K^+)$	4.6 ± 0.9	–	14	–	–	6.1 ± 1.2
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 K^+)$	4.0 ± 0.8	–	4	–	–	5.2 ± 0.8
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ K^0)$	8.0 ± 1.6	–	9	–	–	–
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta)$	0.7 ± 0.4	0.25	0.50 ± 0.17	–	–	0.70 ± 0.23
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta')$	$1.0^{+1.6}_{-0.8}$	0.08	0.20 ± 0.08	–	–	–
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \eta)$	12.4 ± 4.1	–	21	–	–	12.4 ± 3.0
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \eta')$	$12.2^{+14.3}_{-8.7}$	–	4	–	–	–

[11] H.Y. Cheng, B. Tseng, Phys. Rev. D 48 (1993) 4188.

[23] K.K. Sharma, R.C. Verma, Phys. Rev. D 55 (1997) 7067.

[24] K.K. Sharma, R.C. Verma, Eur. Phys. J. C 7 (1999) 217.

Λ_c^+ three body decays

PHYSICAL REVIEW D **93**, 056008 (2016)

Test flavor SU(3) symmetry in exclusive Λ_c decays

Cai-Dian Lü,^{1,*} Wei Wang,^{2,3,†} and Fu-Sheng Yu^{4,‡}

$$\begin{aligned} \mathcal{A}(\Lambda_c \rightarrow p\bar{K}^0\pi^0) &= \frac{1}{\sqrt{2}}\mathcal{A}^{(1)}, & \sqrt{2}\mathcal{A}(\Lambda_c \rightarrow p\bar{K}^0\pi^0) + \mathcal{A}(\Lambda_c \rightarrow pK^-\pi^+) \\ \mathcal{A}(\Lambda_c \rightarrow pK^-\pi^+) &= -\frac{1}{2}\mathcal{A}^{(1)} + \frac{1}{\sqrt{2}}\mathcal{A}^{(2)}, & + \mathcal{A}(\Lambda_c \rightarrow n\bar{K}^0\pi^+) = 0. \\ \mathcal{A}(\Lambda_c \rightarrow n\bar{K}^0\pi^+) &= -\frac{1}{2}\mathcal{A}^{(1)} - \frac{1}{\sqrt{2}}\mathcal{A}^{(2)}. \end{aligned}$$

Three-body charmed baryon Decays with SU(3) flavor symmetry

C.Q. Geng^{1,2,3}, Y.K. Hsiao¹, Chia-Wei Liu² and Tien-Hsueh Tsai²

Phys. Rev. D **99**, 073003 (2019)

$$R(\Delta) \equiv T(\Lambda_c^+ \rightarrow n\bar{K}^0\pi^+) - T(\Lambda_c^+ \rightarrow pK^-\pi^+) - \sqrt{2}T(\Lambda_c^+ \rightarrow p\bar{K}^0\pi^0) = 0.$$

$$T(\Lambda_c^+ \rightarrow \Sigma^+\pi^0\pi^0) - T(\Lambda_c^+ \rightarrow \Sigma^+\pi^+\pi^-) + \frac{1}{2}T(\Lambda_c^+ \rightarrow \Sigma^-\pi^+\pi^+) = 0,$$

$$T(\Lambda_c^+ \rightarrow \Sigma^+K^0\bar{K}^0) - T(\Lambda_c^+ \rightarrow \Sigma^+K^+K^-) - \sqrt{2}T(\Lambda_c^+ \rightarrow \Sigma^0K^+\bar{K}^0) = 0,$$

$$T(\Lambda_c^+ \rightarrow \Xi^0\pi^+K^0) - T(\Lambda_c^+ \rightarrow \Xi^-\pi^+K^+) - \sqrt{2}T(\Lambda_c^+ \rightarrow \Xi^0\pi^0K^+) = 0.$$

Λ_c^+ three body decays

PHYSICAL REVIEW D 93, 056008 (2016)

Test flavor SU(3) symmetry in exclusive Λ_c decays

Cai-Dian Lü,^{1,*} Wei Wang,^{2,3,†} and Fu-Sheng Yu^{4,‡}

$$\begin{aligned} \mathcal{A}(\Lambda_c \rightarrow p\bar{K}^0\pi^0) &= \frac{1}{\sqrt{2}}\mathcal{A}^{(1)}, \\ \mathcal{A}(\Lambda_c \rightarrow pK^-\pi^+) &= -\frac{1}{2}\mathcal{A}^{(1)} + \frac{1}{\sqrt{2}}\mathcal{A}^{(2)}, \\ \mathcal{A}(\Lambda_c \rightarrow n\bar{K}^0\pi^+) &= -\frac{1}{2}\mathcal{A}^{(1)} - \frac{1}{\sqrt{2}}\mathcal{A}^{(2)}. \end{aligned} \quad \xrightarrow{\text{Feynman diagrams}} \quad \begin{aligned} &\sqrt{2}\mathcal{A}(\Lambda_c \rightarrow p\bar{K}^0\pi^0) + \mathcal{A}(\Lambda_c \rightarrow pK^-\pi^+) \\ &+ \mathcal{A}(\Lambda_c \rightarrow n\bar{K}^0\pi^+) = 0. \end{aligned}$$

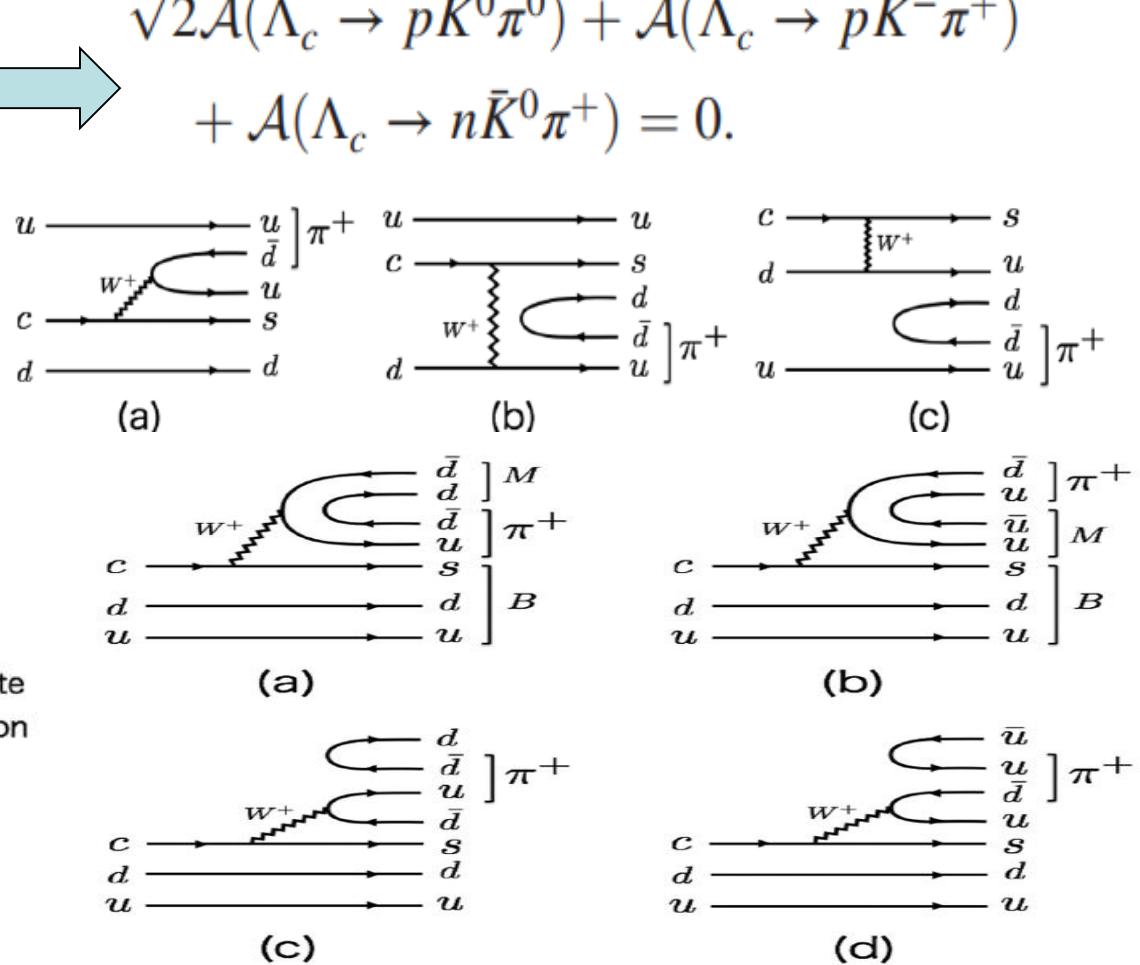
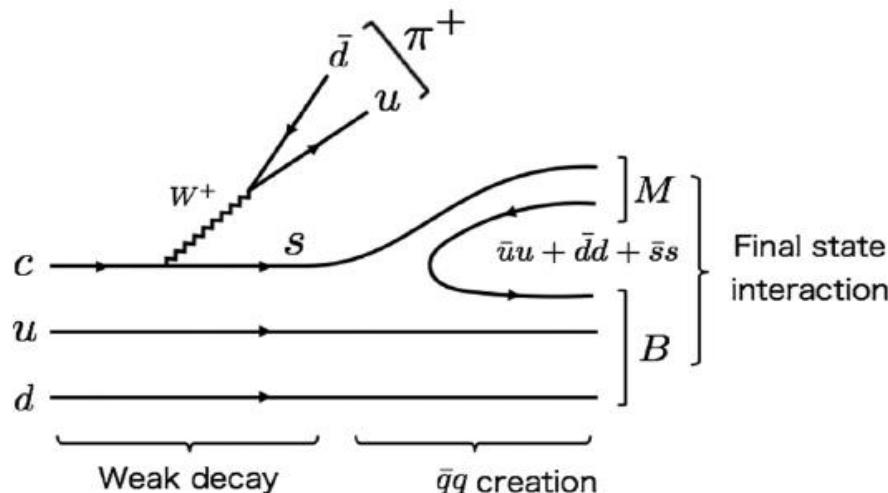


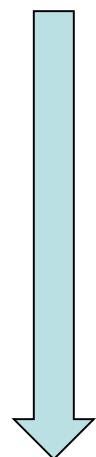
FIG. 1. The dominant diagram for the $\Lambda_c^+ \rightarrow \pi^+ MB$ decay. The solid lines and the wiggly line show the quarks and the W boson, respectively.

K. Miyahara, T. Hyodo, and E. Oset, Phys. Rev. C 92, 055204 (2015).

Weak decay of Λ_c^+ for the study of $\Lambda(1405)$ and $\Lambda(1670)$

$$|MB\rangle = \frac{1}{\sqrt{2}} |s(\bar{u}u + \bar{d}d + \bar{s}s)(ud - du)\rangle \\ = \frac{1}{\sqrt{2}} \sum_{i=1}^3 |P_{3i} q_i (ud - du)\rangle,$$

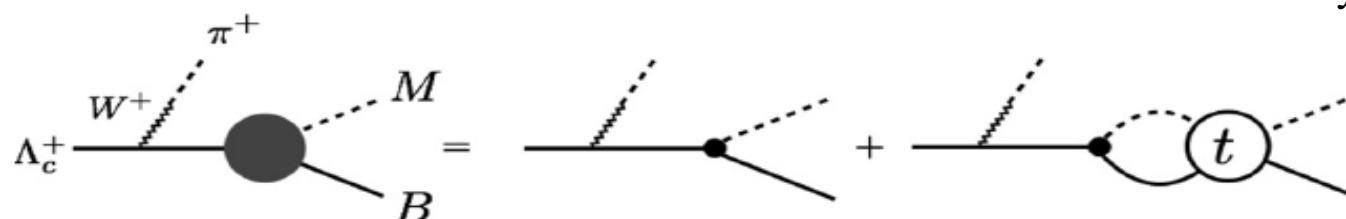
$$q \equiv \begin{pmatrix} u \\ d \\ s \end{pmatrix}, \quad P \equiv q\bar{q} = \begin{pmatrix} u\bar{u} & u\bar{d} & u\bar{s} \\ d\bar{u} & d\bar{d} & d\bar{s} \\ s\bar{u} & s\bar{d} & s\bar{s} \end{pmatrix}.$$



$$\begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{3}} + \frac{\eta'}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{3}} + \frac{\eta'}{\sqrt{6}} & K^0 \\ K^- & \bar{K}^0 & -\frac{\eta}{\sqrt{3}} + \frac{2\eta'}{\sqrt{6}} \end{pmatrix}$$

$$|MB\rangle = |K^- p\rangle + |\bar{K}^0 n\rangle - \frac{\sqrt{2}}{3} |\eta \Lambda\rangle.$$

K. Miyahara, T. Hyodo, and E. Oset,
Phys. Rev. C 92, 055204 (2015).

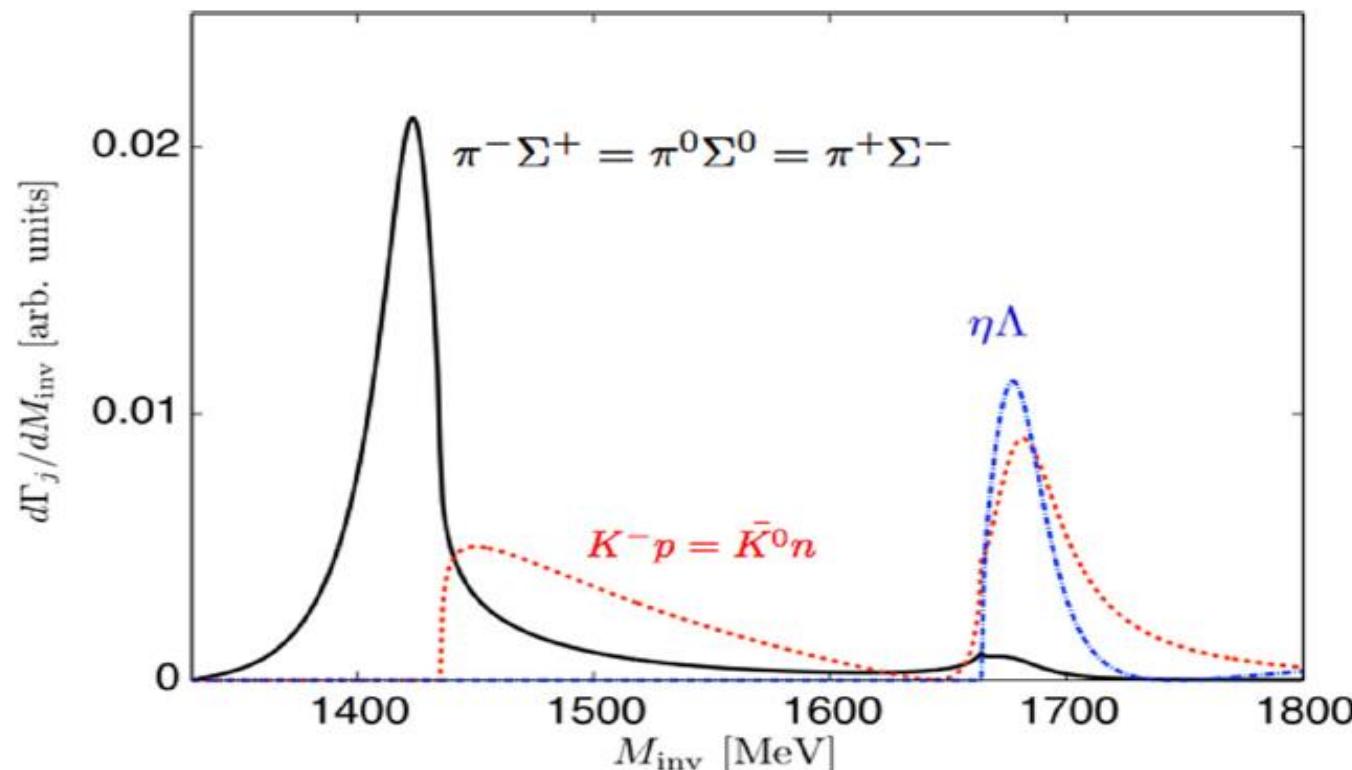


$$\mathcal{M}_j = V_P \left[h_j + \sum_i h_i G_i(M_{\text{inv}}) t_{ij}(M_{\text{inv}}) \right],$$

$$h_{\pi^0\Sigma^0} = h_{\pi^-\Sigma^+} = h_{\pi^+\Sigma^-} = h_{\pi^0\Lambda} = 0,$$

$$h_{K^-p} = h_{\bar{K}^0n} = 1, \quad h_{\eta\Lambda} = -\frac{\sqrt{2}}{3}, \quad \frac{d\Gamma_j}{dM_{\text{inv}}} = \frac{1}{(2\pi)^3} \frac{p_{\pi^+}\tilde{p}_j M_{\Lambda_c^+} M_j}{M_{\Lambda_c^+}^2} |\mathcal{M}_j|^2,$$

$$h_{\eta\Sigma^0} = h_{K^+\Xi^-} = h_{K^0\Xi^0} = 0,$$



Quark Model Predictions

A possible Σ^* state with spin-parity $J^P = \frac{1}{2}^-$

	(Y, I)	I_3	Flavor wave functions	Masses (MeV)
p_8	$(1, \frac{1}{2})$	$\frac{1}{2}$	$[su][ud]_- \bar{s}$	1460
n_8		$-\frac{1}{2}$	$[ds][ud]_- \bar{s}$	1460
Σ_8^+	$(0, 1)$	1	$[su][ud]_- \bar{d}$	1360
Σ_8^0		0	$\frac{1}{\sqrt{2}}([su][ud]_- \bar{u} + [ds][ud]_- \bar{d})$	1360
Σ_8^-		-1	$[ds][ud]_- \bar{u}$	1360
Λ_8	$(0, 0)$	0	$\frac{[ud][su]_- \bar{u} + [ds][ud]_- \bar{d} - 2[su][ds]_- \bar{s}}{\sqrt{6}}$	1533
Ξ_8^0	$(-1, \frac{1}{2})$	$\frac{1}{2}$	$[ds][su]_- \bar{d}$	1520
Ξ_8^-		$-\frac{1}{2}$	$[ds][su]_- \bar{u}$	1520
Λ_1	$(0, 0)$	0	$\frac{[ud][su]_- \bar{u} + [ds][ud]_- \bar{d} + [su][ds]_- \bar{s}}{\sqrt{3}}$	1447

TABLE II: Flavor wave functions and masses of the $\frac{1}{2}^-$ pentaquark octet and singlet.

Ao Zhang, Y. R. Liu, P.Z. Huang, W.Z. Deng, X.L. Chen and S.L. Zhu, High Energy Phys. Nucl. Phys. 29, 250 (2005).

Other Model Predictions

Chiral dynamics in the presence of bound states:
kaon–nucleon interactions revisited

J.A. Oller, Ulf-G. Meißner

Chiral dynamics of the two $\Lambda(1405)$ states

D. Jido^{a,c}, J.A. Oller^{b,*}, E. Oset^c, A. Ramos^d, U.-G. Meißner^e

Nuclear Physics A 725 (2003) 181–200

PHYSICAL REVIEW D 84, 056017 (2011)

Odd-parity light baryon resonances

Physics Letters B 500 (2001) 263–272

z_R	$1401 + 40i$	
$(I = 1)$	g_i	$ g_i $
$\pi \Lambda$	$0.60 + 0.47i$	0.76
$\pi \Sigma$	$1.27 + 0.71i$	1.5
$\bar{K}N$	$-1.24 - 0.73i$	1.4
$\eta \Sigma$	$0.56 + 0.41i$	0.69
$K\Xi$	$0.12 + 0.05i$	0.13

D. Gamermann,^{1,2,*} C. García-Recio,^{3,4,†} J. Nieves,^{5,‡} and L.L. Salcedo^{3,4,§}

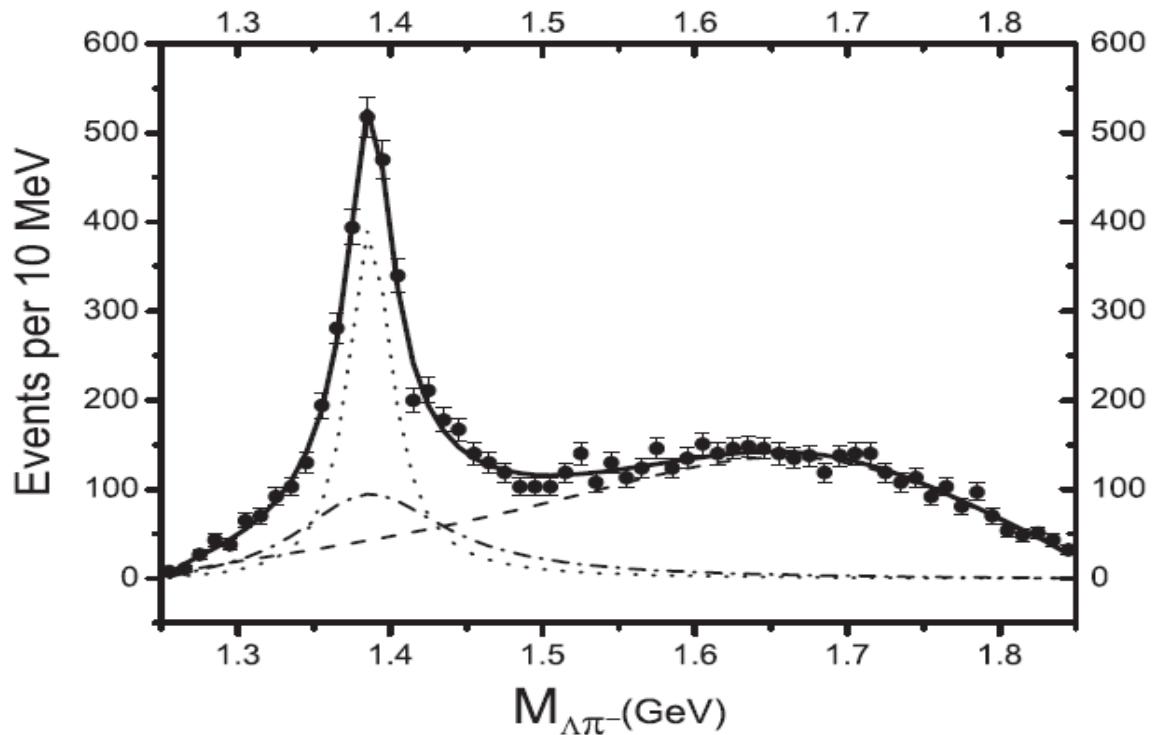
Cusp or “resonance” around the $\bar{K}N$ threshold

J.A. Oller, Eur. Phys. J. A 28, 63–82 (2006). Zhi-Hui Guo and J. A. Oller, PRC 87, 035202 (2013).

L. Roca and E. Oset, PRC 88, 055206 (2013).

K. P. Khemchandani, A. Martinez Torres, and J. A. Oller, arXiv:1810.09990v1.

in the fit. Two type of fits are found as a result. In both cases, the properties of $\Lambda(1405)$ are well reproduced. In addition to this, a Σ state is also found with mass around 1400 MeV. Cross sections,

Evidence for a new Σ^* resonance with $J^P = 1/2^-$ in the old data of the $K^- p \rightarrow \Lambda \pi^+ \pi^-$ reactionJia-Jun Wu,¹ S. Dulat,^{2,3} and B. S. Zou^{1,3}

	$M_{\Sigma^*(3/2)}$	$\Gamma_{\Sigma^*(3/2)}$
Fit1	1385.3 ± 0.7	46.9 ± 2.5
Fit2	$1386.1^{+1.1}_{-0.9}$	$34.9^{+5.1}_{-4.9}$
	$M_{\Sigma^*(1/2)}$	$\Gamma_{\Sigma^*(1/2)}$
	$1381.3^{+4.9}_{-8.3}$	$118.6^{+55.2}_{-35.1}$

Possible evidence for the Σ^* resonance with $J^P = 1/2^-$ around 1380 MeV

PHYSICAL REVIEW C 81, 055203 (2010)

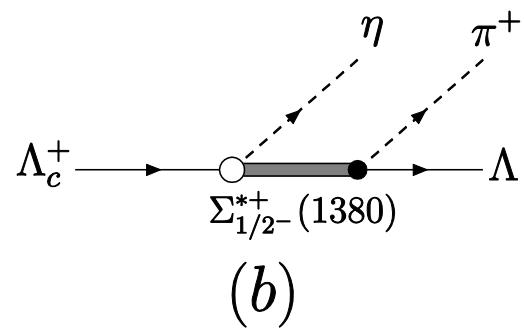
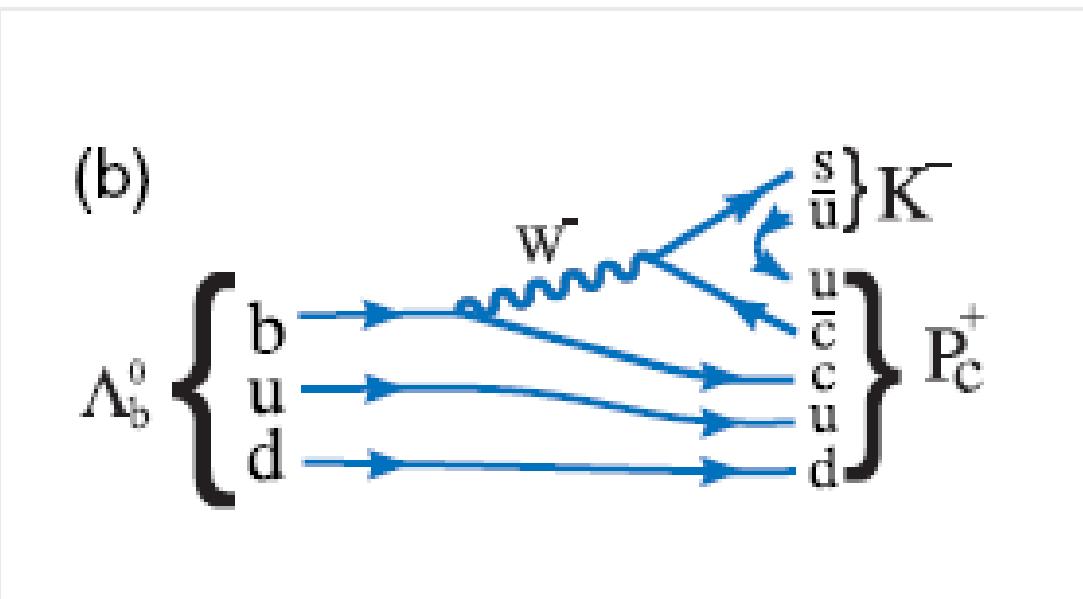
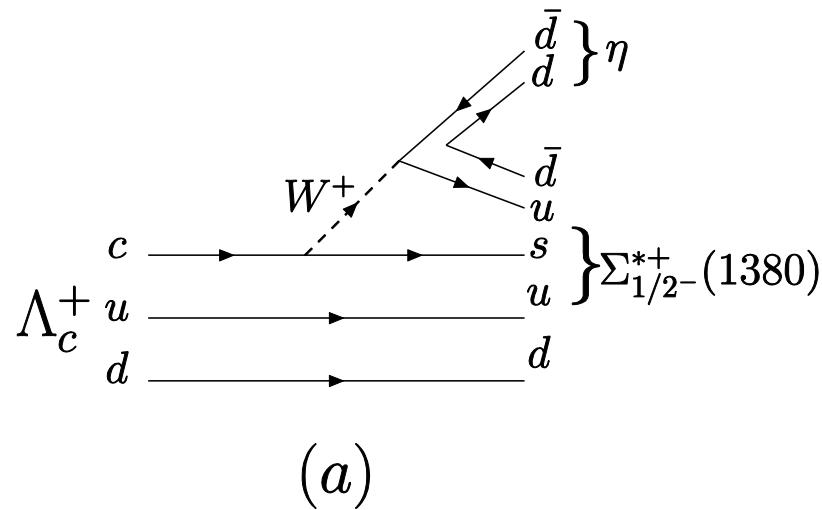
Jia-Jun Wu,¹ S. Dulat,^{2,3} and B. S. Zou^{1,3}**Possible $\Sigma(\frac{1}{2}^-)$ under the $\Sigma^*(1385)$ peak in $K\Sigma^*$ photoproduction**

Puze Gao, Jia-Jun Wu, and B. S. Zou

Yun-Hua Chen and B. S. Zou, PRC 88, 024304 (2013).

Ju-Jun Xie, Jia-Jun Wu, and Bing-Song Zou, PRC 90, 055204 (2014).

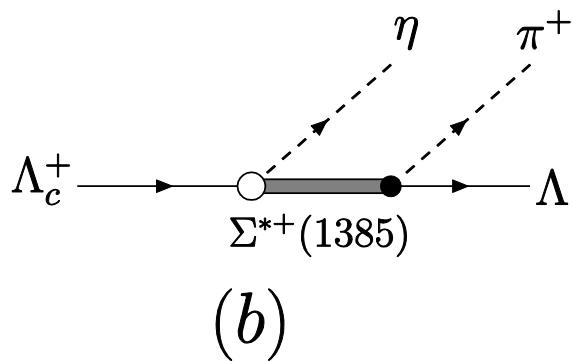
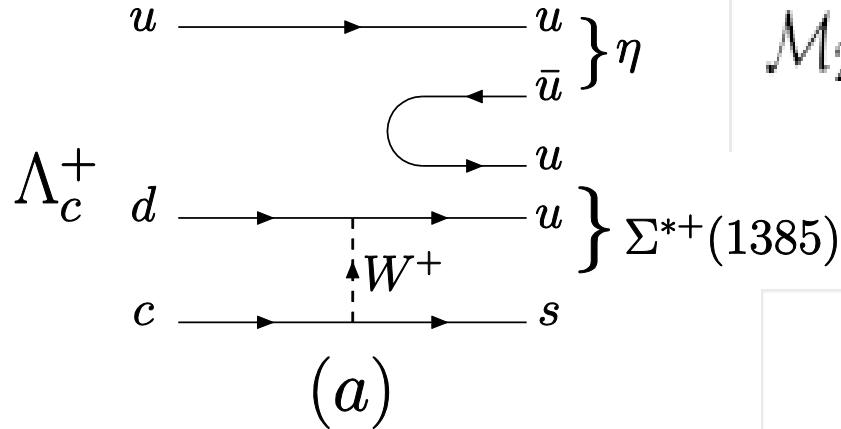
$\Sigma(1380)$ in $\Lambda_c^+ \rightarrow \eta\pi^+\Lambda$ decay



$$\mathcal{M}_1 = ig_{\pi\Lambda\Sigma_1^*} \bar{u}(p_3) G^{\Sigma_1^*}(q) (A_1 + B_1 \gamma_5) u(p),$$

$$G^{\Sigma_1^*}(q) = i \frac{q + M_{\Sigma_1^*}}{q^2 - M_{\Sigma_1^*}^2 + i M_{\Sigma_1^*} \Gamma_{\Sigma_1^*}},$$

$\Sigma(1385)$ in $\Lambda_c^+ \rightarrow \eta\pi^+\Lambda$ decay



$$\mathcal{M}_2 = \frac{i g_{\pi \Lambda \Sigma_2^*}}{m_\eta m_\pi} \bar{u}(p_3) p_2^\mu G_{\mu\nu}^{\Sigma_2^*}(q) p_1^\nu (A_2 + B_2 \gamma_5) u(p),$$

$$G_{\mu\nu}^{\Sigma_2^*}(q) = i \frac{q + M_{\Sigma_2^*}}{q^2 - M_{\Sigma_2^*}^2 + i M_{\Sigma_2^*} \Gamma_{\Sigma_2^*}} P_{\mu\nu},$$

with

$$P^{\mu\nu} = -g^{\mu\nu} + \frac{1}{3} \gamma^\mu \gamma^\nu + \frac{2q^\mu q^\nu}{3M_{\Sigma_2^*}^2} + \frac{\gamma^\mu q^\nu - \gamma^\nu q^\mu}{3M_{\Sigma_2^*}},$$

Invariant mass distributions

$$\frac{d\Gamma}{dM_{\pi^+\Lambda}} = \frac{m_\Lambda}{32\pi^3 M_{\Lambda_c^+}} \int \sum |\mathcal{M}|^2 |\vec{p}_1| |\vec{p}^*| d\cos\theta^*$$

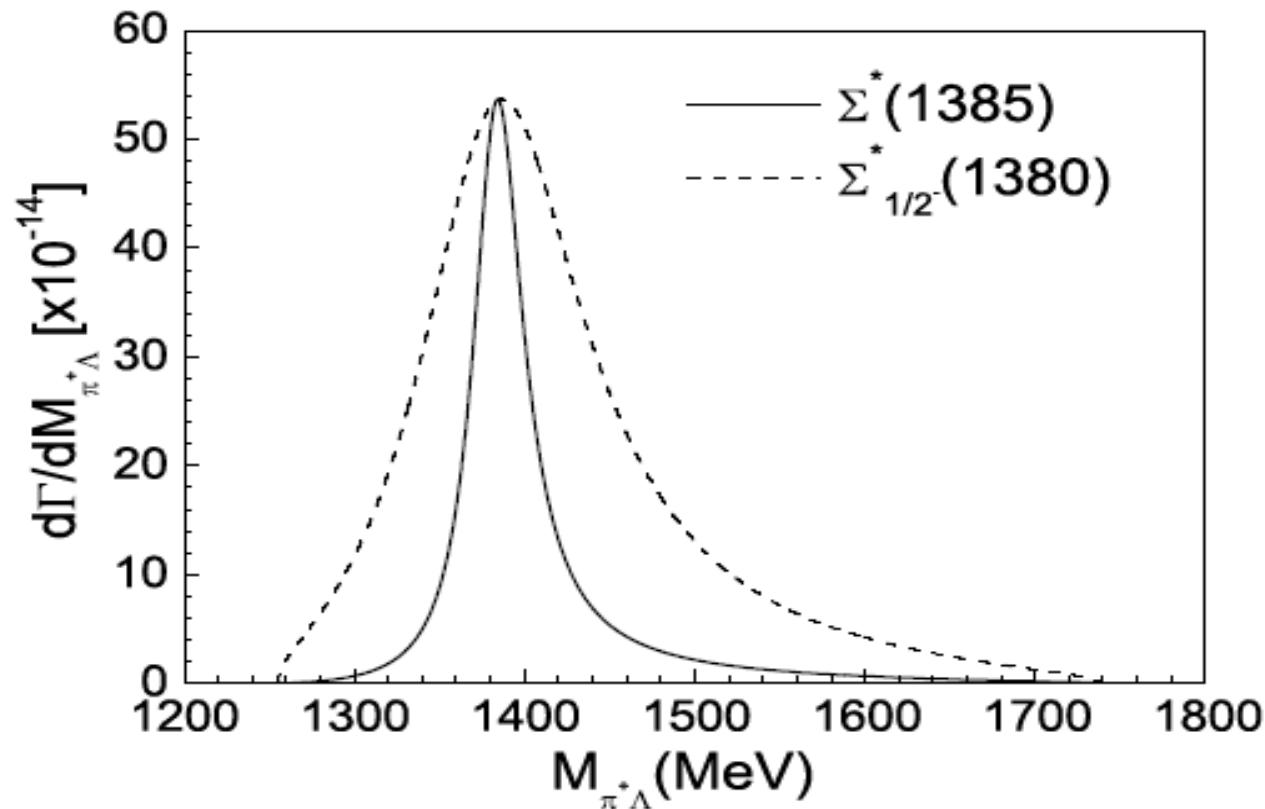


FIG. 5: Invariant mass distributions $d\Gamma/dM_{\pi^+\Lambda}$ as a function of $M_{\pi^+\Lambda}$.

Ju-Jun Xie and Li-Sheng Geng, PRD 96,054009 (2017).

Decay angle and energy distributions

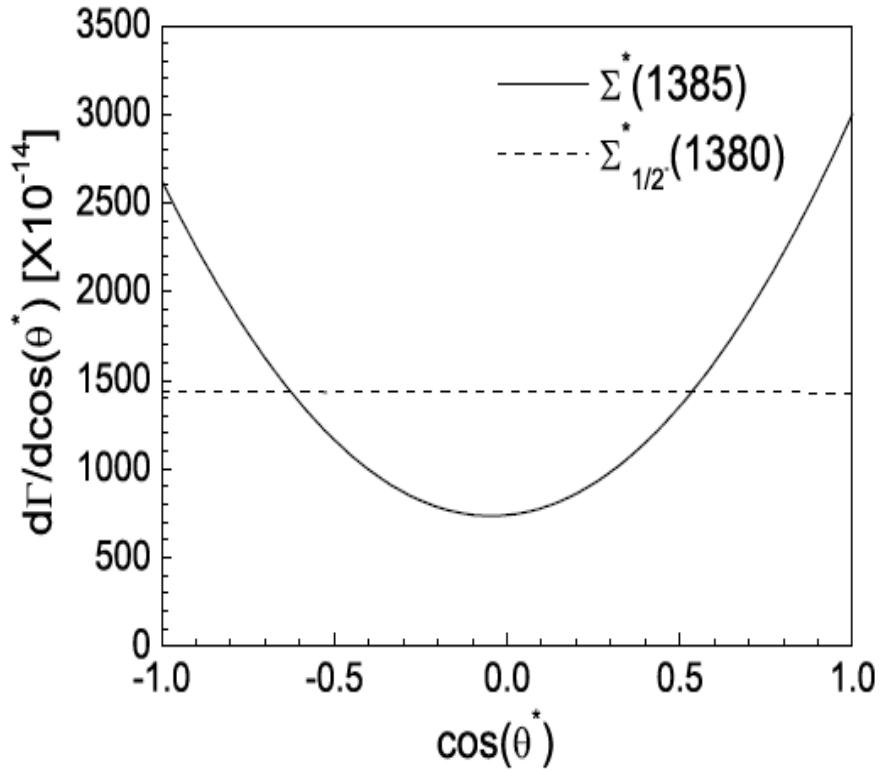


FIG. 6: Angle distributions $d\Gamma/d\cos\theta^*$ in the c.m. frame of $\pi^+\Lambda$ system as a function of $\cos\theta^*$.

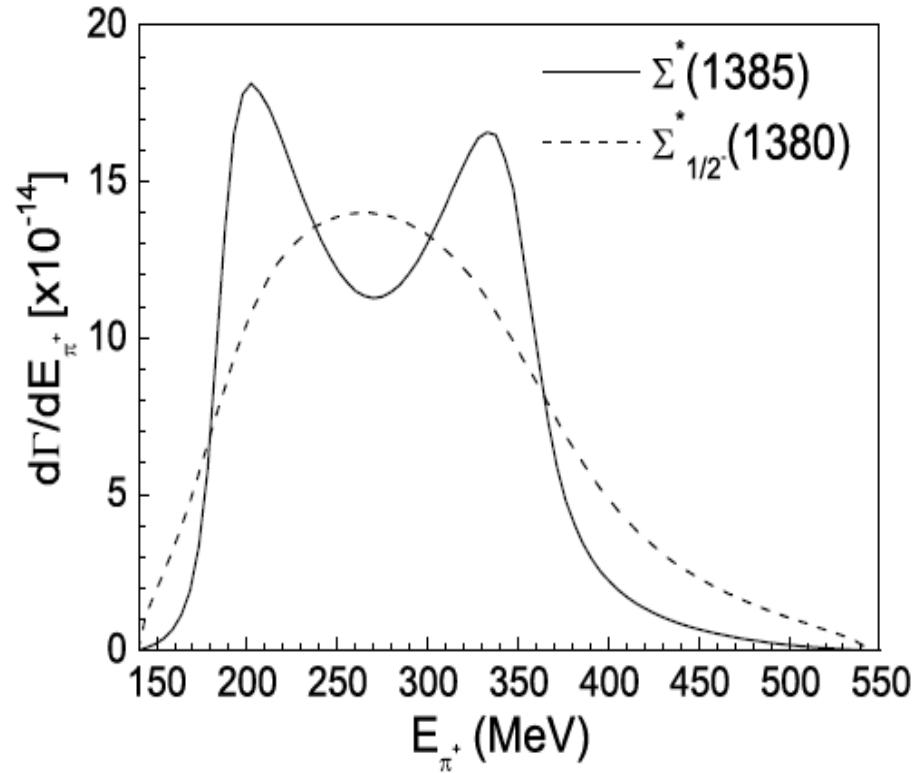
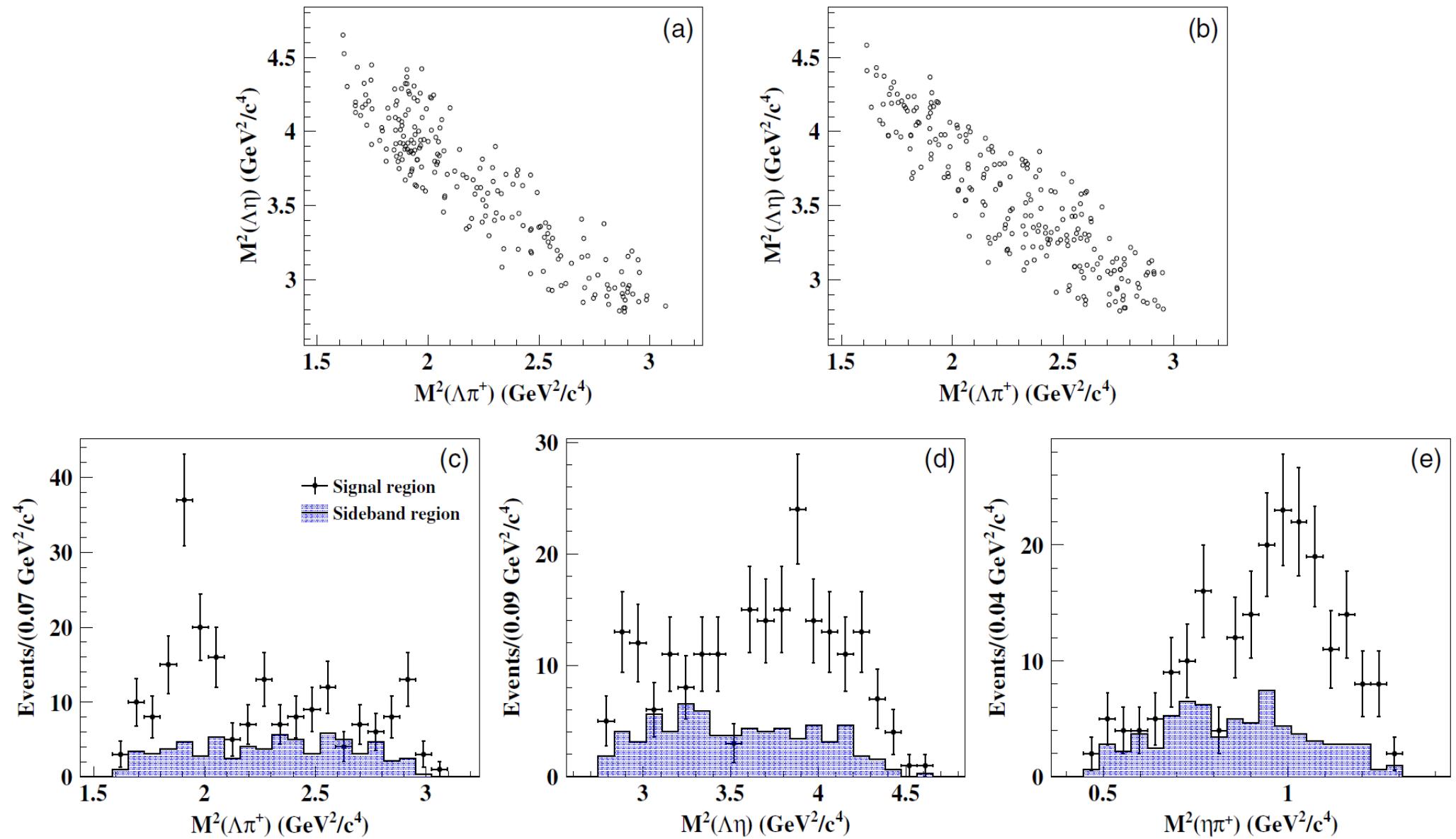


FIG. 7: Energy distributions $d\Gamma/dE_{\pi^+}$ in the rest frame of Λ_c^+ as a function of E_{π^+} .

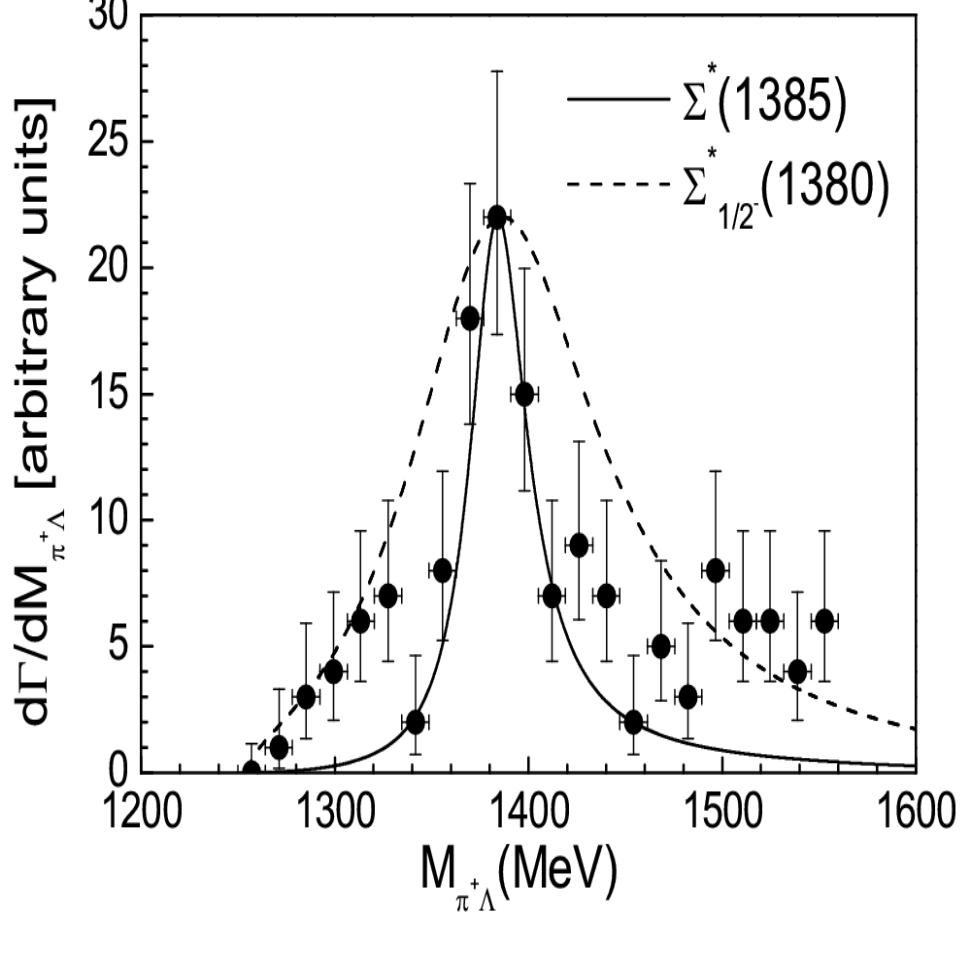
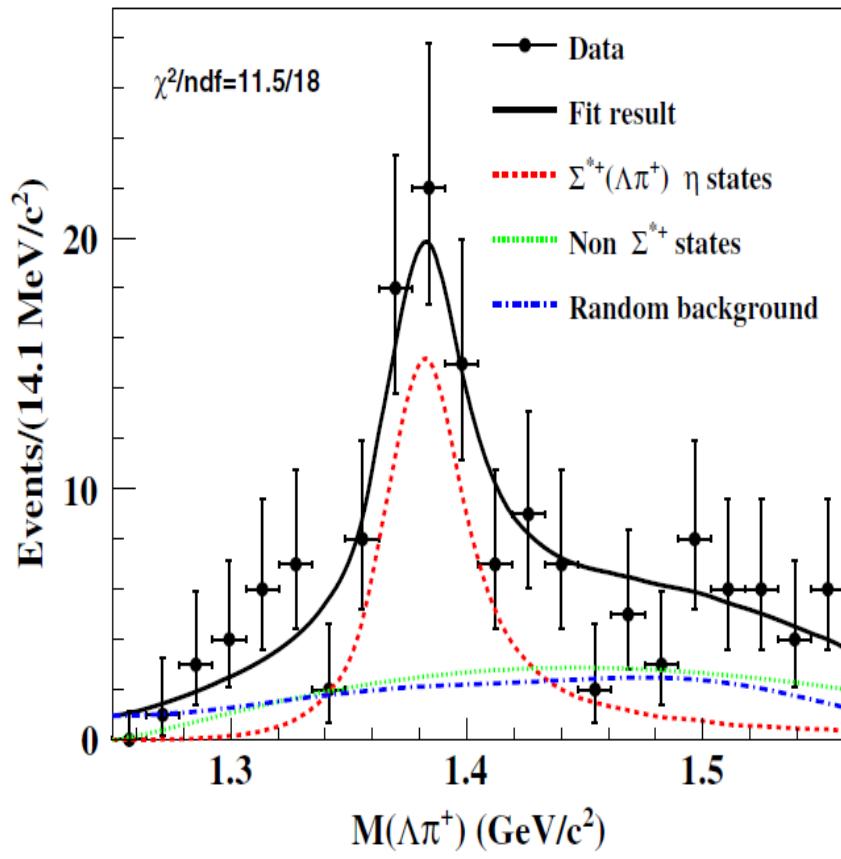
Measurement of the absolute branching fractions of $\Lambda_c^+ \rightarrow \Lambda\eta\pi^+$ and $\Sigma(1385)^+\eta$

(BESIII Collaboration)

PRD 99, 032010 (2019).



$\pi^+\Lambda$ invariant mass distributions at low energies

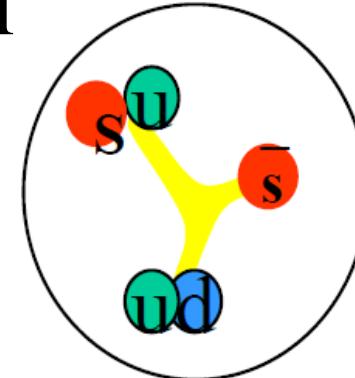


$N^*(1535)$: strangeness component

Couples strongly to strangeness channel

$$uud \text{ (L=1) } 1/2^- \sim N^*(1535) \sim [ud][us] \bar{s}$$

Mode	Fraction (Γ_i/Γ)
$\Gamma_1 \quad N\pi$	32–52 %
$\Gamma_2 \quad N\eta$	30–55 %



Larger $[ud][us] \bar{s}$ component in $N^*(1535)$ makes it coupling strong to $N\eta$ & $K\Lambda$.

$$J/\psi \rightarrow \bar{p}N^* \rightarrow \bar{p}(K\Lambda) / \bar{p}(p\eta) \rightarrow \text{large } g_{N^*K\Lambda}$$

Liu&Zou, PRL96 (2006) 042002; Geng,Oset,Zou&Doring, PRC79 (2009) 025203

$$\gamma p \rightarrow p\eta' \& pp \rightarrow pp\eta' \rightarrow \text{large } g_{N^*N\eta'}$$

M.Dugger et al., PRL96 (2006) 062001; Cao&Lee, PRC78(2008) 035207

$$\pi^- p \rightarrow n\phi \& pp \rightarrow pp\phi \& pn \rightarrow d\phi \rightarrow \text{large } g_{N^*\bar{N}\phi}$$

Xie, Zou & Chiang, PRC77(2008)015206; Cao, Xie, Zou & Xu, PRC80(2009)025203

$N^*(1535)$: dynamically generated state

- Pole position $z_R = [(1490 \sim 1530) - i(45 \sim 125)]\text{MeV}$
PDG 2018  $(M_R, \Gamma_R) = (\simeq 1510, \simeq 170)\text{MeV}$

PHYSICAL REVIEW C, VOLUME 65, 035204

Chiral unitary approach to S-wave meson baryon scattering in the strangeness $S=0$ sector

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Apartado Correos 22085, E-46071 Valencia, Spain

(Received 31 October 2001; published 14 February 2002)

Chiral dynamics of the $S_{11}(1535)$ and $S_{11}(1650)$ resonances revisited

Peter C. Bruns^a, Maxim Mai^{b,*}, Ulf-G. Meißner^{b,c}

Physics Letters B 697 (2011) 254–259

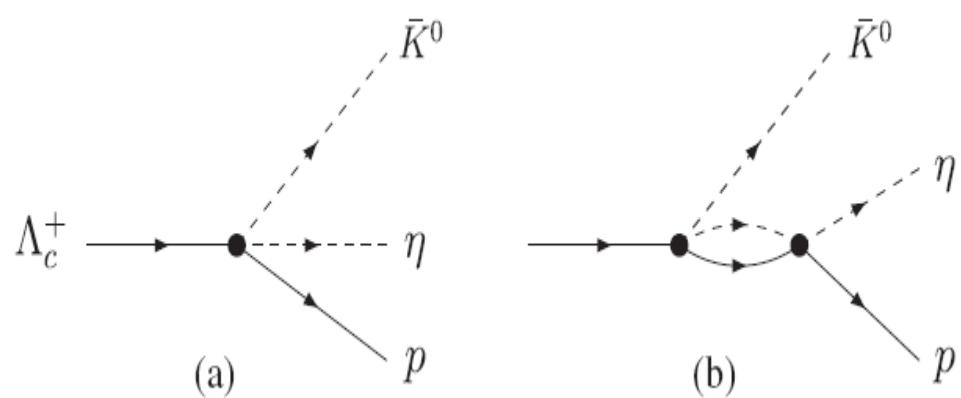
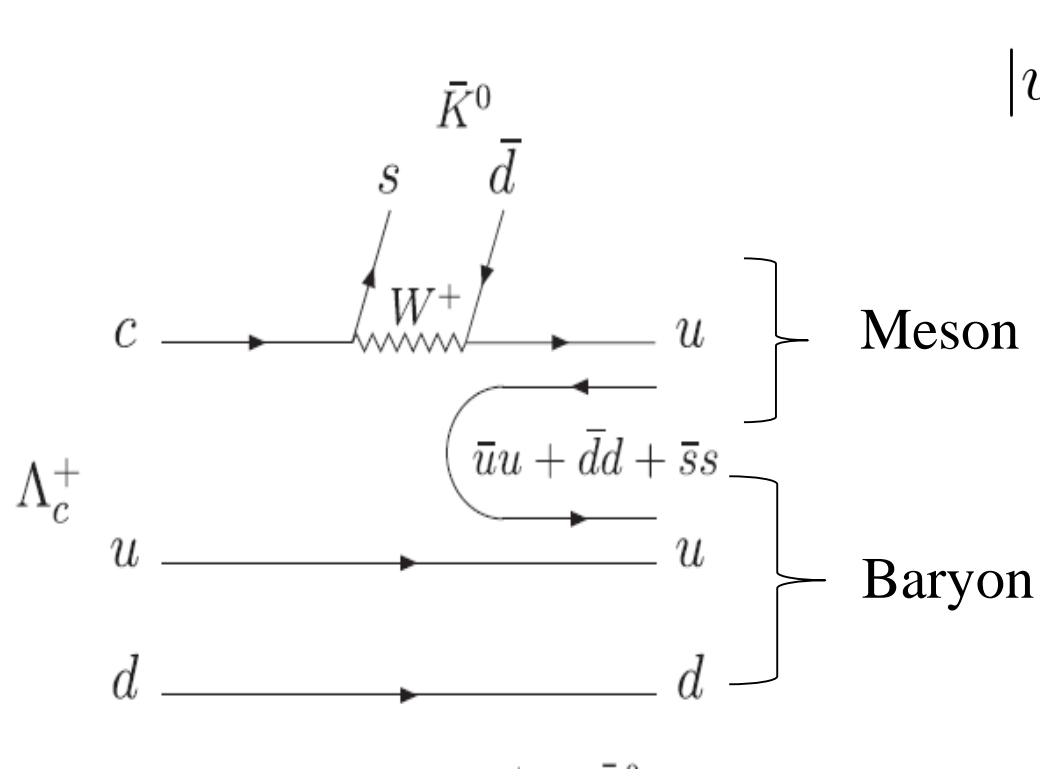
- Breit-Wigner parameterization

$$(M_R, \Gamma_R) = (1525 \sim 1545, 125 \sim 175)\text{MeV} = (\simeq 1535, \simeq 150)\text{MeV}$$



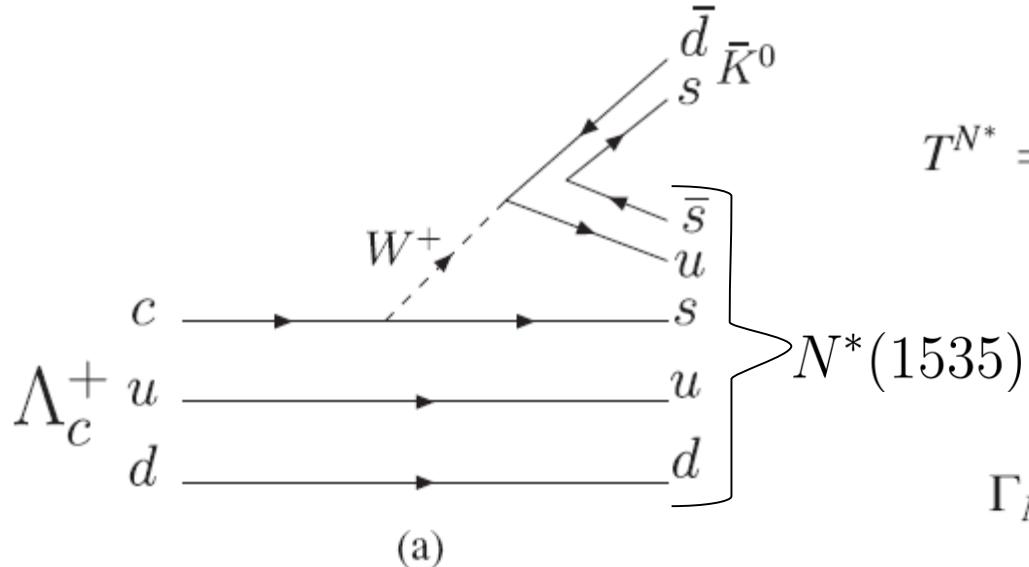
PDG 2018

The $N^*(1535)$ as a dynamically generated state



$$\begin{aligned}
 |uud\rangle &\rightarrow \frac{1}{\sqrt{2}}|u(ud - du)\rangle \\
 &\quad + |\bar{u}u + \bar{d}d + \bar{s}s\rangle \\
 |MB\rangle &= \frac{\sqrt{3}}{3}|\eta p\rangle + \frac{\sqrt{2}}{2}|\pi^0 p\rangle + |\pi^+ n\rangle - \frac{\sqrt{6}}{3}|K^+ \Lambda\rangle, \\
 T^{MB} &= V_P \left(\frac{\sqrt{3}}{3} + \frac{\sqrt{3}}{3}G_{\eta p}(M_{\eta p})t_{\eta p \rightarrow \eta p}(M_{\eta p}) \right. \\
 &\quad + \frac{\sqrt{2}}{2}G_{\pi^0 p}(M_{\eta p})t_{\pi^0 p \rightarrow \eta p}(M_{\eta p}) \\
 &\quad + G_{\pi^+ n}(M_{\eta p})t_{\pi^+ n \rightarrow \eta p}(M_{\eta p}) \\
 &\quad \left. - \frac{\sqrt{6}}{3}G_{K^+ \Lambda}(M_{\eta p})t_{K^+ \Lambda \rightarrow \eta p}(M_{\eta p}) \right),
 \end{aligned}$$

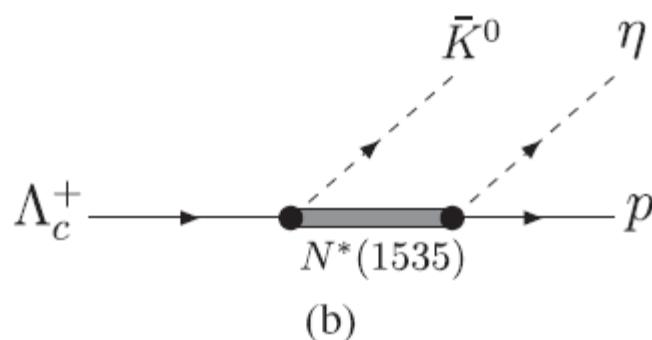
Effective Lagrangian approach and the $N^*(1535)$ resonance as a Breit-Wigner resonance



$$T^{N^*} = ig_{N^*\eta}\bar{u}(p_3, s_p)G_{N^*}(q)(A + B\gamma_5)u(p, s_{\Lambda_c^+}),$$

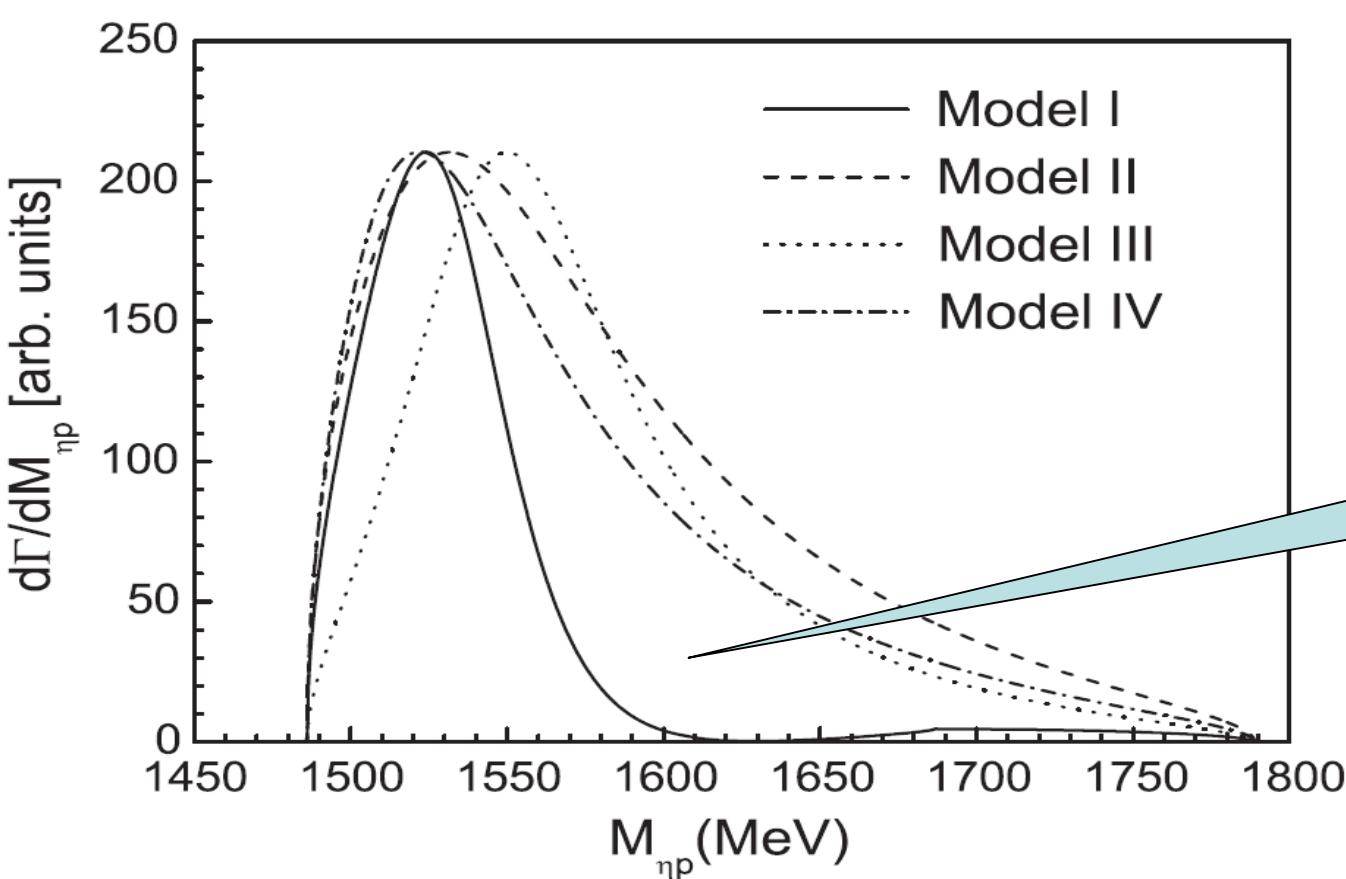
$$G_{N^*}(q) = i \frac{\not{q} + M_{N^*}}{q^2 - M_{N^*}^2 + iM_{N^*}\Gamma_{N^*}(q^2)},$$

$$\Gamma_{N^*}(q^2) = \Gamma_{N^*\rightarrow\pi N}(q^2) + \Gamma_{N^*\rightarrow\eta N}(q^2) + \Gamma_0,$$



Ju-Jun Xie and Li-Sheng Geng, PRD 96, 054009 (2017).

Invariant ηp mass distributions



$$\frac{d\Gamma}{dM_{\eta p}} = \frac{1}{16\pi^3} \frac{m_p p_{\bar{K}^0} p_\eta^*}{M_{\Lambda_c^+}} |T|^2,$$

Model I : $T = T^{MB}$

Different line shapes

Model II : $T = T^{N^}$, $M_{N^*} = 1535$ MeV, $\Gamma_{N^*} = \Gamma_{N^*}(q^2)$*

Model III : $T = T^{N^}$, $M_{N^*} = 1543$ MeV, $\Gamma_{N^*} = 92$ MeV*

Model IV : $T = T^{N^}$, $M_{N^*} = 1500$ MeV, $\Gamma_{N^*} = 110$ MeV*

Other contributions

$$N^*(1650) \rightarrow \eta p$$

Σ^* resonances

$$\rightarrow \bar{K}^0 p$$

$\Sigma^*(1660)1/2^+ :$ *p-wave*

$\Sigma^*(1670)3/2^- :$ *d-wave*

$\Sigma^*(1750)1/2^- :$ *s-wave, but,*

very small phase space

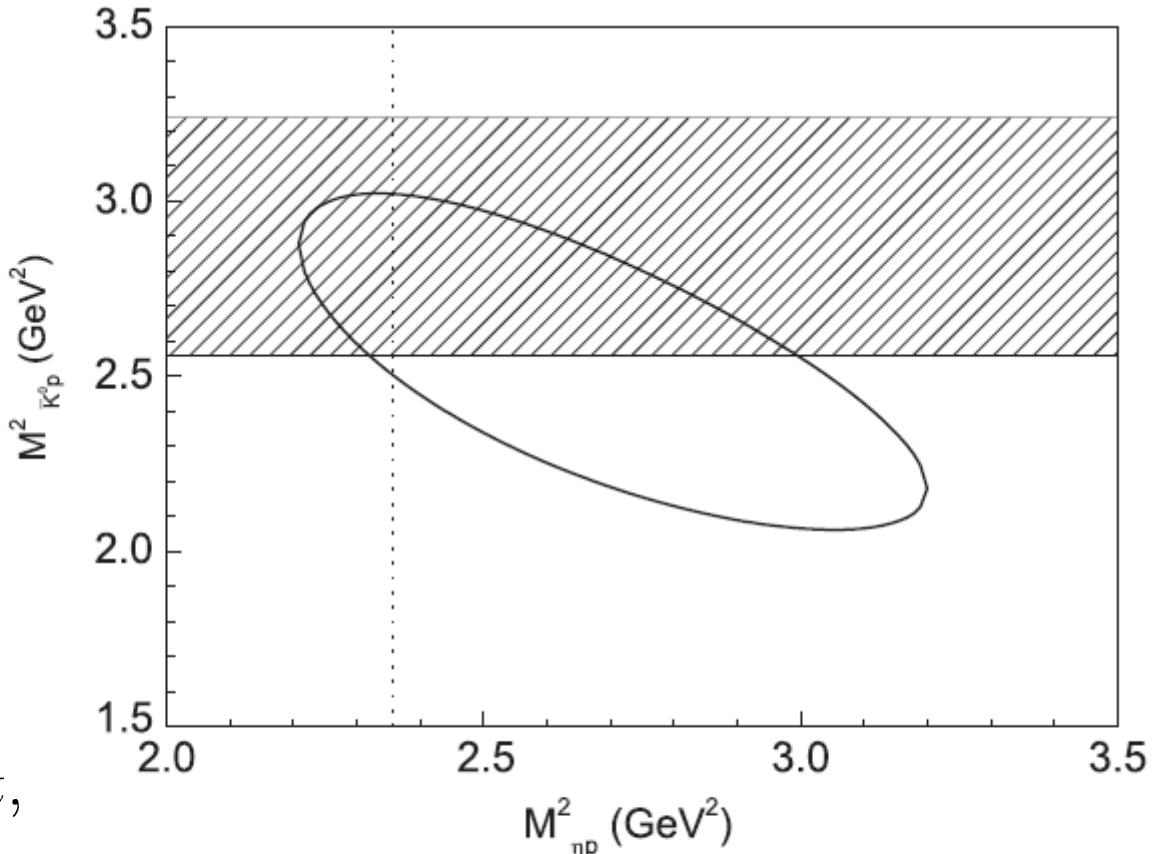


FIG. 7. Dalitz plot for $M_{\eta p}^2$ and $M_{\bar{K}^0 p}^2$ in the $\Lambda_c^+ \rightarrow \bar{K}^0 \eta p$ decay. The $N^*(1535)$ energy is shown by the vertical dotted line, and the horizontal band represents the masses of Σ^* states from 1600 to 1800 MeV.

Production of $N^*(1535)$ and $N^*(1650)$ in $\Lambda_c \rightarrow \bar{K}^0 \eta p$ (πN) decay

ϕN bound state

PHYSICAL REVIEW C, VOLUME 63, 022201(R)

ϕ - N bound state

H. Gao,¹ T.-S. H. Lee,² and V. Marinov¹

PHYSICAL REVIEW C **73**, 025207 (2006)

$N\phi$ states in a chiral quark model

F. Huang,^{1,2,3} Z. Y. Zhang,² and Y. W. Yu²

PHYSICAL REVIEW C **95**, 055202 (2017)

Search for a hidden strange baryon-meson bound state from ϕ production in a nuclear medium

Haiyan Gao,^{1,2} Hongxia Huang,^{1,3,*} Tianbo Liu,^{1,2,†} Jialun Ping,³ Fan Wang,⁴ and Zhiwen Zhao¹

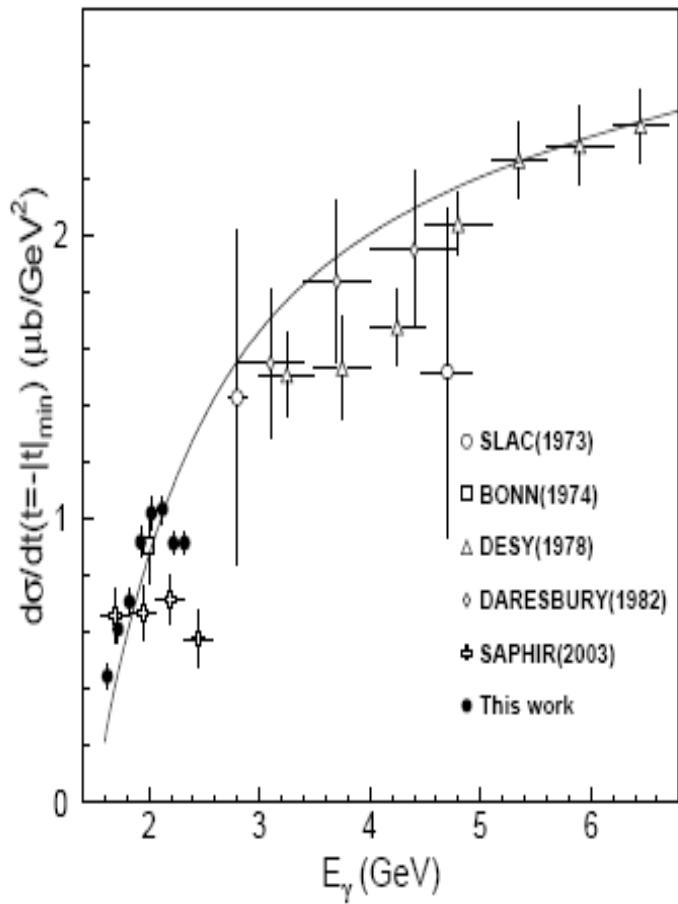
We investigate the hidden strange light baryon-meson system. With the resonating-group method, two bound states, $\eta' - N$ and $\phi - N$, are found in the quark delocalization color screening model. Focusing on the $\phi - N$ bound state around 1950 MeV, we obtain the total decay width of about 4 MeV by calculating the phase shifts in

Decay patterns of low-lying $N_{s\bar{s}}$ states via strangeness channels

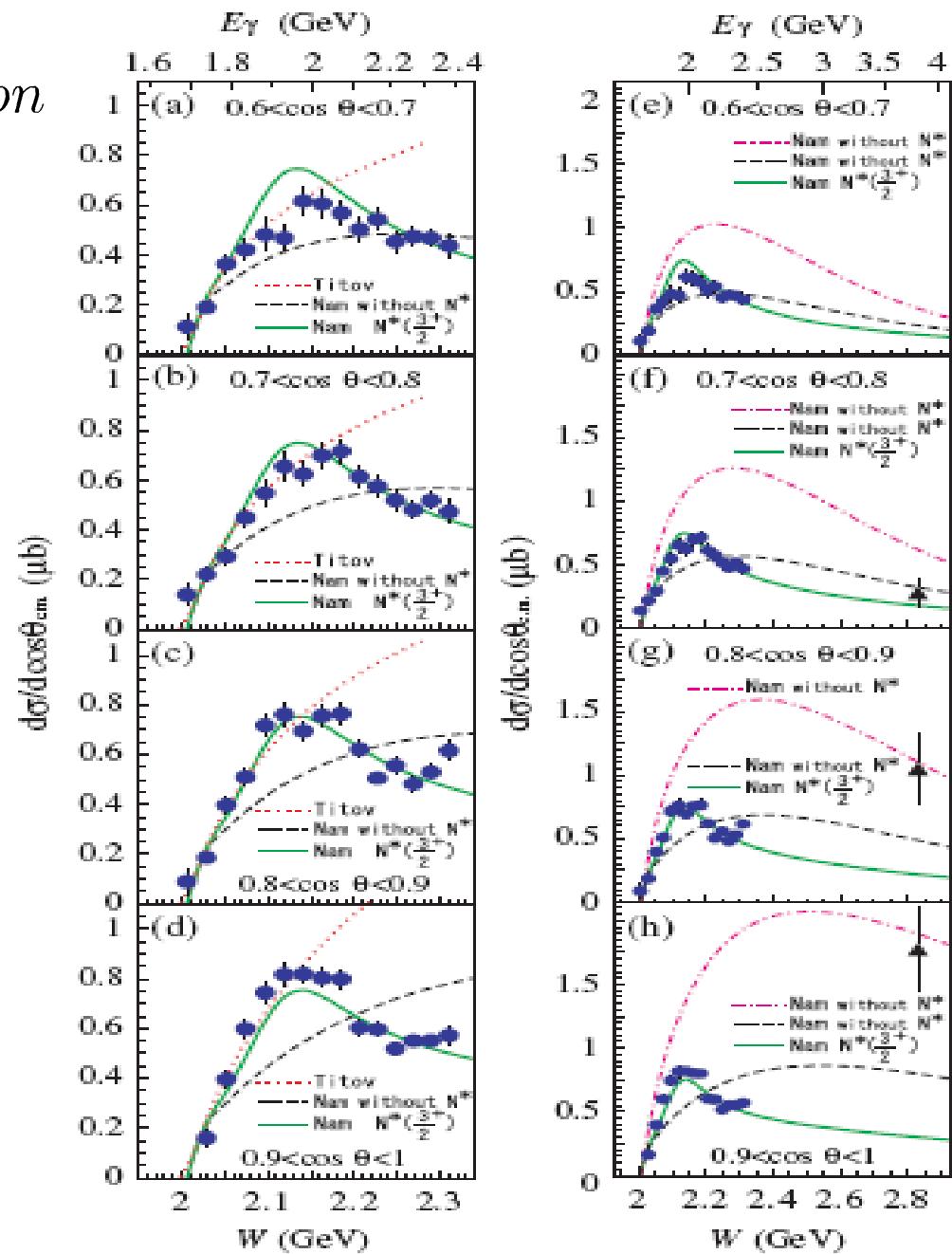
Chun-Sheng An,¹ Ju-Jun Xie,² and Gang Li^{3,*}

PHYSICAL REVIEW C **98**, 045201 (2018)

$\gamma p \rightarrow K^+ \Lambda(1520)$ reaction



$\gamma p \rightarrow p\phi$ reaction



The $\gamma p \rightarrow \phi p$ reaction

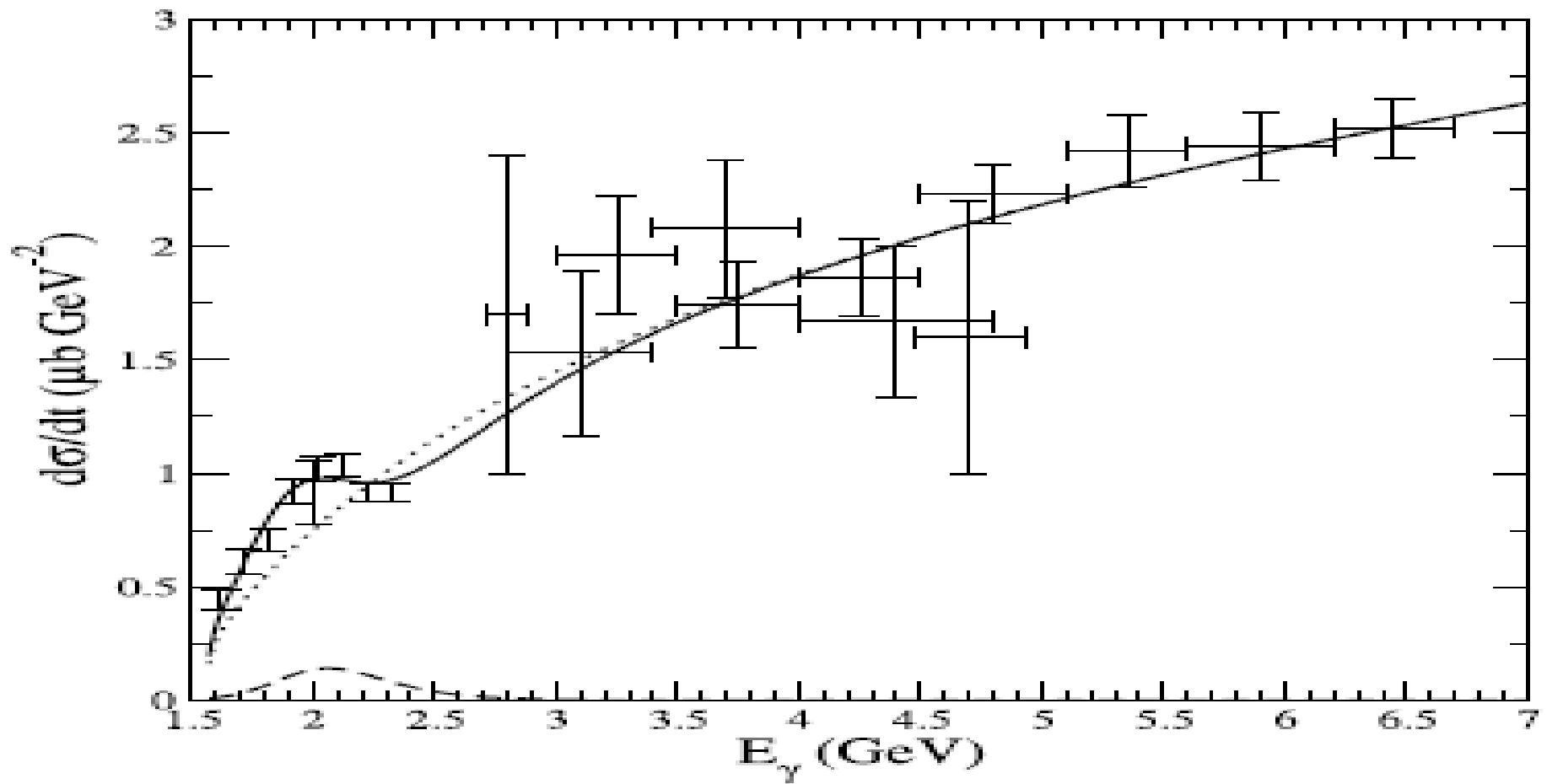
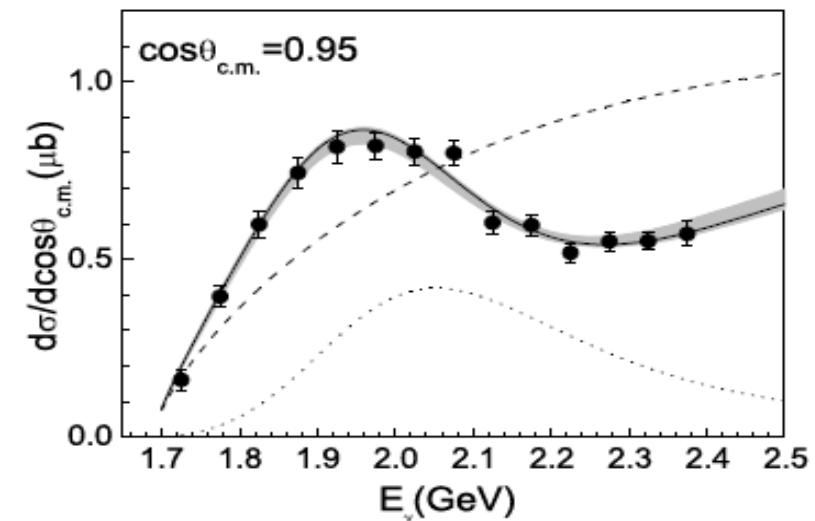
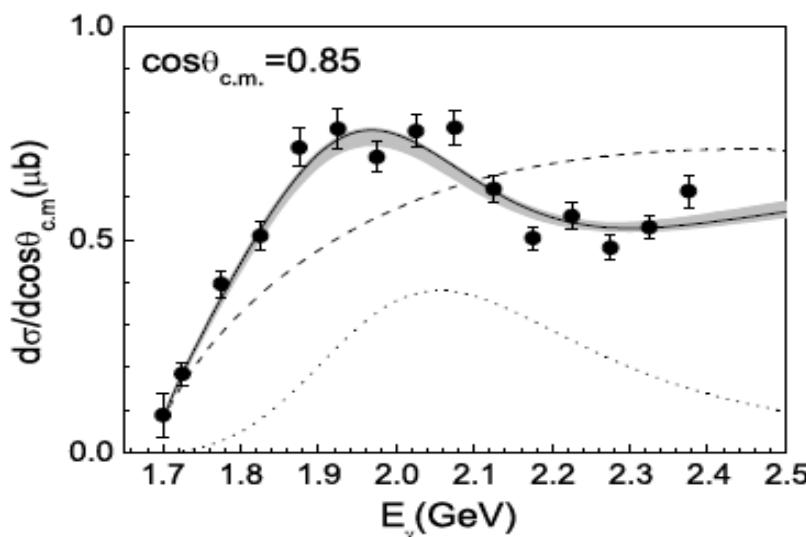
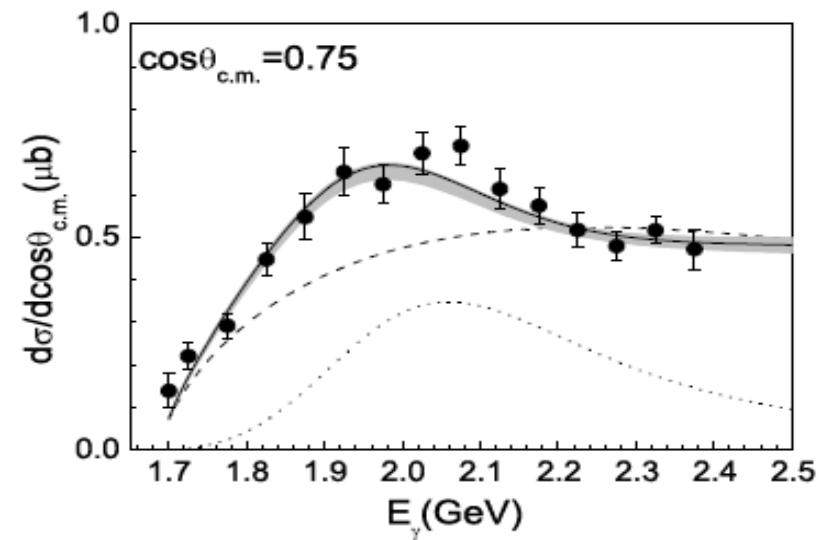
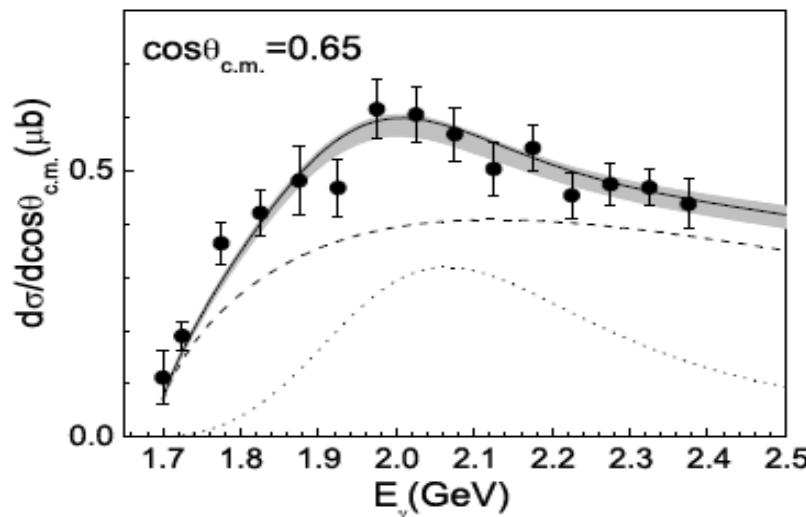
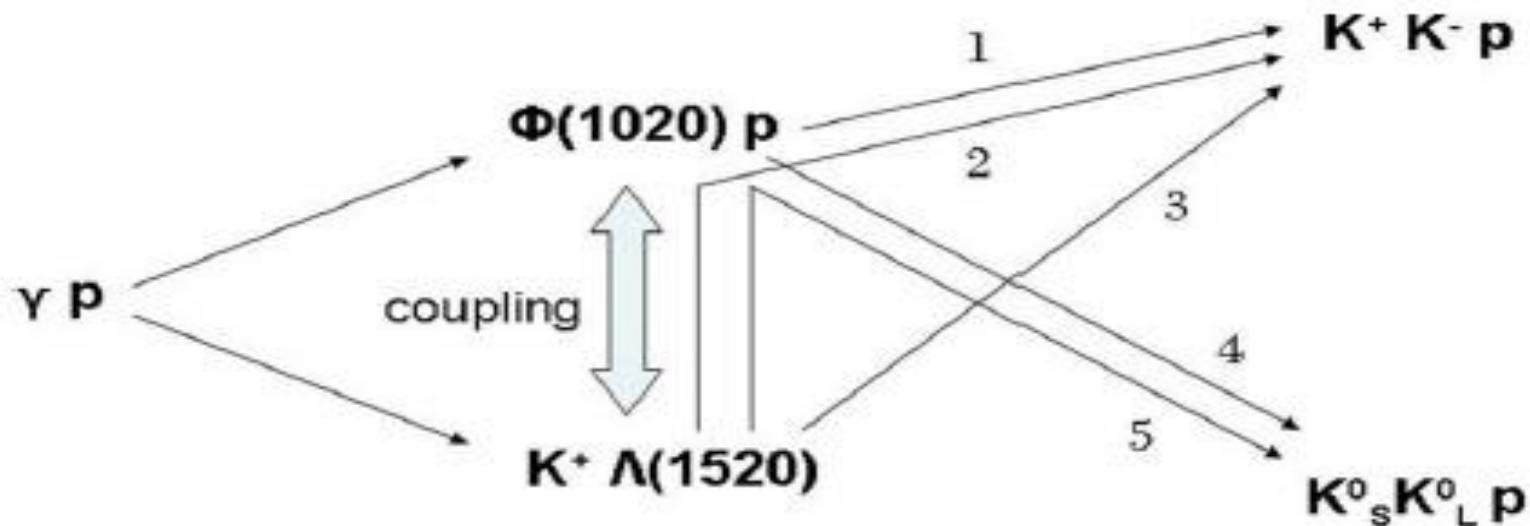


Fig. 2. Differential cross section of $\gamma p \rightarrow \phi p$ at forward direction as a function of photon energy E_γ . The dotted, dashed, and solid lines denote contributions from nonresonant, resonance with $j^P = 3/2^-$, and their sum, respectively. Data are from Refs. [10,17].

Alvin Kiswandhi, Ju-Jun Xie, Shin Nan Yang, PLB, 691, 214 (2010).

The $\gamma p \rightarrow K^+ \Lambda(1520)$ reaction

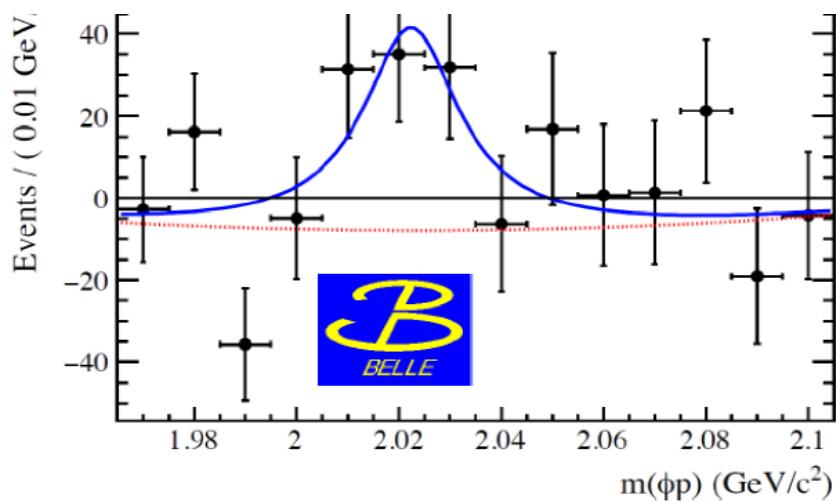
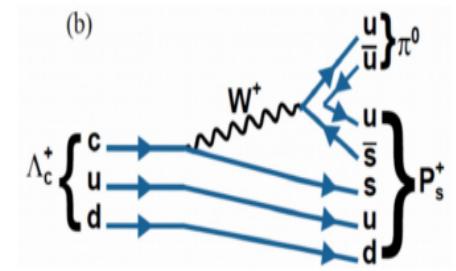
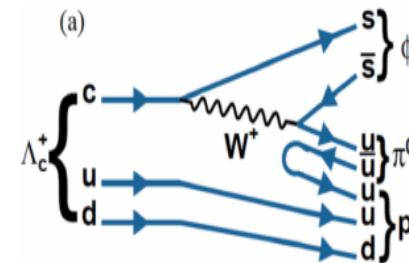
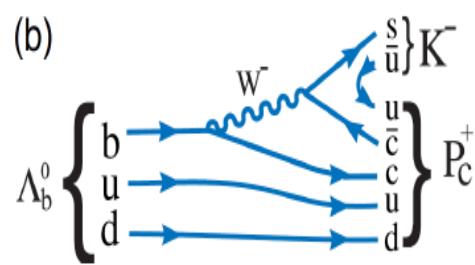
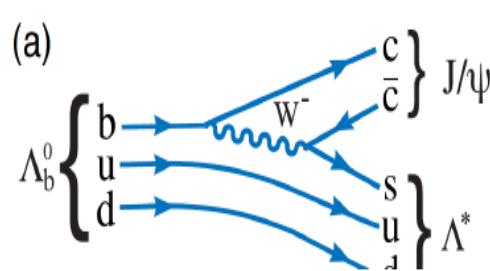




The $\gamma p \rightarrow p\phi$ and $\gamma p \rightarrow K^+\Lambda(1520)$ reactions should be studied together.

Possible ϕp state in $\Lambda_c^+ \rightarrow \pi^0 p \phi$ decay

R. Lebed, PRD92(2015)114030



$\Sigma^+ \rightarrow p\pi^0$ vetoed

From Cheng-Ping Shen

- No significant Ps signal
- Best fit yields a peak at $M=(2025 \pm 5)$ MeV/c² and $\Gamma=(22 \pm 12)$ MeV

[PRD96, 051102\(R\) \(2017\)](#); 915fb⁻¹

Number of candidate $\Lambda_c \rightarrow Ps\pi^0 \rightarrow \phi p\pi^0$ events: 77.6 ± 28.1

$B(\Lambda_c \rightarrow Ps\pi^0) \times B(Ps \rightarrow \phi p) < 8.3 \times 10^{-5}$ @90% C.L.

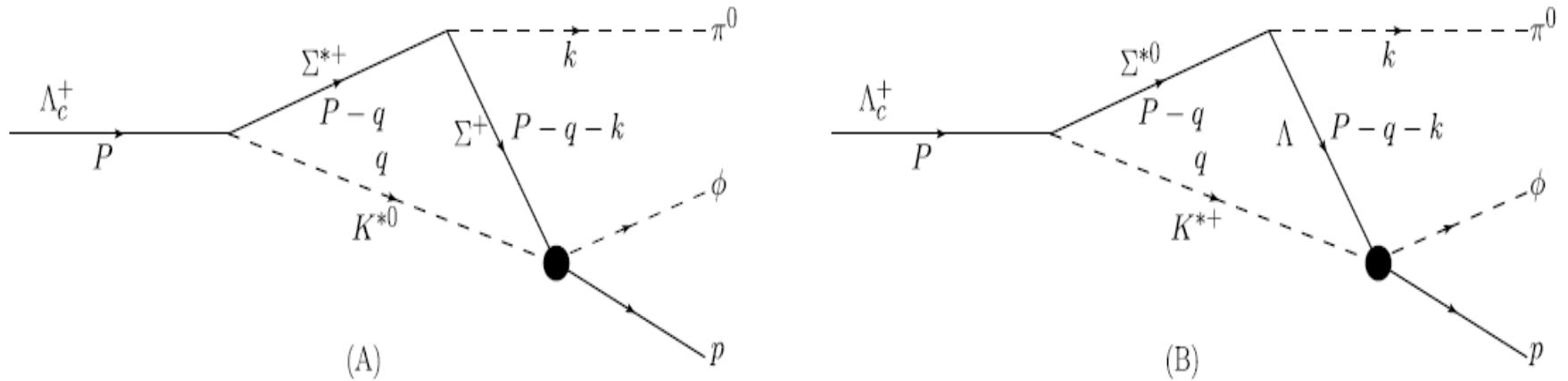


Fig. 1. Triangle diagrams for the $\Lambda_c^+ \rightarrow \pi^0 p \phi$ decay. (A): Σ^+ -exchange. (B): Λ -exchange. The definitions of the kinematical variables (P, q, k) are also shown.

$$\begin{aligned}
 t = & \frac{g_{\Lambda_c \Sigma^* K^*} g_\phi \cdot \vec{k}}{m_\pi} \sum_{i=\Sigma, \Lambda} \mathcal{C}_i \int \frac{d^4 q}{(2\pi)^4} \\
 & \times \frac{i 2 m_{\Sigma^*}}{(P - q)^2 - m_{\Sigma^*}^2 + i m_{\Sigma^*} \Gamma_{\Sigma^*}} \frac{i}{q^2 - m_{K^*}^2 + i m_{K^*} \Gamma_{K^*}} \\
 & \times \frac{i 2 m_i}{(P - q - k)^2 - m_i^2 + i \epsilon}, \tag{4}
 \end{aligned}$$

where we have defined $\mathcal{C}_\Sigma = \frac{\sqrt{6}}{3} t_{K^{*0} \Sigma^+ \rightarrow \phi p}$ and $\mathcal{C}_\Lambda = -t_{K^{*+} \Lambda \rightarrow \phi p}$,

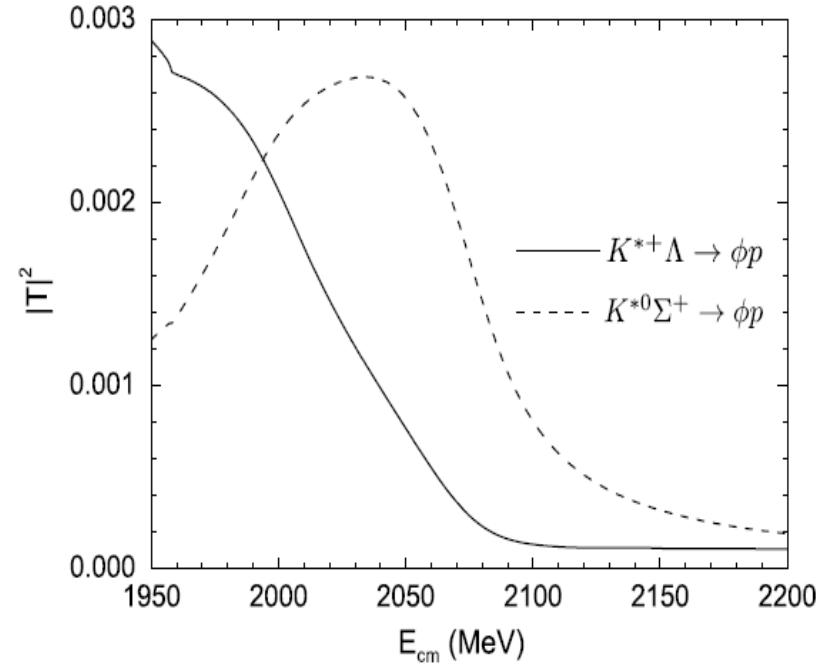


Fig. 3. The squared norm of the T -matrix elements for $K^{*+} \Lambda \rightarrow \phi p$ and $K^{*0} \Sigma^+ \rightarrow \phi p$ as a function of the meson-baryon invariant mass E_{cm} in the model of Ref. [72].

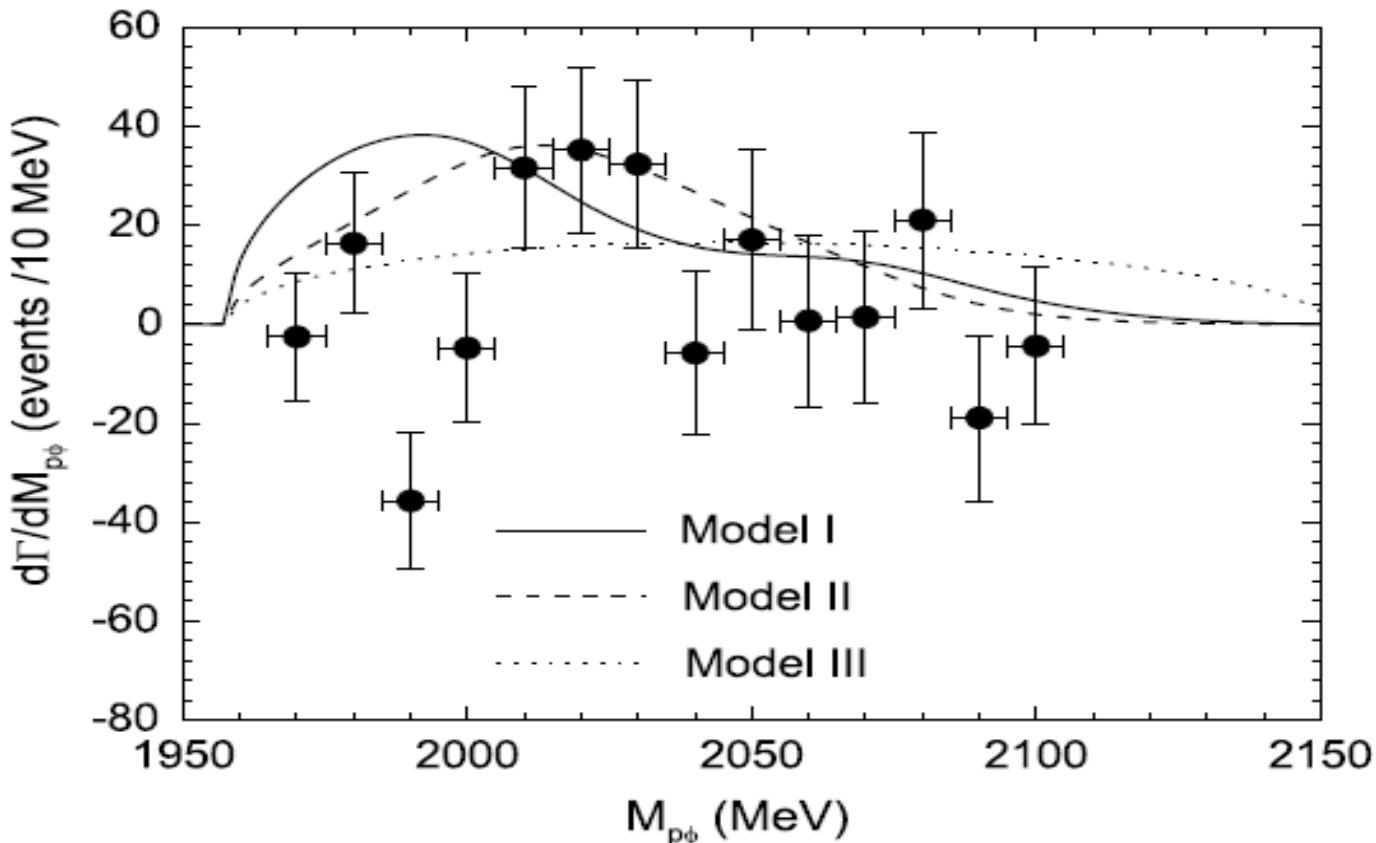


Fig. 2. Invariant mass distribution of the $\Lambda_c^+ \rightarrow \pi^0 p\phi$ decay. The experimental data are taken from Ref. [47].

Model I: the BV interaction model (P_s generated) of A. Ramos, E. Oset, PLB727(2013)287

Model II: no resonance, constant interaction; Model III: phase space

Summary

The $\Lambda_c^+ \rightarrow \eta\pi^+\Lambda$ decay can be used to study the Σ^ and Λ^* resonances*

The $\Lambda_c^+ \rightarrow \bar{K}^0\eta p$ decay can be used to study the $N^(1535)$ resonance*

Possible ϕp state, P_s , in the $\Lambda_c^+ \rightarrow \pi^0\phi p$ decay

TS produces a bump at around 2.02 GeV

Ps, if exists, could distort the line shape, but difficult to be distinguished from TS in this process

We need more efforts, both on theoretical and experimental sides.

Thank you very much for your attention!

$$\frac{d\Gamma}{dM_{\eta p}} = f_1 A^2 + f_2 B^2.$$

$$R = \frac{f_2 B^2}{f_1 A^2} = \frac{f_2}{f_1}.$$

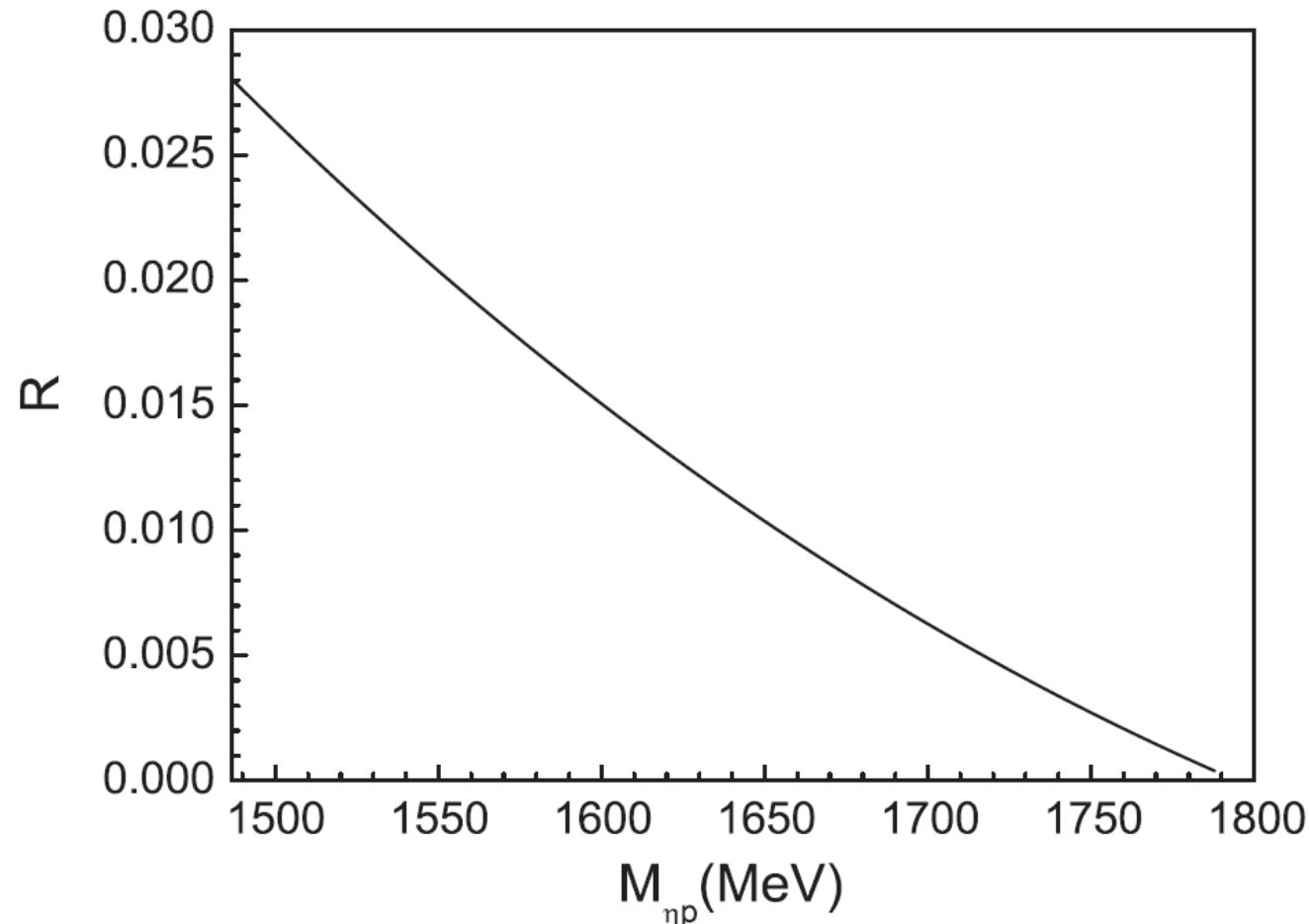


FIG. 6. Ratio R of the B and A terms as a function of the ηp invariant mass.