

# Hadron Spectroscopy

A few introductory comments

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# Self Introduction

Home town: Brooklyn, New York City

“Bay Ridge- Sunset Park” area:

from  $\approx 1920 \rightarrow \approx 1970$ : “Little Norway”

$\approx 1970 \rightarrow$  now: NYC’s “Chinatown #3”

BS Physics City College of New York

MS & PhD University of Wisconsin

1972-1992 Professor at U. of Rochester

1992-2009 Professor at U. of Hawaii

2009-2014 Professor at Seoul National U.

1990  $\rightarrow$  now member of the Belle Experiment

1992  $\rightarrow$  now member of the BES I, BES II, & BES III expt

Research interests: CP violation

Hadron Spectroscopy

1984 1<sup>st</sup> time in China; started long-time collaboration  
with Prof. Zheng ZhiPeng (Zheng YangHeng’s father)

# Spectroscopy

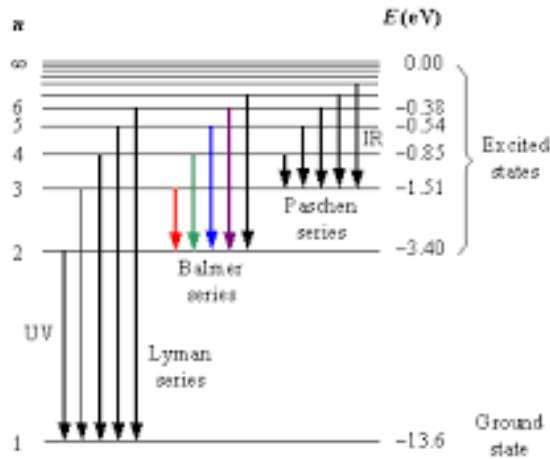
Powerful tool for understanding fundamental laws of Physics

Atomic (especially Hydrogen) spectra → Discovery of QM  
& Pauli Exclusion Principle

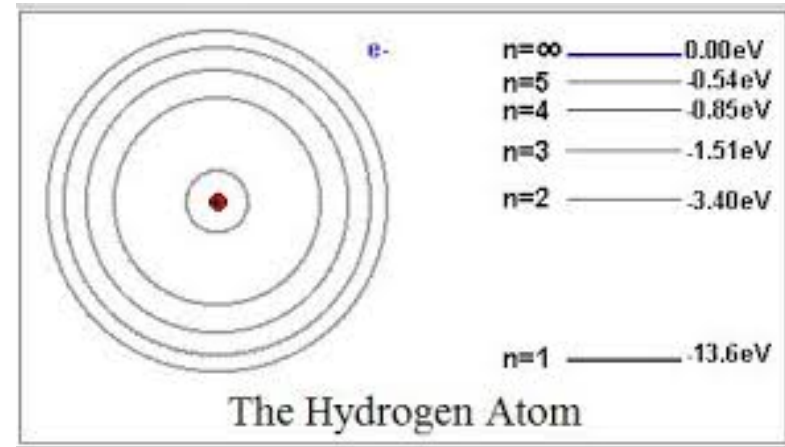
Nuclear Spectroscopy → Discovery & properties of the strong force

Hadron Spectroscopy → Discovery of Flavor & Quarks

# Hydrogen Atom Spectrum



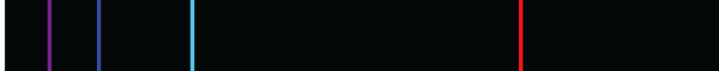
Energy levels of the hydrogen atom, with some of the transitions between them that give rise to the spectral lines indicated



Absorption of visible light



Emission of visible light



656.1 nm | 486.1 nm | 434.1 nm | 410.2 nm

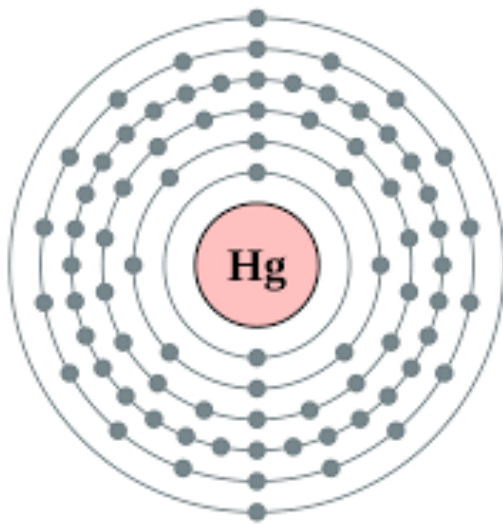
Balmer formula:  $E_n = \frac{13.6\text{eV}}{n^2}$

$$13.6\text{eV} = \frac{\mu_e e^4}{2\hbar^2}$$

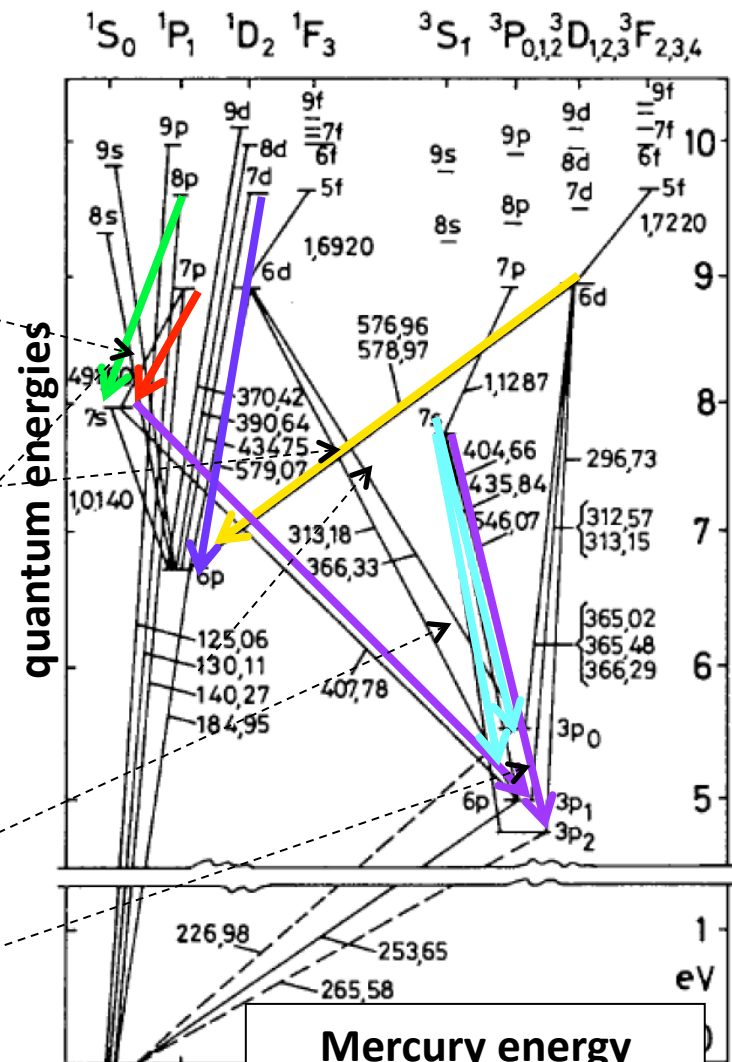
# Decoding atomic spectra

80: Mercury

2,8,18,32,18,2



Mercury  
spectrum



(a)

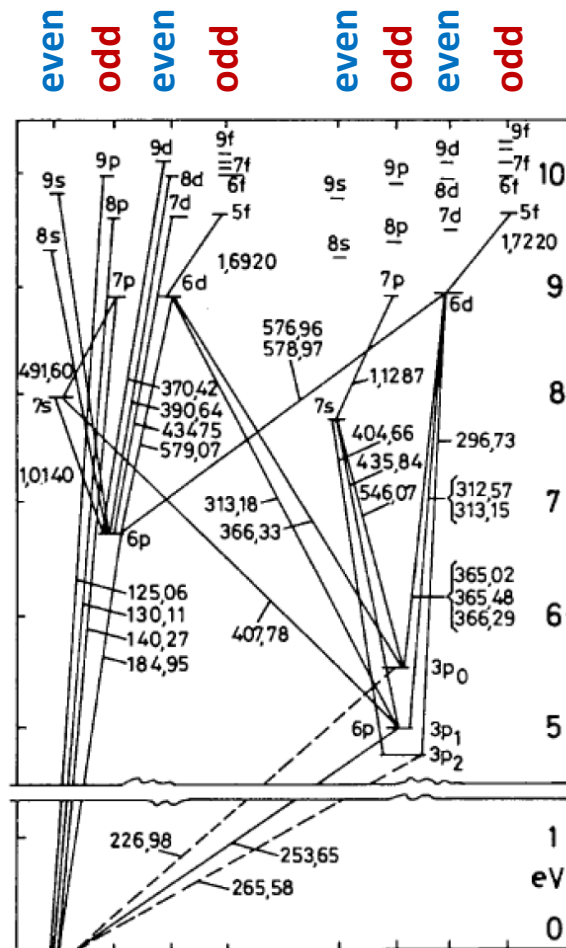
λ(nm) (b) ©2011



Otto Laporte  
1902-1971

# 1924 Otto Laporte

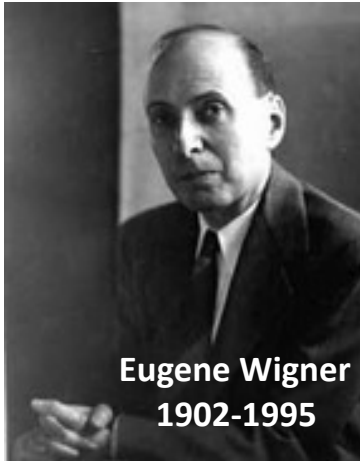
Allowed quantum states are *either* even or odd



## Laporte rule

even  $\rightarrow$  odd OK  
 odd  $\rightarrow$  even OK  
 even  $\nrightarrow$  even not allowed  
 odd  $\nrightarrow$  odd not allowed

# Wigner: Laporte rule is a consequence of Left-Right symmetry of Nature



**Left  $\leftrightarrow$  Right symmetry  
= “Parity” symmetry**

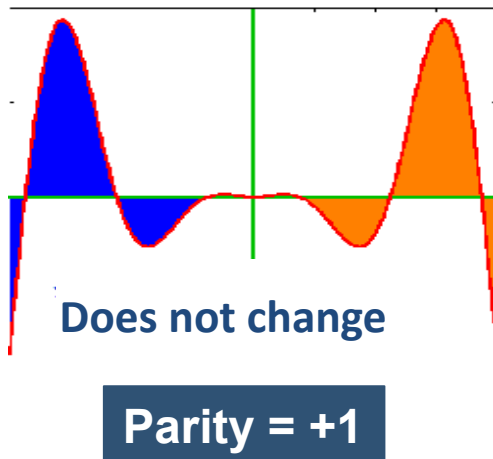
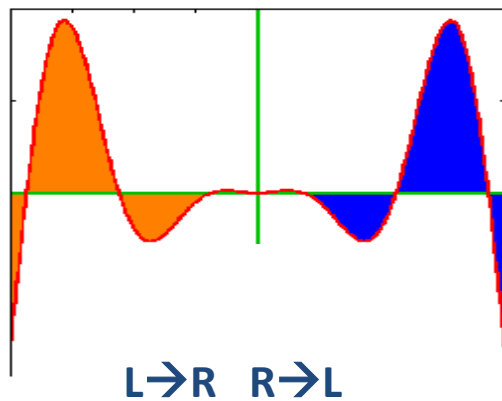
Rules governing Atomic Physics (E&M) are  $L \leftrightarrow R$  symmetric:

i.e., they “Conserve” Parity

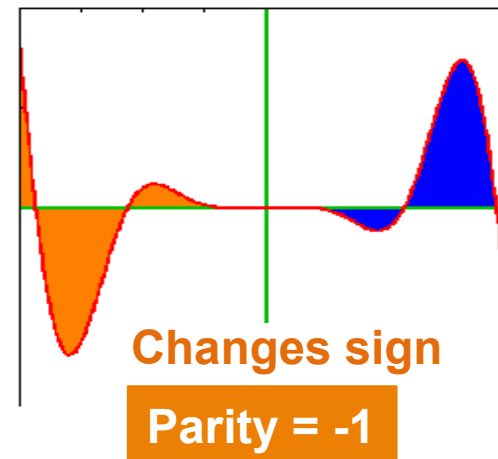
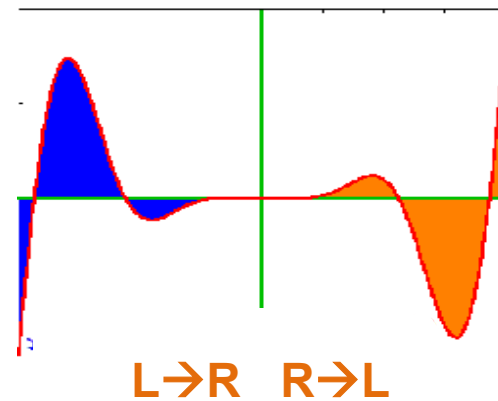
**1963 Nobel Physics prize “for the discovery and application of fundamental symmetry principles”**

# Even & Odd quantum functions

Even Function



Odd Function

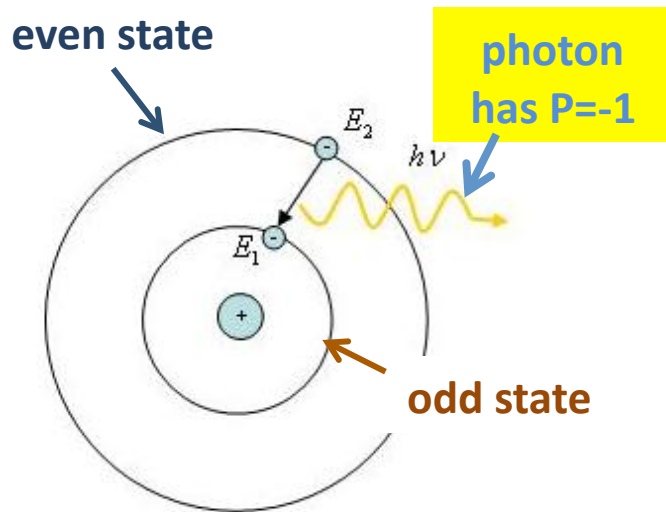


# Parity Conservation in QM

Left  $\leftrightarrow$  Right symmetry of Nature



Conservation of Parity



initially:

even state  
( $P_{\text{even}}=+1$ )

$$P_{\text{initial}}=+1$$

finally:

odd state + Photon  
( $P_{\text{odd}}=-1$ ) ( $P_{\text{phot}}=-1$ )

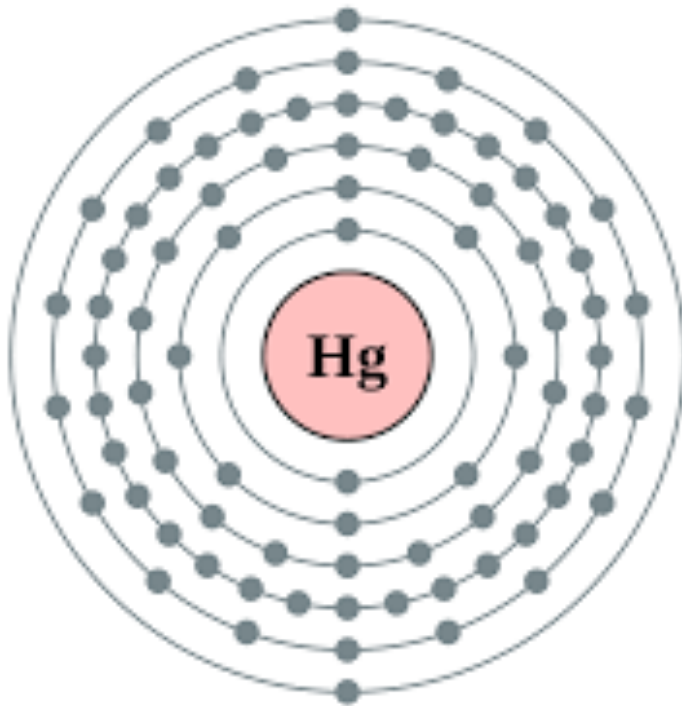
$$P_{\text{final}}=(-1)(-1)=+1$$

Parity is conserved

# Atomic shell structure

80: Mercury

2,8,18,32,18,2



properties of  $Y_l^m(\theta, \varphi) \rightarrow$  shells

$$\frac{1}{\sin \theta} \frac{\partial}{\partial \theta} \left( \sin^2 \theta \frac{\partial Y}{\partial \theta} \right) + \frac{1}{\sin^2 \theta} \frac{\partial^2 Y}{\partial \varphi^2} = -\lambda Y$$

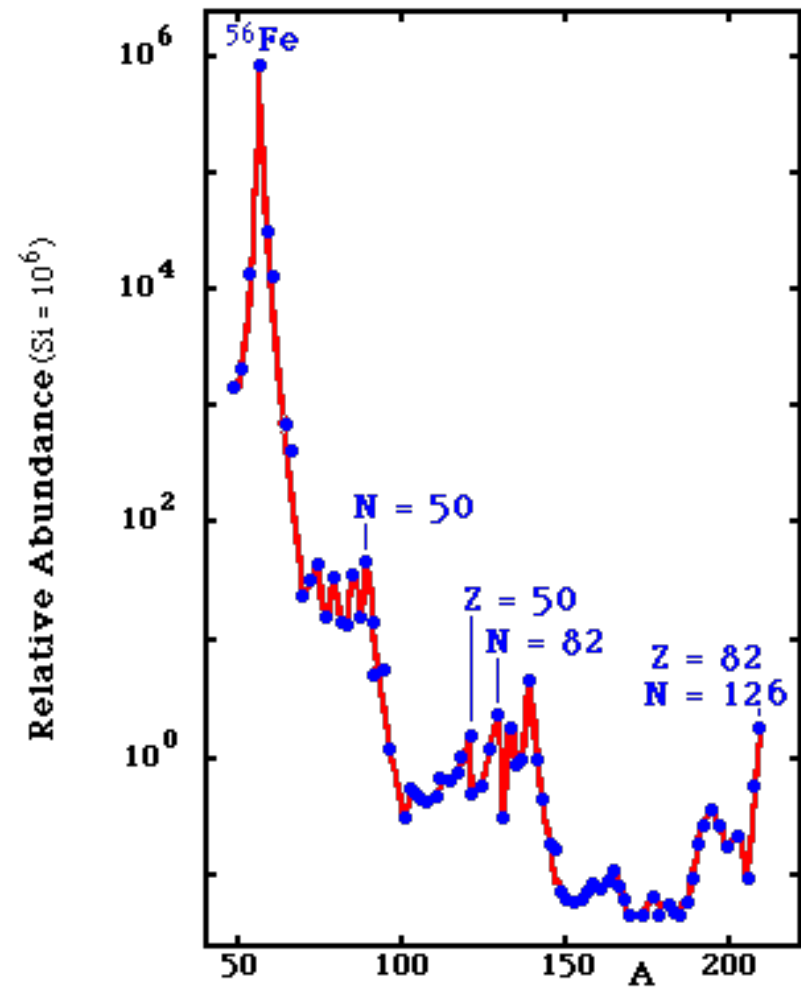
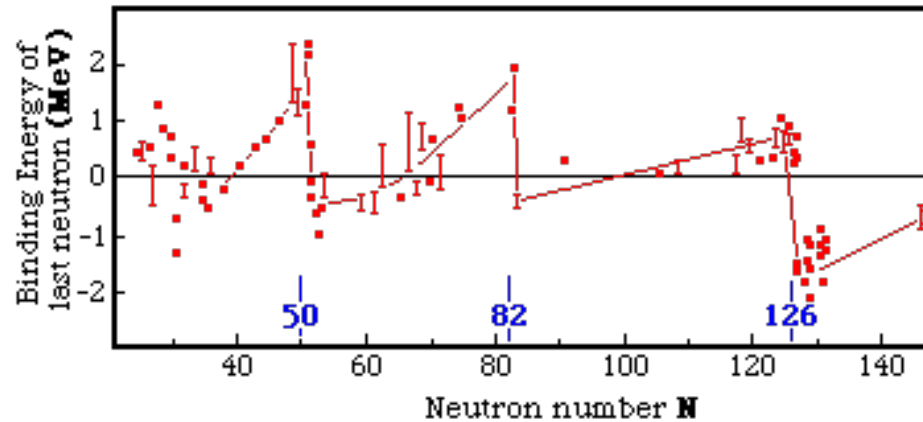
Solutions:  $Y_l^m(\theta, \varphi)$ ;  $\lambda = l(l+1)$  &  $|m| \leq l$

$m$  &  $l$  are integers

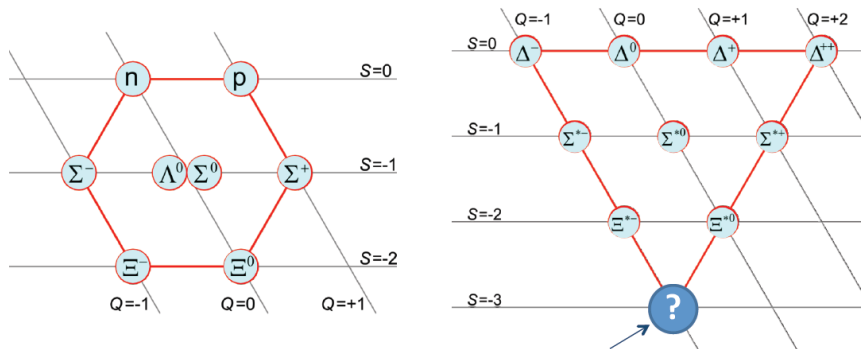
Same for all spherically symmetric systems

# Nuclear Spectroscopy

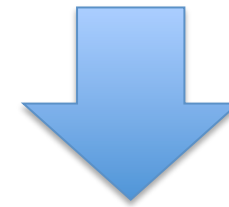
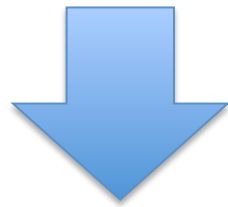
Shell structure in nuclei



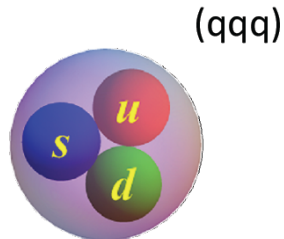
# Hadron Spectroscopy



$SU(3)$



$$\pi^- = (d\bar{u})$$



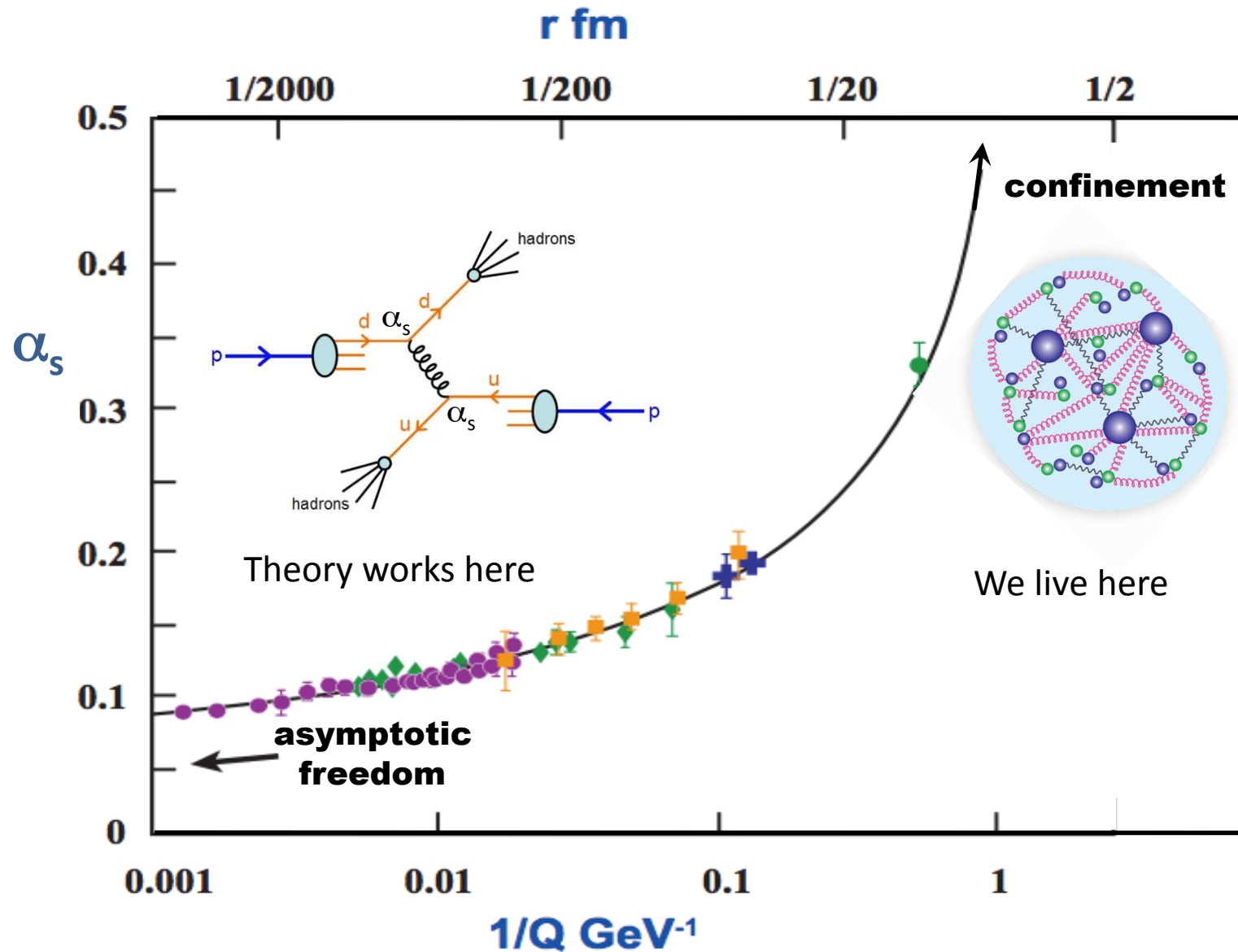
$$\Lambda = (uds)$$

Quarks

# Atomic- vs Nuclear- vs Hadron- spectroscopy

|         | Constituent particles                          | Interparticle force                               |
|---------|------------------------------------------------|---------------------------------------------------|
| Atoms   | electrons/protons<br>well understood           | Coulombic<br>well understood                      |
| Nuclei  | protons/neutrons<br>well understood            | Nuclear potential<br>empirical models             |
| Hadrons | quarks/antquarks/gluons<br>NOT well understood | Long-range QCD color force<br>NOT well understood |

# The QCD “dilemma”



# QCD Lagrangian

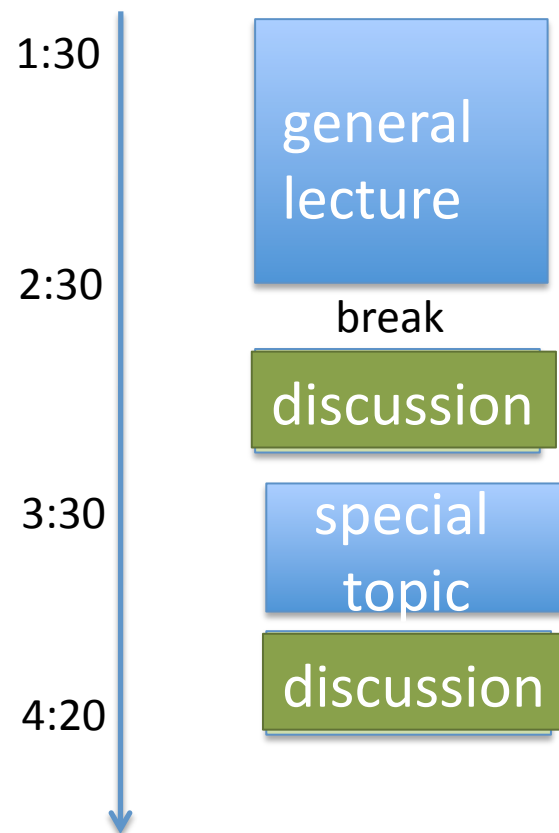
$$\mathcal{L}_{\text{QCD}} = \bar{\psi}_i (i(\gamma^\mu D_\mu)_{ij} - m \delta_{ij}) \psi_j - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}$$

$$G_{\mu\nu}^a = \partial_\mu \mathcal{A}_\nu^a - \partial_\nu \mathcal{A}_\mu^a + gf^{abc} \mathcal{A}_\mu^b \mathcal{A}_\nu^c$$

$\mathcal{A}_\mu^a$ ,  $a=1, \dots, 8$ , are the gluon fields

- In principle, all details of hadron spectroscopy are contained in this Lagrangian
- For distances the size of hadrons (or nuclei), it is hopelessly difficult to solve
- No useful mathematical expressions relevant to hadron spectroscopy that are based on first principle QCD calculations have ever been realized.
- Maybe a better understanding of the hadron spectrum will translate into a better understanding of long-distance QCD

# Plan for these classes



# Plan for the course

## Main Lectures

1<sup>ST</sup> hadrons, quantum numbers, notation  
-- octets and decuplets –

SU(3) and quarks light-quark spectroscopy  
-- discovery of QCD---

Charmonium mesons, QCD's "hydrogen atom"

tetra-quarks, pentaquarks, hadronic molecules, ...

## special topics

Dalitz plots

angular  
distributions

multi-dimensional  
analyses