

# Hyperon physics at Supper tau-charm factory

平荣刚

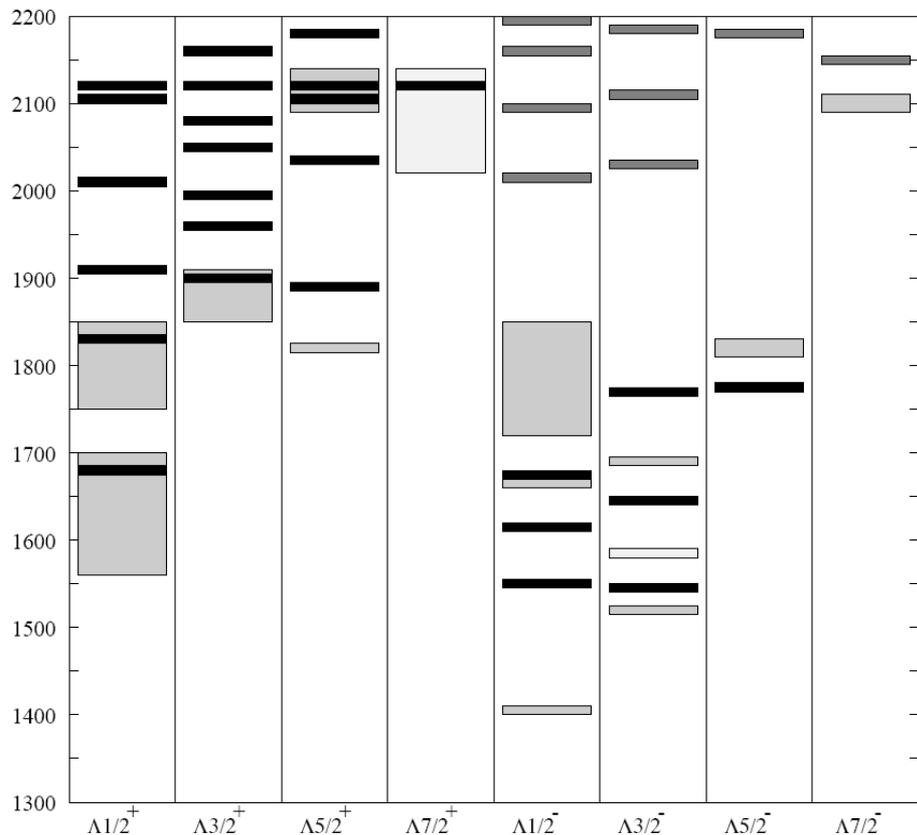
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- **Hyperon spectroscopy**
- **Hyperon non-leptonic decays and CP violation**
- **Hyperon semi-leptonic decays**
- **Hyperon radiative decays**
- **Rare decays**

# Hyperon spectroscopy

## Status of the $\Lambda$ and $\Sigma$ resonances (PDG2012)

| Particle        | $J^P$ | Overall status | Status as seen in — |              |             |                                | Particle       | $J^P$ | Overall status | Status as seen in — |              |             |                                |                 |
|-----------------|-------|----------------|---------------------|--------------|-------------|--------------------------------|----------------|-------|----------------|---------------------|--------------|-------------|--------------------------------|-----------------|
|                 |       |                | $N\bar{K}$          | $\Lambda\pi$ | $\Sigma\pi$ | Other channels                 |                |       |                | $N\bar{K}$          | $\Lambda\pi$ | $\Sigma\pi$ | Other channels                 |                 |
|                 |       |                |                     |              |             |                                | $\Sigma(1193)$ | 1/2+  | ****           |                     |              |             |                                | $N\pi$ (weakly) |
|                 |       |                |                     |              |             |                                | $\Sigma(1385)$ | 3/2+  | ****           |                     | ****         | ****        |                                |                 |
|                 |       |                |                     |              |             |                                | $\Sigma(1480)$ |       | *              | *                   | *            | *           |                                |                 |
| $\Lambda(1116)$ | 1/2+  | ****           |                     | F            |             | $N\pi$ (weakly)                | $\Sigma(1560)$ |       | **             |                     | **           | **          |                                |                 |
| $\Lambda(1405)$ | 1/2-  | ****           | ****                | o            | ****        |                                | $\Sigma(1580)$ | 3/2-  | *              | *                   | *            |             |                                |                 |
| $\Lambda(1520)$ | 3/2-  | ****           | ****                | r            | ****        | $\Lambda\pi\pi, \Lambda\gamma$ | $\Sigma(1620)$ | 1/2-  | **             | **                  | *            | *           |                                |                 |
| $\Lambda(1600)$ | 1/2+  | ***            | ***                 | b            | **          |                                | $\Sigma(1660)$ | 1/2+  | ***            | ***                 | *            | **          |                                |                 |
| $\Lambda(1670)$ | 1/2-  | ****           | ****                | i            | ****        | $\Lambda\eta$                  | $\Sigma(1670)$ | 3/2-  | ****           | ****                | ****         | ****        | several others                 |                 |
| $\Lambda(1690)$ | 3/2-  | ****           | ****                | d            | ****        | $\Lambda\pi\pi, \Sigma\pi\pi$  | $\Sigma(1690)$ |       | **             | *                   | **           | *           | $\Lambda\pi\pi$                |                 |
| $\Lambda(1800)$ | 1/2-  | ***            | ***                 | d            | **          | $N\bar{K}^*, \Sigma(1385)\pi$  | $\Sigma(1750)$ | 1/2-  | ***            | ***                 | **           | *           | $\Sigma\eta$                   |                 |
| $\Lambda(1810)$ | 1/2+  | ***            | ***                 | e            | **          | $N\bar{K}^*$                   | $\Sigma(1770)$ | 1/2+  | *              |                     |              |             |                                |                 |
| $\Lambda(1820)$ | 5/2+  | ****           | ****                | n            | ****        | $\Sigma(1385)\pi$              | $\Sigma(1775)$ | 5/2-  | ****           | ****                | ****         | ***         | several others                 |                 |
| $\Lambda(1830)$ | 5/2-  | ****           | ***                 | F            | ****        | $\Sigma(1385)\pi$              | $\Sigma(1840)$ | 3/2+  | *              | *                   | **           | *           |                                |                 |
| $\Lambda(1890)$ | 3/2+  | ****           | ****                | o            | **          | $N\bar{K}^*, \Sigma(1385)\pi$  | $\Sigma(1880)$ | 1/2+  | **             | **                  | **           |             | $N\bar{K}^*$                   |                 |
| $\Lambda(2000)$ |       | *              |                     | r            | *           | $\Lambda\omega, N\bar{K}^*$    | $\Sigma(1915)$ | 5/2+  | ****           | ***                 | ****         | ***         | $\Sigma(1385)\pi$              |                 |
| $\Lambda(2020)$ | 7/2+  | *              | *                   | b            | *           |                                | $\Sigma(1940)$ | 3/2-  | ***            | *                   | ***          | **          | quasi-2-body                   |                 |
| $\Lambda(2100)$ | 7/2-  | ****           | ****                | i            | ***         | $\Lambda\omega, N\bar{K}^*$    | $\Sigma(2000)$ | 1/2-  | *              |                     | *            |             | $N\bar{K}^*, \Lambda(1520)\pi$ |                 |
| $\Lambda(2110)$ | 5/2+  | ***            | **                  | d            | *           | $\Lambda\omega, N\bar{K}^*$    | $\Sigma(2030)$ | 7/2+  | ****           | ****                | ****         | **          | several others                 |                 |
| $\Lambda(2325)$ | 3/2-  | *              | *                   | d            |             | $\Lambda\omega$                | $\Sigma(2070)$ | 5/2+  | *              | *                   |              | *           |                                |                 |
| $\Lambda(2350)$ |       | ***            | ***                 | e            | *           |                                | $\Sigma(2080)$ | 3/2+  | **             |                     | **           |             |                                |                 |
| $\Lambda(2585)$ |       | **             | **                  | n            |             |                                | $\Sigma(2100)$ | 7/2-  | *              |                     | *            | *           |                                |                 |
|                 |       |                |                     |              |             |                                | $\Sigma(2250)$ |       | ***            | ***                 | *            | *           |                                |                 |
|                 |       |                |                     |              |             |                                | $\Sigma(2455)$ |       | **             | *                   |              |             |                                |                 |
|                 |       |                |                     |              |             |                                | $\Sigma(2620)$ |       | **             | *                   |              |             |                                |                 |
|                 |       |                |                     |              |             |                                | $\Sigma(3000)$ |       | *              | *                   | *            |             |                                |                 |
|                 |       |                |                     |              |             |                                | $\Sigma(3170)$ |       | *              |                     |              |             | multi-body                     |                 |



PDG mass range

$3^*$  or  $4^*$

$*$  or  $**$

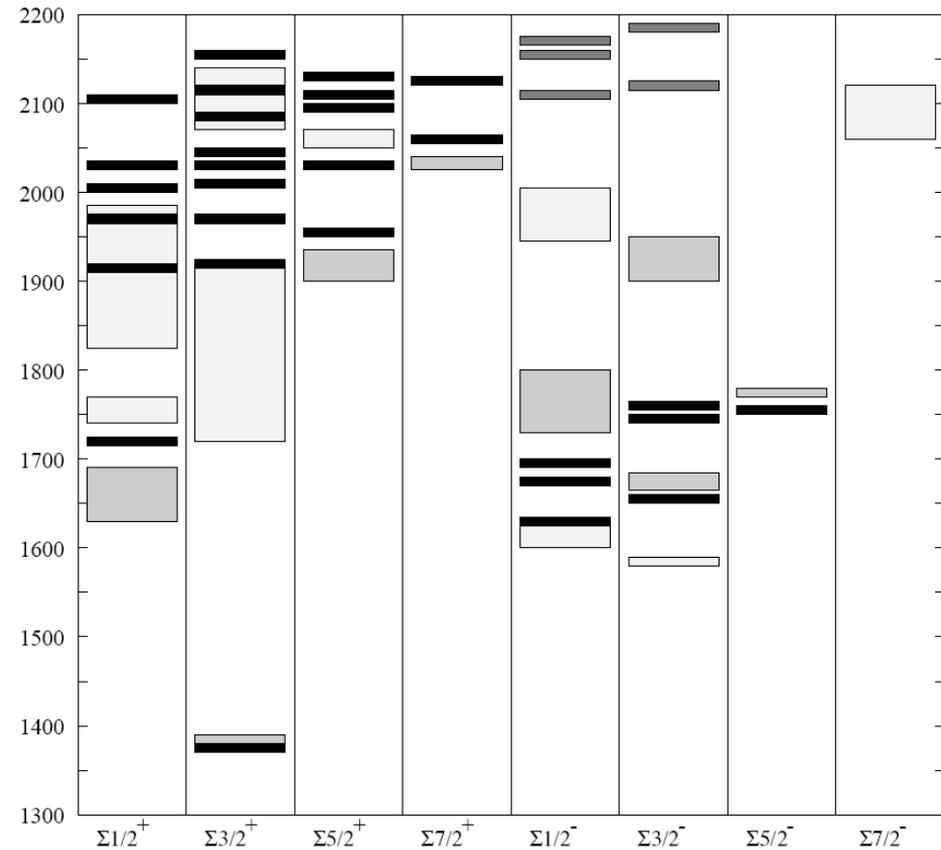
N=3 band

—

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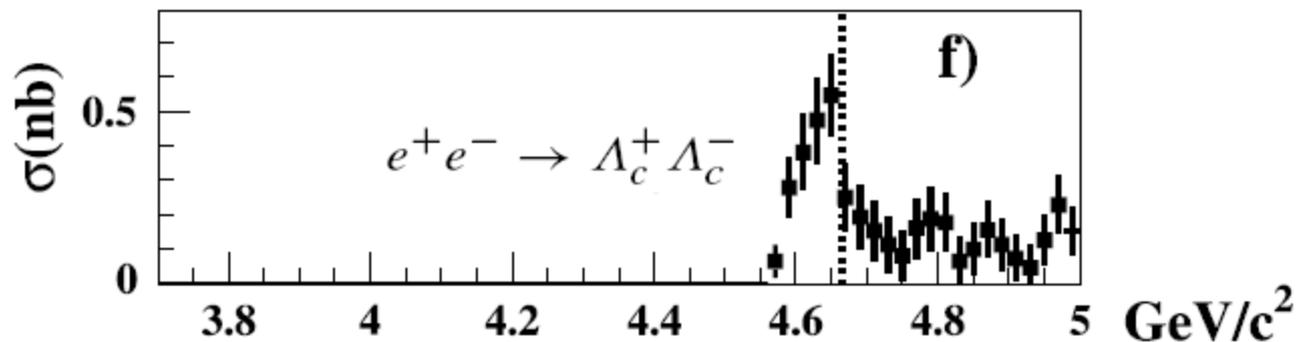
N=0,1,2 bands

Comparison of hyperon spectroscopy between PDG and quark models.



# Status and comments:

1. Evidence for most hyperon resonances, esp.  $\Sigma$ , is poor.
2. The field remains at a standstill (PDG comment)
3. Most hyperon resonances are established from production experiments; Tau-charm experiments make a little contributions.
4. Established hyperon spectroscopy is confronted with the “missing state problem” as raised in quark model.
5.  $J/\psi$  or  $\psi'$  decays don't allow to access most of the excited hyperon resonances due to the limited phase space.
6. Do we need to go higher energy to produce  $\Lambda_c^+ \underline{\Lambda}_c^+$ ,  $\Sigma_c \underline{\Sigma}_c, \dots$  ?



# Hyperon non-leptonic decays and CP violation

Hyperon(1/2+)  $\rightarrow$  Baryon(1/2+)+P(0-)

Partial waves: S (parity violating), P (parity conserving)

Helicity amplitudes:  $F_+ \neq F_-$  ( $\pm : \pm 1/2$ )

$$S = \frac{1}{\sqrt{2}}(F_+ + F_-), \quad P = \frac{1}{\sqrt{2}}(F_+ - F_-)$$

The transition rate is proportional to

$$R(\hat{\omega}_Y, \hat{\omega}_B) = 1 + \gamma \hat{\omega}_Y \cdot \hat{\omega}_B + (1 - \gamma)(\hat{\omega}_Y \cdot \hat{B})(\hat{\omega}_B \cdot \hat{B}) + \alpha(\hat{\omega}_Y + \hat{\omega}_B) \cdot \hat{B} + \beta(\hat{\omega}_Y \times \hat{\omega}_B) \cdot \hat{B}$$

$$\alpha^2 + \beta^2 + \gamma^2 = 1$$

$$\alpha = \frac{|F_+|^2 - |F_-|^2}{|F_+|^2 + |F_-|^2} = \frac{2\Re(S^*P)}{|S|^2 + |P|^2},$$

$$\beta = \frac{2\Im(F_+^*F_-)}{|F_+|^2 + |F_-|^2} = \frac{2\Im(S^*P)}{|S|^2 + |P|^2}$$

$$\gamma = \frac{2\Re(F_+^*F_-)}{|F_+|^2 + |F_-|^2} = \frac{|S|^2 - |P|^2}{|S|^2 + |P|^2}$$

CP conserving:

$$\alpha_Y = -\alpha_{\bar{Y}},$$

$$\beta_Y = -\beta_{\bar{Y}},$$

$$\gamma_Y = \gamma_{\bar{Y}},$$

$$\Gamma_Y = \Gamma_{\bar{Y}}.$$

# CP violation in Standard model (via higher order penguin diagram)

$$|A_Y| \equiv \left| \frac{\alpha_Y + \alpha_{\bar{Y}}}{\alpha_Y - \alpha_{\bar{Y}}} \right| \sim 10^{-5} - 5 \times 10^{-4}$$

$$|B'_Y| \equiv \left| \frac{\beta_Y + \beta_{\bar{Y}}}{\alpha_Y - \alpha_{\bar{Y}}} \right| \sim 10|A_Y| \sim 10^{-4} - 5 \times 10^{-3}$$

$$|B_Y| \equiv \left| \frac{\beta_Y + \beta_{\bar{Y}}}{\beta_Y - \beta_{\bar{Y}}} \right| \sim 100|A_Y| \sim 10^{-3} - 5 \times 10^{-2}$$

$$|\Delta_Y| \equiv \left| \frac{\Gamma_Y - \Gamma_{\bar{Y}}}{\Gamma_Y + \Gamma_{\bar{Y}}} \right| \sim 0.1|A_Y| \sim 10^{-6} - 5 \times 10^{-5}$$

J/ $\psi$  event scale: @BESII: 1.5 month  $\sim$  1 billion

8\*100 billion/year with luminosity 100\*BESII

$\psi'$  events:  $\sim$ 120 Billion / year

| Modes       | J/ $\psi \rightarrow \Lambda \underline{\Lambda}$ | J/ $\psi \rightarrow \Sigma \underline{\Sigma}$ | J/ $\psi \rightarrow \Xi \underline{\Xi}$ | $\psi' \rightarrow \Omega \underline{\Omega}$ |
|-------------|---|---|---|---|
| Events/year | 1.3 billion                                       | $\sim$ 1billion                                 | 0.7billion                                | 6 million                                     |

# Do we need polarized beam?

| $J/\Psi$ Decay channel | Beam polar. | Measured parameter combinations   | Measured parameters  | CP odd observables                  |
|------------------------|-------------|---|--|-------------------------------------|
| $\Lambda\bar{\Lambda}$ | NO          | $\alpha_\Lambda\alpha_{\bar{\Lambda}}$  | $\alpha_\Lambda\alpha_{\bar{\Lambda}}$   | $A_\Lambda$<br>(requires ext. data) |
| $\Lambda\Lambda$       | YES         | $\alpha_\Lambda, \alpha_{\bar{\Lambda}},$<br>$\alpha_\Lambda\alpha_{\bar{\Lambda}}$   | $\alpha_\Lambda, \alpha_{\bar{\Lambda}}$   | $A_\Lambda$                         |
| $\Xi^-\bar{\Xi}^+$     | NO          | $\alpha_\Xi\alpha_{\bar{\Xi}}, \alpha_\Xi\alpha_\Lambda, \alpha_\Xi\alpha_{\bar{\Lambda}}, \alpha_\Lambda\alpha_{\bar{\Lambda}}$<br>$\alpha_\Xi\alpha_{\bar{\Lambda}}, \alpha_{\bar{\Xi}}\alpha_\Lambda,$<br>$\alpha_\Lambda\alpha_{\bar{\Lambda}}\beta_\Xi, \alpha_\Lambda\alpha_{\bar{\Lambda}}\beta_{\bar{\Xi}}, \alpha_\Lambda\alpha_{\bar{\Lambda}}\gamma_\Xi,$<br>$\alpha_\Lambda\alpha_{\bar{\Lambda}}\gamma_{\bar{\Xi}}, \alpha_\Xi\alpha_{\bar{\Lambda}}\beta_{\bar{\Xi}}, \alpha_\Xi\alpha_{\bar{\Lambda}}\gamma_{\bar{\Xi}}, \dots$<br>$\alpha_\Xi\alpha_{\bar{\Xi}}\alpha_\Lambda\alpha_{\bar{\Lambda}}, \alpha_\Lambda\alpha_{\bar{\Lambda}}\beta_\Xi\beta_{\bar{\Xi}}, \dots$ | $\alpha_\Lambda, \alpha_{\bar{\Lambda}}$<br>$\alpha_\Xi, \alpha_{\bar{\Xi}}$<br>$\beta_\Xi, \beta_{\bar{\Xi}}$ | $A_\Xi$<br>$A_\Lambda$<br>$B'_\Xi$  |
| $\Xi^-\bar{\Xi}^+$     | YES         | As without polarisation plus<br>$\alpha_\Xi, \alpha_{\bar{\Xi}}, \alpha_\Lambda, \alpha_{\bar{\Lambda}},$<br>$\alpha_\Lambda\beta_\Xi, \alpha_{\bar{\Lambda}}\beta_{\bar{\Xi}}, \alpha_\Lambda\gamma_\Xi, \alpha_{\bar{\Lambda}}\gamma_{\bar{\Xi}},$<br>$\alpha_\Xi\alpha_{\bar{\Xi}}\alpha_\Lambda, \alpha_\Xi\alpha_{\bar{\Xi}}\alpha_{\bar{\Lambda}}, \alpha_\Xi\alpha_\Lambda\alpha_{\bar{\Lambda}}, \dots$<br>$\alpha_\Xi\alpha_\Lambda\alpha_{\bar{\Lambda}}\beta_{\bar{\Xi}}, \dots$   | $\alpha_\Lambda, \alpha_{\bar{\Lambda}}$<br>$\alpha_\Xi, \alpha_{\bar{\Xi}}$<br>$\beta_\Xi, \beta_{\bar{\Xi}}$ | $A_\Xi$<br>$A_\Lambda$<br>$B'_\Xi$  |

# Sensitivity estimation on the CP violation

$$\delta A_Y = \frac{1}{\alpha |P|} \sqrt{\frac{3}{N} + \frac{3}{\bar{N}}}$$

Assuming 40% polar.

1 year events

| modes  | W/o polarization | CP-odd parameter                 | SM prediction  | sensitivity             |
|--|------------------|----------------------------------|--|-------------------------|
| $J/\psi \rightarrow \Lambda \underline{\Lambda}$ | No               | $A_\Lambda$                      | $10^{-5} \sim 5 \times 10^{-4}$                                    | $1.5 \times 10^{-3}$    |
|  | Yes              | $A_\Lambda$                      | $10^{-5} \sim 5 \times 10^{-4}$                                    | $< 1.5 \times 10^{-3}$  |
| $J/\psi \rightarrow \Sigma \underline{\Sigma}$   | No               | $A_\Sigma$                       |  | $\sim 10^{-3}$          |
|  | Yes              | $A_\Sigma$                       |  | $< 10^{-3}$             |
| $J/\psi \rightarrow \Xi \underline{\Xi}$         | No               | $A_\Xi, A_\Lambda,$<br>$A_{\Xi}$ | $10^{-5} \sim 5 \times 10^{-4}$<br>$10^{-4} \sim 5 \times 10^{-3}$ | $\sim 3 \times 10^{-4}$ |
|  | Yes              | $A_\Xi, A_\Lambda, A_{\Xi}$      |  | $< 3 \times 10^{-4}$    |
| $\psi' \rightarrow \Omega \underline{\Omega}$    | No               | $A_\Omega$                       |  | $> 10^{-2}$             |
|  | Yes              | $A_\Omega$                       |  | $\sim 10^{-2}$          |

# Hyperon semi-leptonic decays

For  $B \rightarrow b e^- \nu_e$  decay:

$$\mathcal{M} = \frac{G_S}{\sqrt{2}} \bar{u}_b (O_\alpha^V + O_\alpha^A) u_B \bar{u}_e \gamma^\alpha (1 + \gamma_5) v_\nu$$

$$O_\alpha^V = f_1(q^2) \gamma^\alpha + \frac{f_2(q^2)}{M_B} \sigma_{\alpha\beta} q^\beta + \frac{f_3(q^2)}{M_B} q_\alpha$$

$$O_\alpha^A = \left( g_1(q^2) \gamma^\alpha + \frac{g_2(q^2)}{M_B} \sigma_{\alpha\beta} q^\beta + \frac{g_3(q^2)}{M_B} q_\alpha \right) \gamma_5$$

$$G_S = G_F V_{us} \text{ for } |\Delta S| = 1$$

- To extract the element  $V_{us}$  of the CKM matrix independently from kaon decays
- To extract the ratio of form factor between axial-vector and vector components.

Results from  $V_{us}$  analysis using measured  $g_1/f_1$  values

| Decay                                       | Rate                   | $g_1/f_1$         | $V_{us}$            |
|---|------------------------|-------------------|---------------------|
| Process                                     | $(\mu\text{sec}^{-1})$ |                   |                     |
| $\Lambda \rightarrow pe^{-}\bar{\nu}$       | 3.161(58)              | 0.718(15)         | $0.2224 \pm 0.0034$ |
| $\Sigma^- \rightarrow ne^{-}\bar{\nu}$      | 6.88(24)               | -0.340(17)        | $0.2282 \pm 0.0049$ |
| $\Xi^- \rightarrow \Lambda e^{-}\bar{\nu}$  | 3.44(19)               | 0.25(5)           | $0.2367 \pm 0.0099$ |
| $\Xi^0 \rightarrow \Sigma^+ e^{-}\bar{\nu}$ | 0.876(71)              | 1.32(+.22/ - .18) | $0.209 \pm 0.027$   |
| Combined                                    | —                      | —                 | $0.2250 \pm 0.0027$ |

SU(3) breaking effects, exp. uncertainties

Table 1:  $|V_{us}|f_+(0)$  from  $K_{\ell 3}$ .

| Decay Mode    | $ V_{us} f_+(0)$    |
|---------------|---------------------|
| $K^\pm e 3$   | $0.2173 \pm 0.0008$ |
| $K^\pm \mu 3$ | $0.2176 \pm 0.0011$ |
| $K_L e 3$     | $0.2163 \pm 0.0006$ |
| $K_L \mu 3$   | $0.2168 \pm 0.0007$ |
| $K_S e 3$     | $0.2154 \pm 0.0013$ |
| Average       | $0.2166 \pm 0.0005$ |

Opportunity?

Need vertex detector!

PDG2012

# Hyperon radiative decays

- involve radiative and weak interactions
- Hara's theorem violation:

asymmetry parameter :

Hara's theorem:

$$|\alpha(\Sigma^+ \rightarrow p\gamma)| \approx 0.2$$

exp. :

$$\alpha(\Sigma^+ \rightarrow p\gamma) = -0.76 \pm 0.08$$

- The key issue is SU(3) breaking effects
  - VDM+SU(6)
  - Soft-pion approximation

# Rare decays

PDG2012

| $\Sigma^+$ DECAY MODES  |    | Fraction ( $\Gamma_i/\Gamma$ )                         |                  | Confidence level | $\rho$ (MeV/c)              |
|---|----|--|------------------|------------------|-----------------------------|
| <b><math>\Delta S = \Delta Q</math> (SQ) violating modes or<br/><math>\Delta S = 1</math> weak neutral current (S1) modes</b> |    |  |                  |                  |                             |
|   |    |  |                  |                  | <b>1 billion evts /year</b> |
| $n e^+ \nu_e$   | SQ | $< 5$  | $\times 10^{-6}$ | 90%              | 224                         |
| $n \mu^+ \nu_\mu$   | SQ | $< 3.0$  | $\times 10^{-5}$ | 90%              | 202                         |
| $p e^+ e^-$   | S1 | $< 7$  | $\times 10^{-6}$ |                  | 225                         |
| $p \mu^+ \mu^-$   | S1 | $( 9 \begin{smallmatrix} +9 \\ -8 \end{smallmatrix} )$ | $\times 10^{-8}$ |                  | 121                         |

**Upper limits:  $<10^{-8}$  @STCF**

| $\Xi^-$ DECAY MODES                                   |    | Fraction ( $\Gamma_i/\Gamma$ ) |                  | Confidence level | $\rho$ (MeV/c)                |
|---|----|--------------------------------|------------------|------------------|-------------------------------|
| <b><math>\Delta S = 2</math> forbidden (S2) modes</b> |    |                                |                  |                  |                               |
|   |    |                                |                  |                  | <b>0.7 billion evts /year</b> |
| $n \pi^-$   | S2 | $< 1.9$                        | $\times 10^{-5}$ | 90%              | 304                           |
| $n e^- \bar{\nu}_e$                                   | S2 | $< 3.2$                        | $\times 10^{-3}$ | 90%              | 327                           |
| $n \mu^- \bar{\nu}_\mu$                               | S2 | $< 1.5$                        | %                | 90%              | 314                           |
| $p \pi^- \pi^-$                                       | S2 | $< 4$                          | $\times 10^{-4}$ | 90%              | 223                           |
| $p \pi^- e^- \bar{\nu}_e$                             | S2 | $< 4$                          | $\times 10^{-4}$ | 90%              | 305                           |
| $p \pi^- \mu^- \bar{\nu}_\mu$                         | S2 | $< 4$                          | $\times 10^{-4}$ | 90%              | 251                           |
| $p \mu^- \mu^-$                                       | L  | $< 4$                          | $\times 10^{-8}$ | 90%              | 272                           |

**Upper limits:  $\sim 10^{-7}$  @STCF**

# Summary

- **Search for excited hyperons is limited from charmonium decays. Production from  $\Lambda_c$  decays is an alternative.**
- **The sensitivity to search for CP violation in hyperon decays at STCF can reach the limit predicted by SM.**
- **Large statistics of hyperon at STCF can get a better precision of  $V_{us}$  than that from K decays, and allow a better understand the SU(3) breaking effects.**
- **A better upper limits for  $\Delta_s=1$  or 2 rare decays**

# Basic ideas about generator supper-tau-charm factory

- Good news: the beam polarization option has been implimented in KKMC as author informed
- generation of charmonium produced from polarized beams can be realized by setting the spin matrix for the charmonium in EvtGen.



| decay modes                                | branching fractions                |
|--|------------------------------------|
| $\Sigma^- \rightarrow ne^- \bar{\nu}$      | $(1.017 \pm 0.034) \times 10^{-3}$ |
| $\Lambda \rightarrow pe^- \bar{\nu}$       | $(8.32 \pm 0.14) \times 10^{-4}$   |
| $\Xi^0 \rightarrow \Sigma^+ e^- \bar{\nu}$ | $(2.53 \pm 0.08) \times 10^{-4}$   |