

# Gluonic Probe for the Short Range Correlations in Nucleus

Feng Yuan

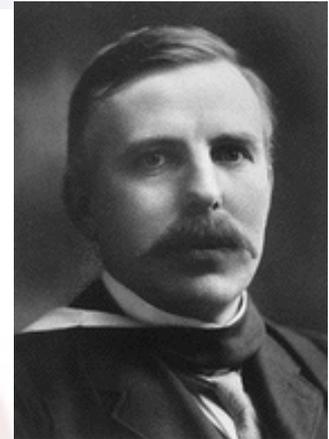
Lawrence Berkeley National Laboratory

Xu, Yuan, PLB 801, 135187 (2020)

Hatta, Strikman, Xu, Yuan, PLB 803, 135321 (2020)

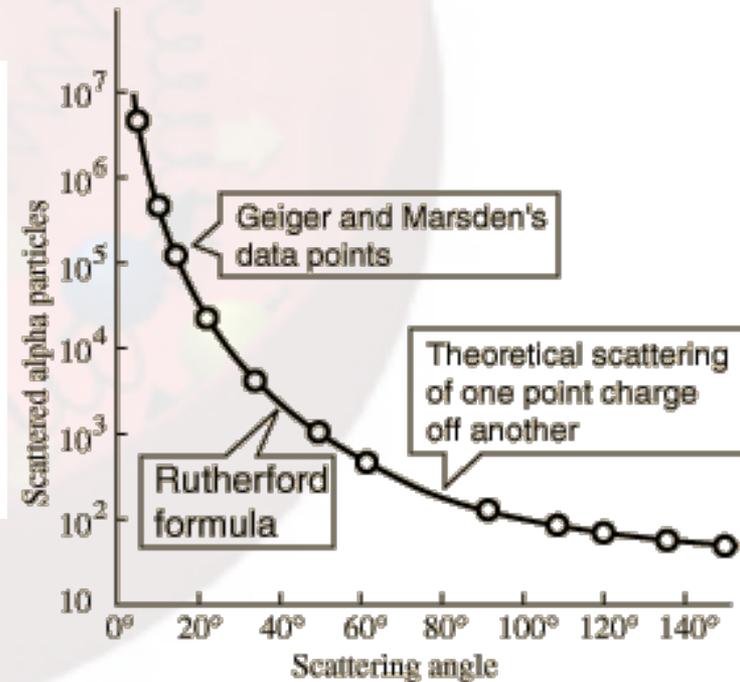
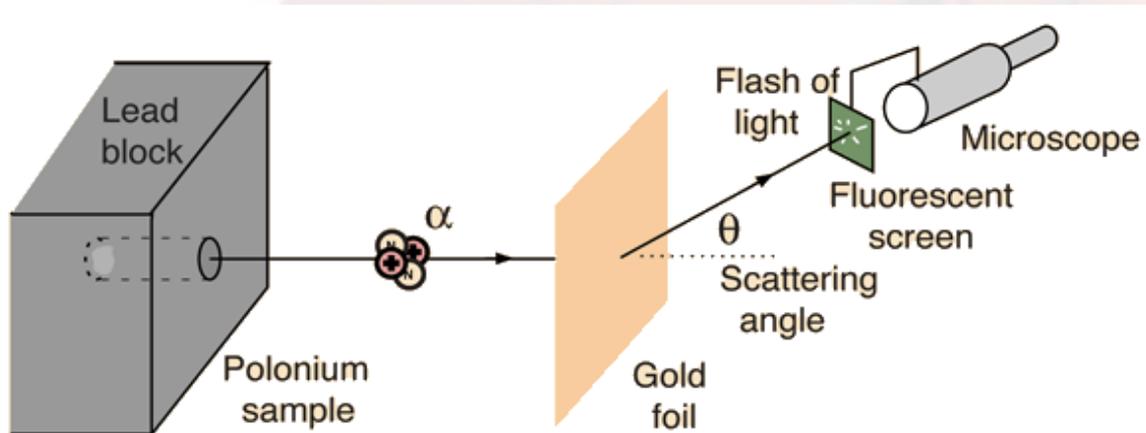


# Rutherford scattering



The Scattering of  $\alpha$  and  $\beta$  Particles by Matter and the Structure of the Atom

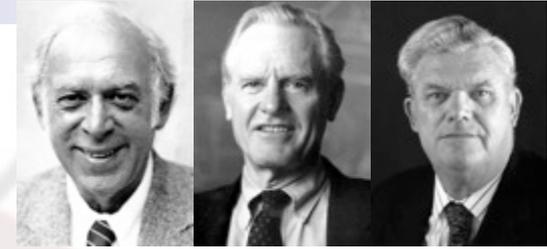
E. Rutherford, F.R.S.\*  
*Philosophical Magazine*  
Series 6, vol. 21  
May 1911, p. 669-688



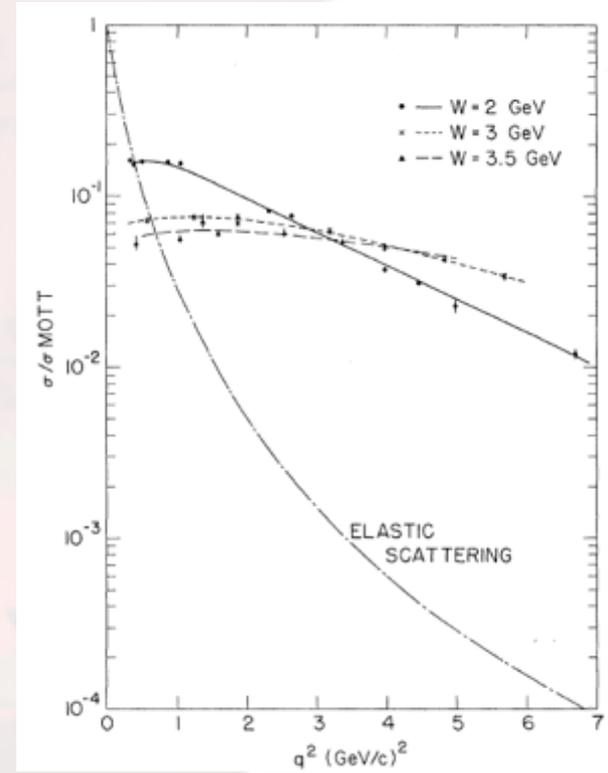
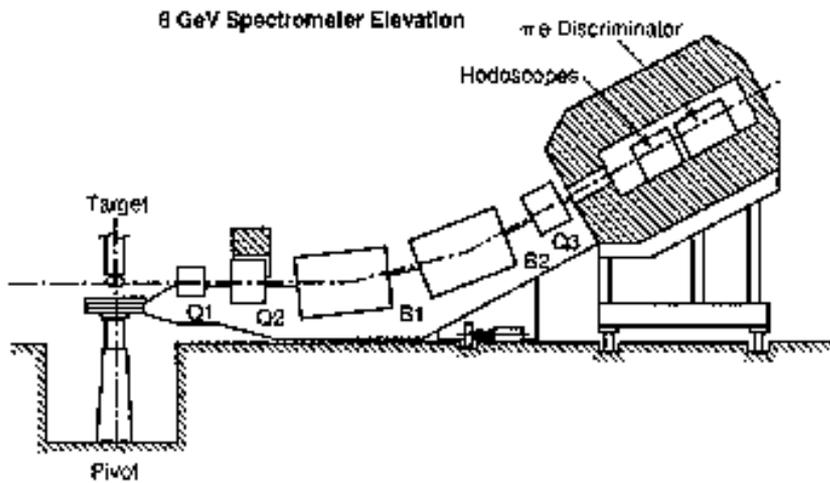
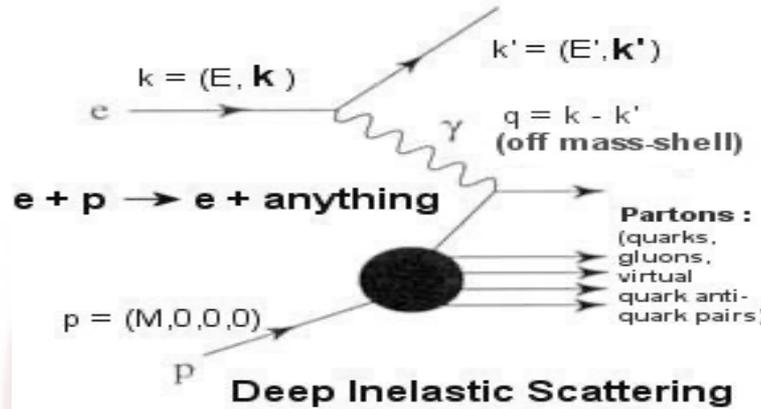
Discovery of Nuclei

# Deep Inelastic Scattering

## Discovery of Quarks



Friedman Kendall Taylor



**Bjorken Scaling:  $Q^2 \rightarrow \text{Infinity}$**   
**Feynman Parton Model:**  
**Point-like structure in Nucleon**

# Quantum Chromodynamics



- There is no doubt that QCD is the right theory for hadron physics
- However, many fundamental questions...
- How does the **nucleon mass** emerge from the light quarks dynamically?
- Why quarks and gluons are **confined** inside the nucleon?
- How do the fundamental **nuclear forces** arise from QCD?
- We don't have a **comprehensive picture** of the nucleon structure as we don't have an approximate QCD nucleon wave function

# Central questions for nuclear structure physics

**Where** do heavy elements come from?

**How** does the nuclear chart emerge from QCD?

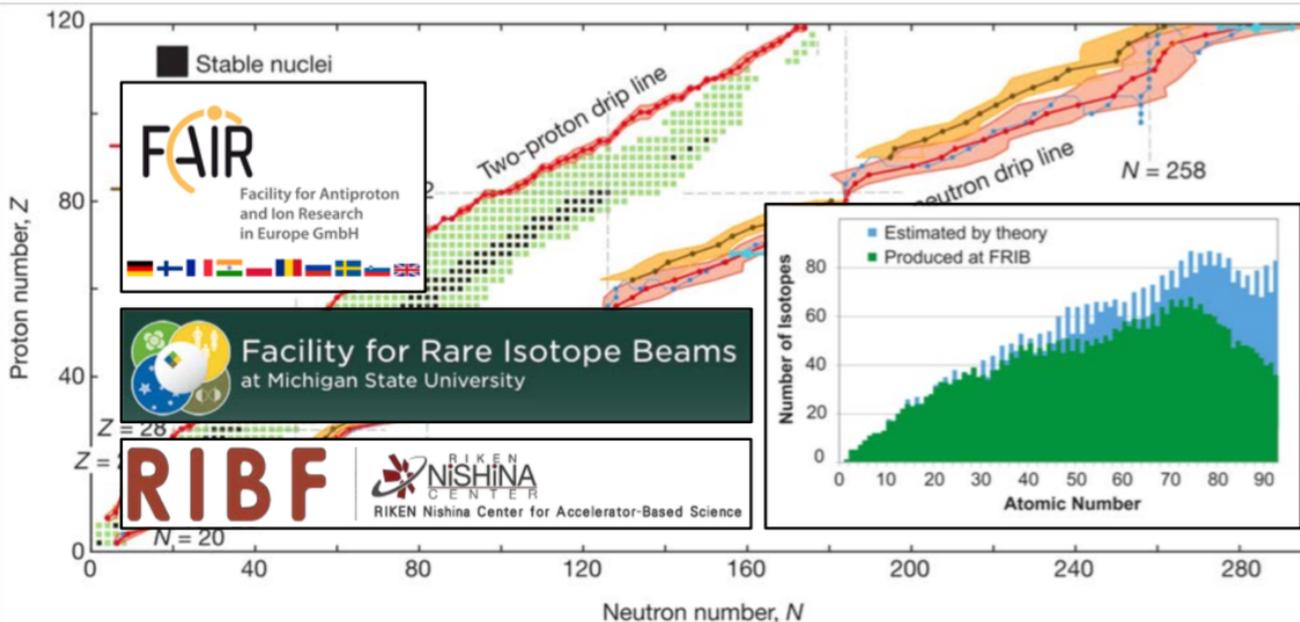
**How** to predict properties of nuclei?

observables

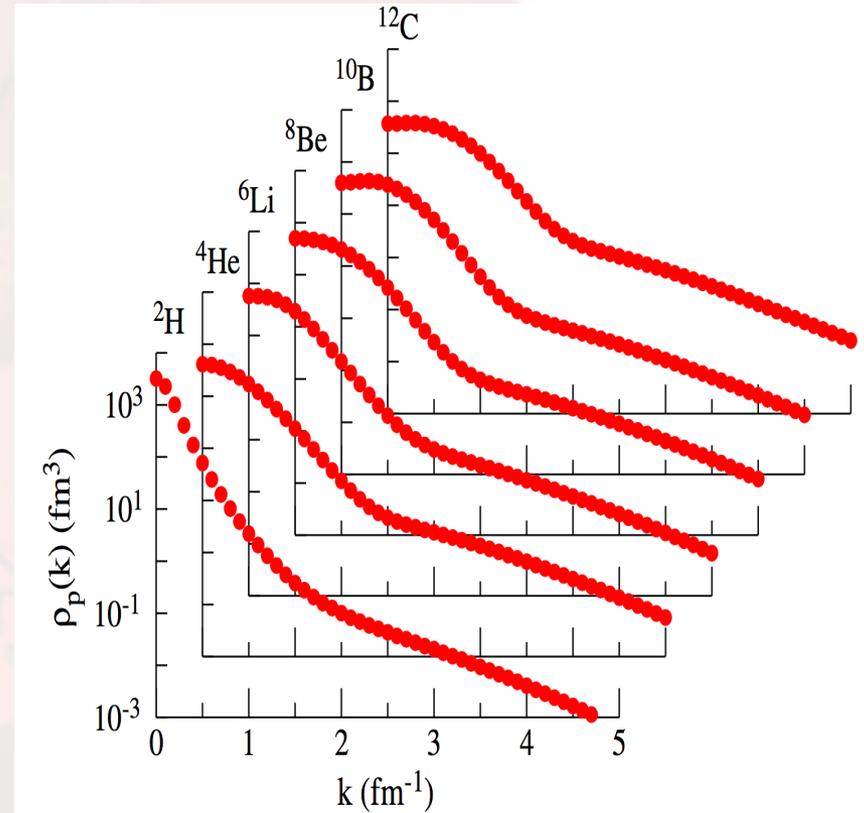
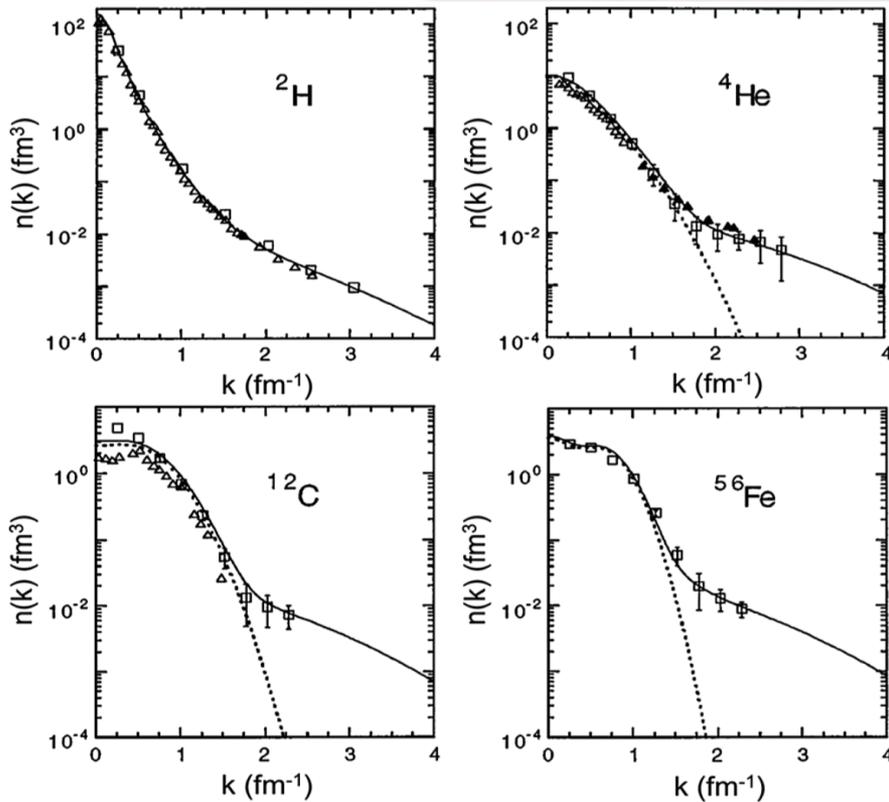
many-body  
framework

effective  
field theory

quantum  
chromodynamics



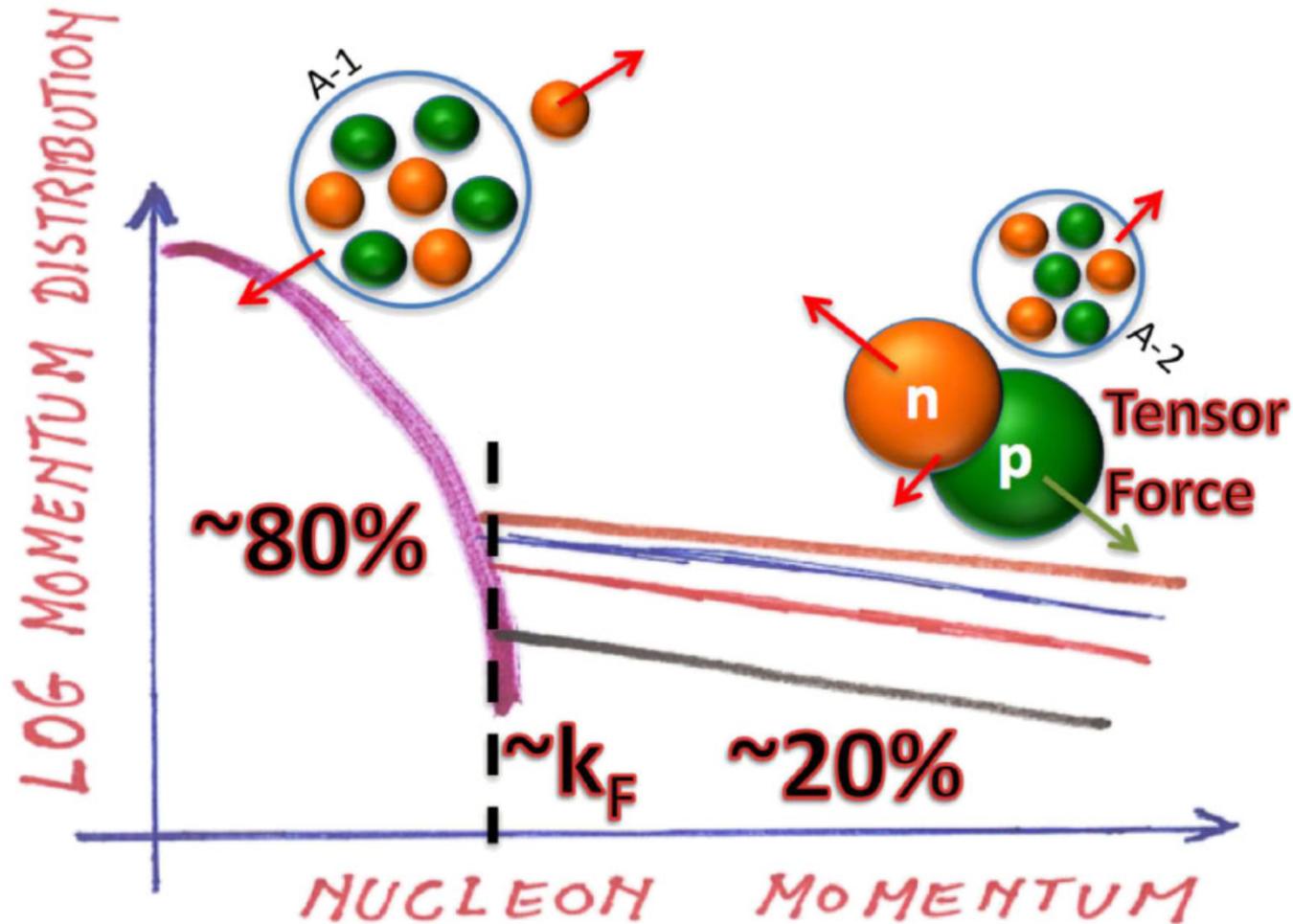
# Nucleon momentum distribution inside nucleus



Electron scattering exp.

Carlson et al, RMP, 2015

# Basic Picture



# What is short-range correlation

- Neutron-proton close in coordinate space
- Momentum space
  - Low total momentum
  - High relative momentum

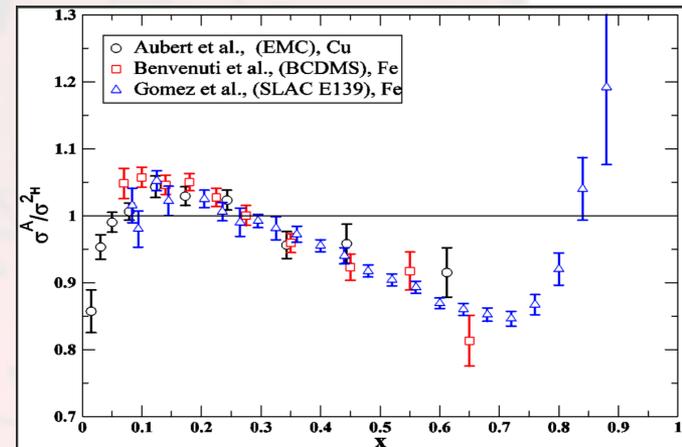
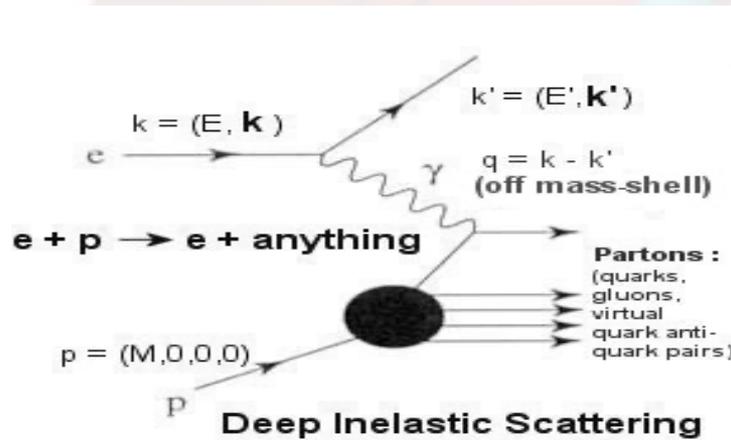
# Three Different Ways to Probe the SRC

- Momentum distribution of nucleons
  - Limited to low momentum region
- Knock out experiments
- Hard partonic processes: structure function modifications
  - EMC effects
  - Fast moving partons
    - (Structure function at  $x_B > 1$ )

JLab's major  
Activities:  
Quark

# EMC: nuclear modification of structure functions

- DIS structure function measures the parton distribution in nucleon/nucleus



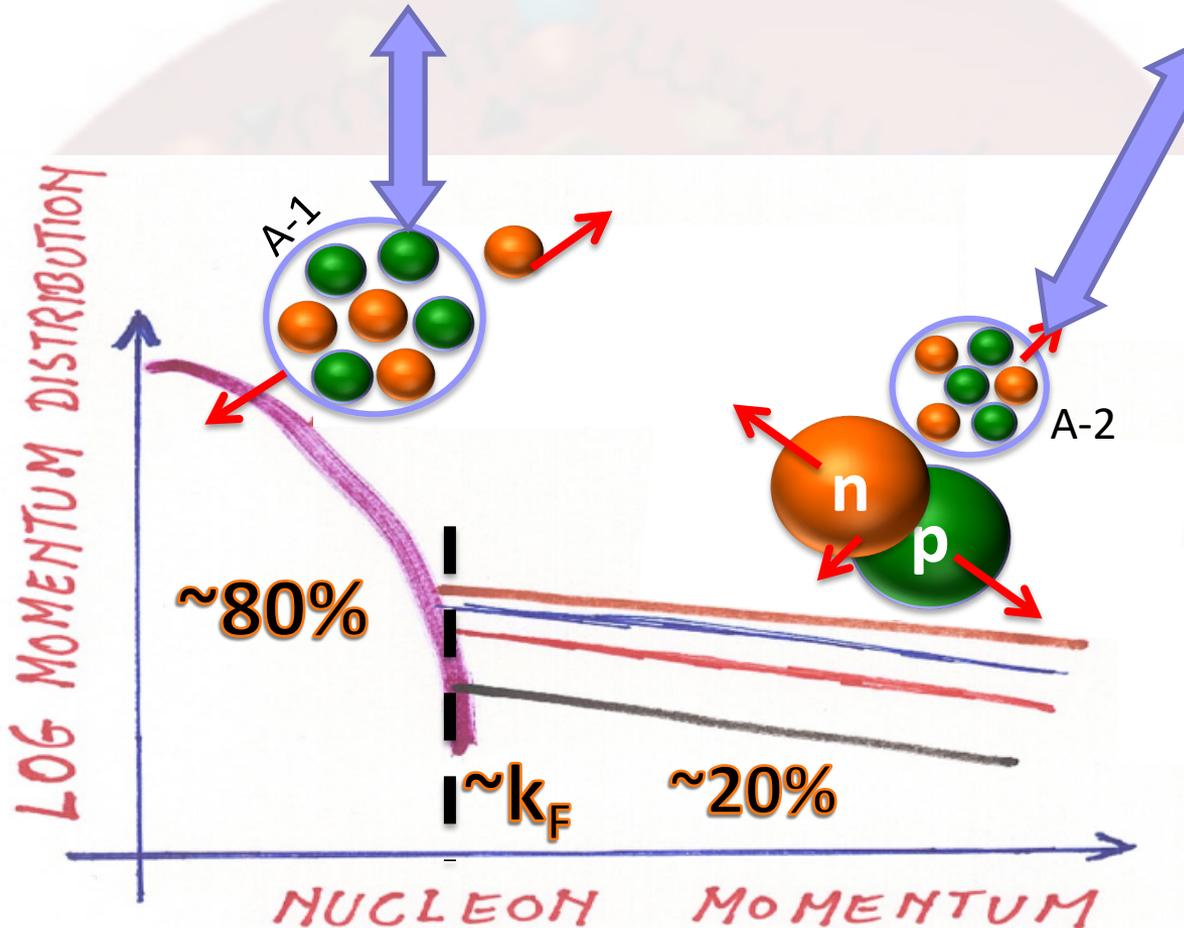
$$F_2^A = Z F_2^p + N F_2^n$$



$$\frac{\sigma_A / A}{\sigma_D / 2} \approx 1$$

# Bound = 'quasi Free' + Modified SRCs

$$\sigma_A = n_p \sigma_p + n_n \sigma_n + n_{np} (\Delta \sigma_p + \Delta \sigma_n)$$



Universality is the key to establish the physics associated with SRC!!

# Universality of SRC Contributions

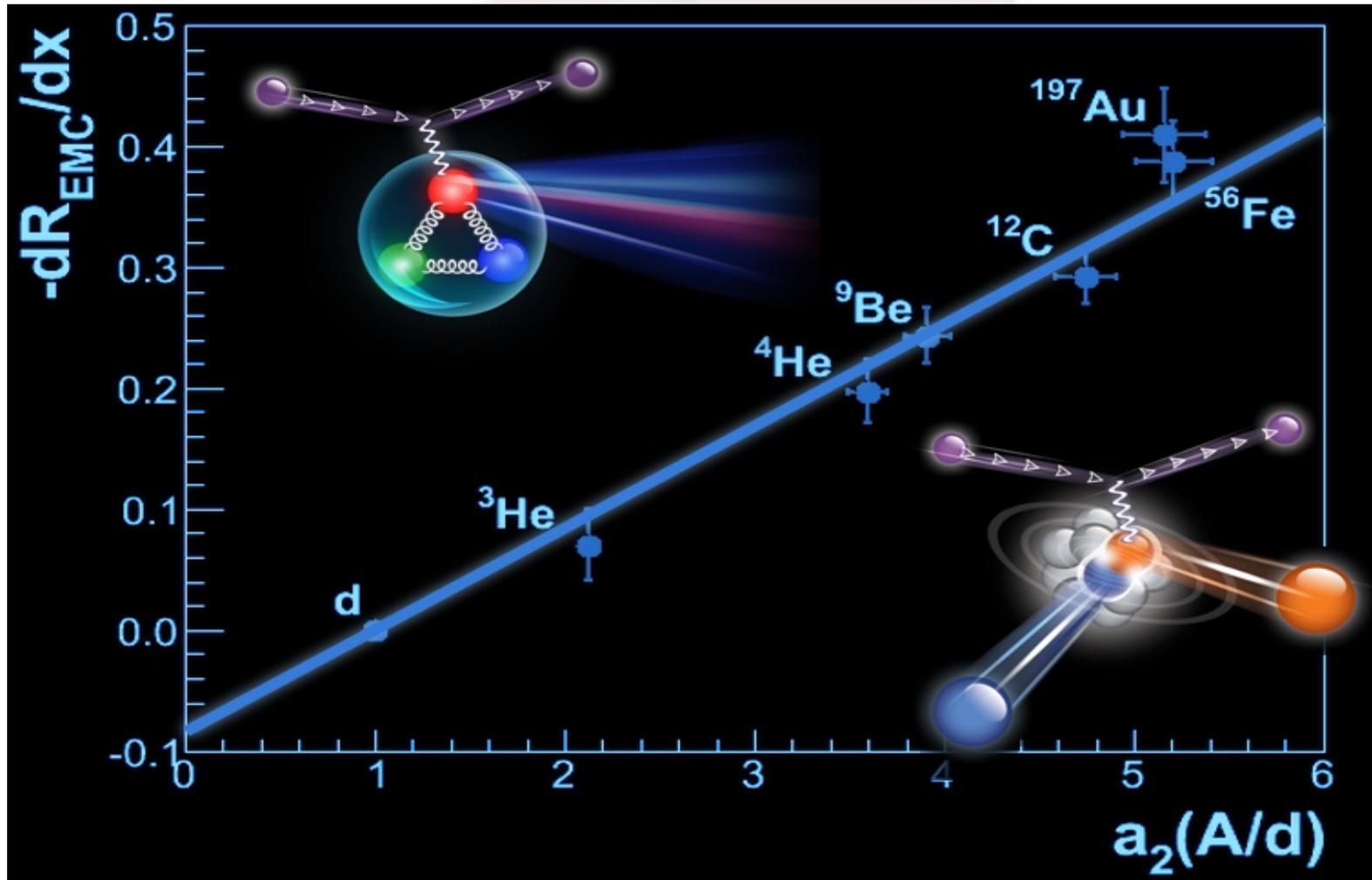
## ■ Different processes

- Same SRC pair contribute to different hard processes
- Universal partonic structure

## ■ Different nuclei

- Only depend on the probability of the SRC pair, nuclear dependence same for different processes
- Link different nuclei by the SRC factors

# Universality: Quark Sector



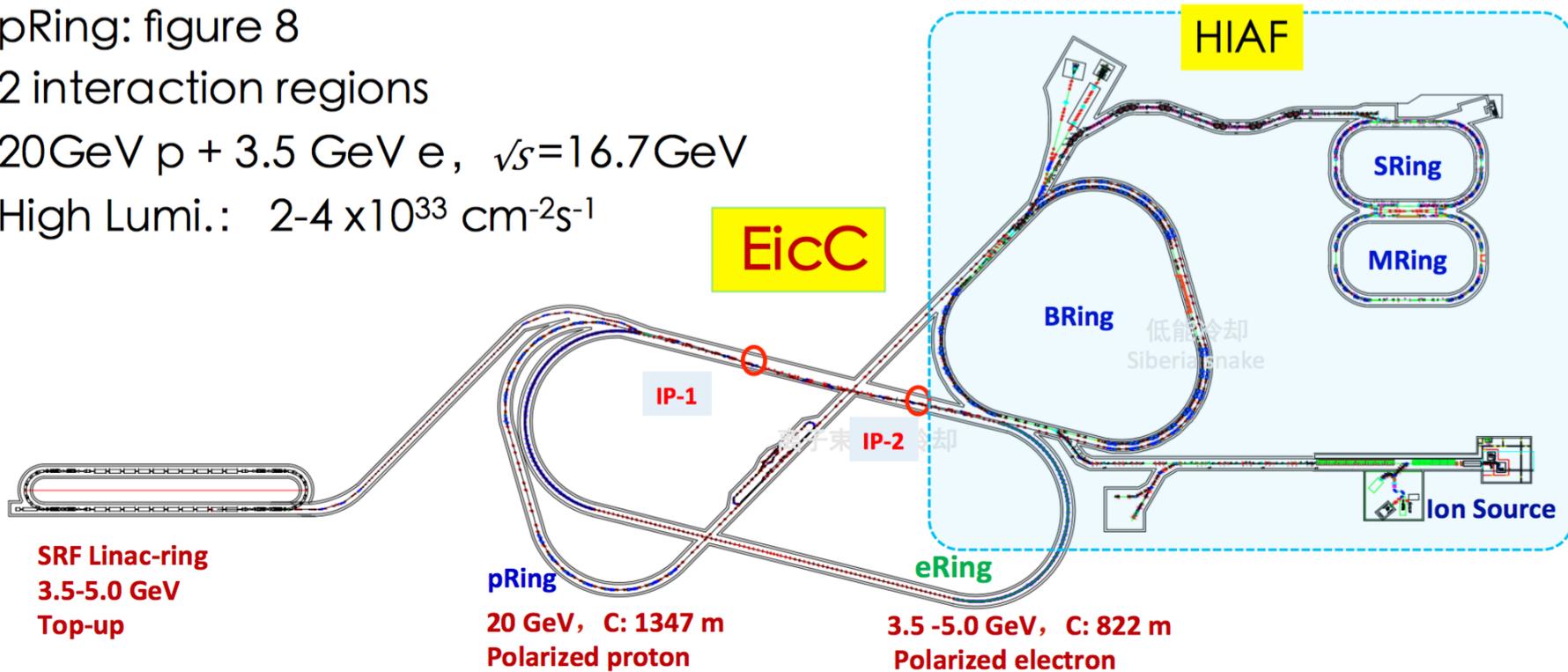
# Gluonic probe for SRC at an Intermediate Energy EIC

- Kinematic focus will be in the EMC region
- Energy is high enough to study heavy flavor production
  - Charm Structure Function
  - Sub-threshold production of open Charm and Charmonium

# Polarized Electron-Ion Collider in China **EicC**

## EicC Accelerator Complex

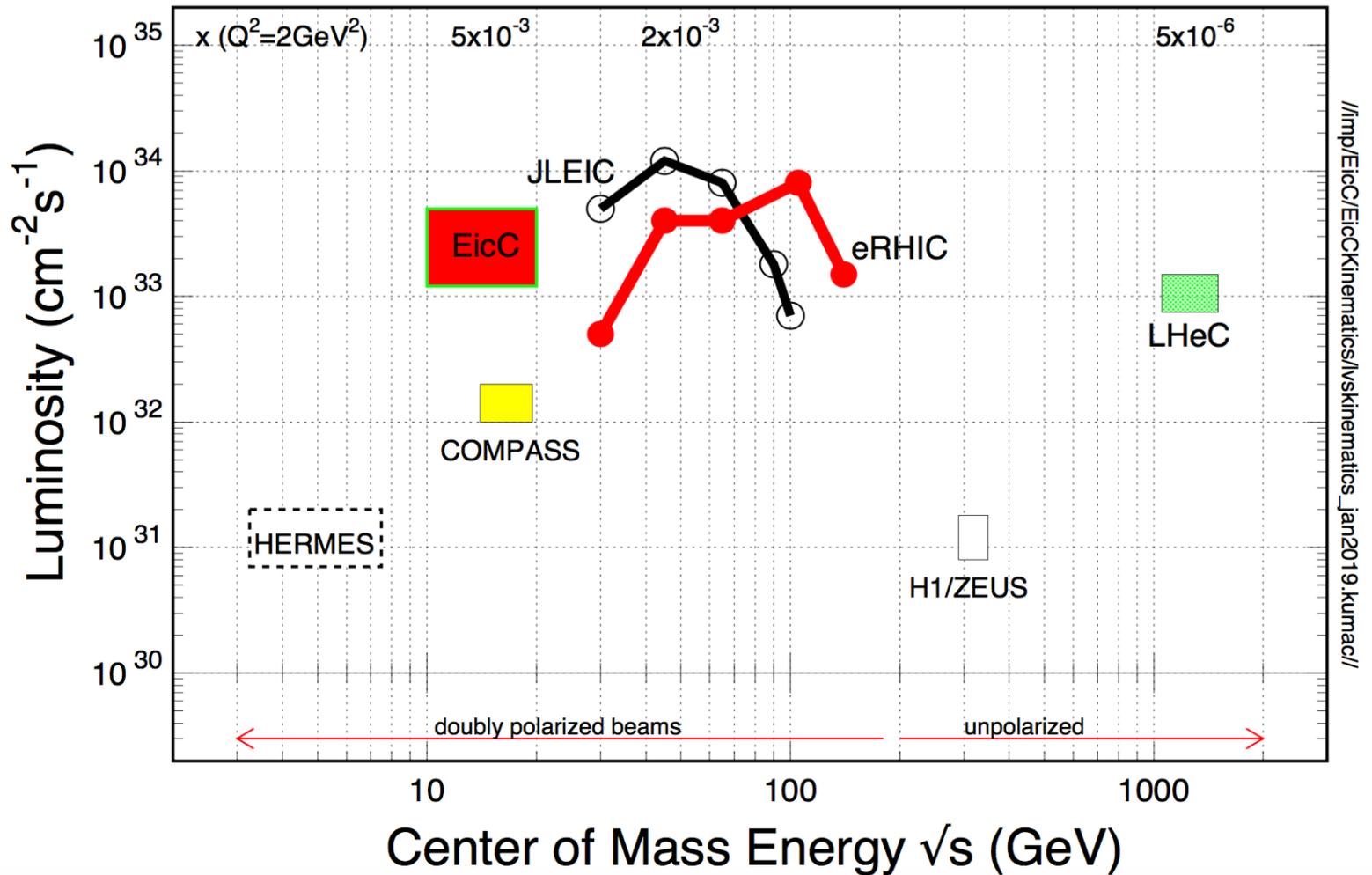
- pRing: figure 8
- 2 interaction regions
- 20 GeV p + 3.5 GeV e,  $\sqrt{s}=16.7\text{ GeV}$
- High Lumi.:  $2-4 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$



Nu Xu@QCD Workshop,  
Weihai, July 2019



# Designed Energy and Luminosity



# Gluon distribution in nucleus: SRC contributions

- Because of isospin symmetry:

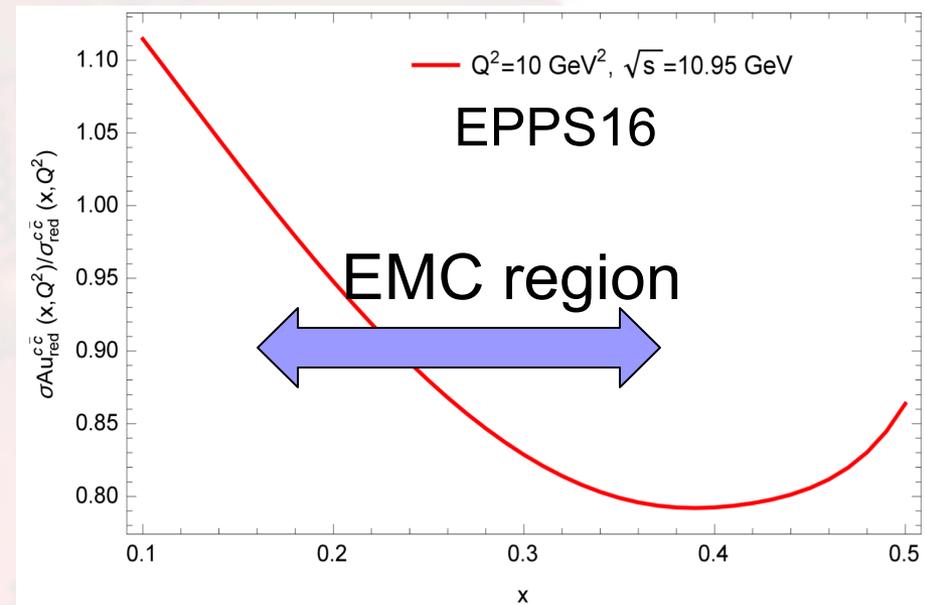
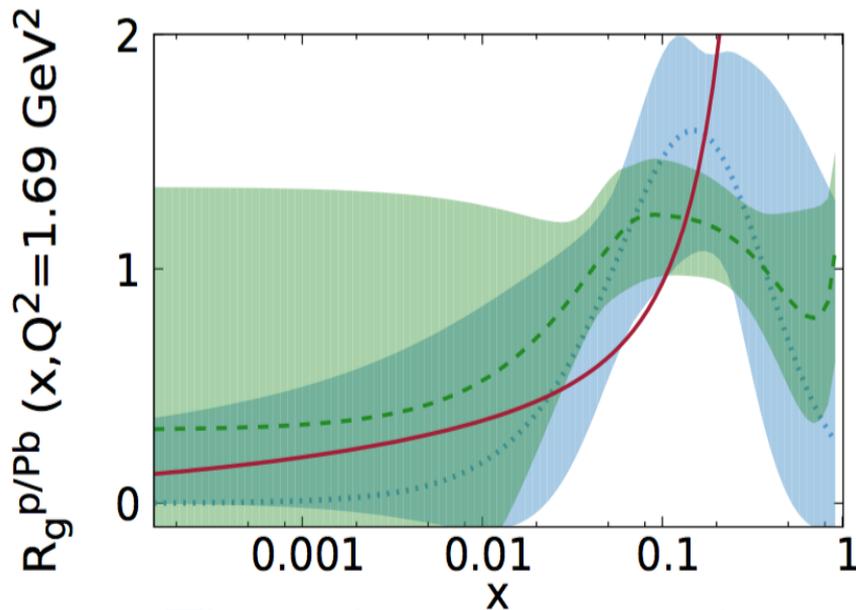
$$g_A(x, Q^2) = Ag_p(x, Q^2) + 2n_{src}^A \delta \tilde{g}(x, Q^2)$$

- Compare to the quark sector

$$\begin{aligned} F_2^A &= (Z - n_{src}^A) F_2^p + (N - n_{src}^A) F_2^n + n_{src}^A (F_2^{p*} + F_2^{n*}) \\ &= ZF_2^p + NF_2^n + n_{src}^A (\Delta F_2^p + \Delta F_2^n) \end{aligned}$$

**SRC Factor:  $n_{src}^A$**

# EMC Effects in Charm $F_2$ at EicC

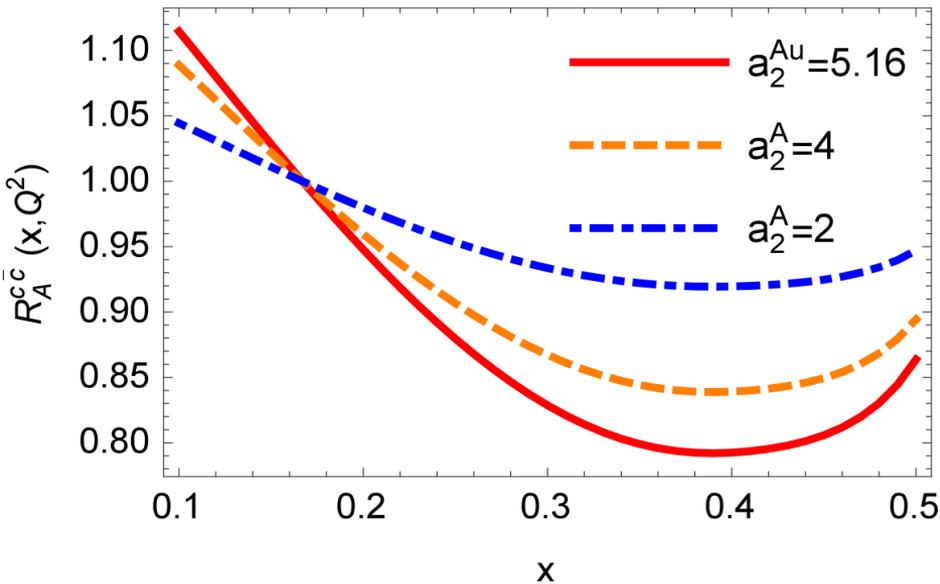


There is no constraint for the gluon EMC:  
 EPPS16, 1612.05741  
 nCTEQ, 1509.00792  
 TUJU19, 1908.03355

Gluon momentum fraction=  
 $x(1+4m_c^2/Q^2)$

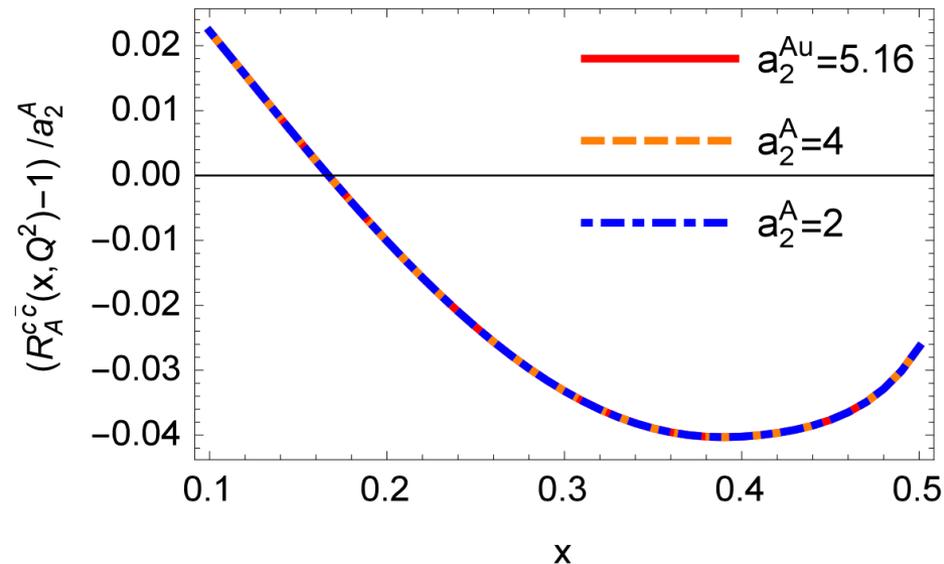
# Universality of the nuclear modifications

$Q^2=10 \text{ GeV}^2, \sqrt{s}=10.95 \text{ GeV}$

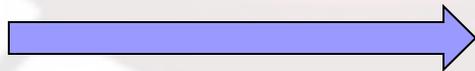


Au: EPPS16; others follow the universal behavior

$Q^2=10 \text{ GeV}^2, \sqrt{s}=10.95 \text{ GeV}$



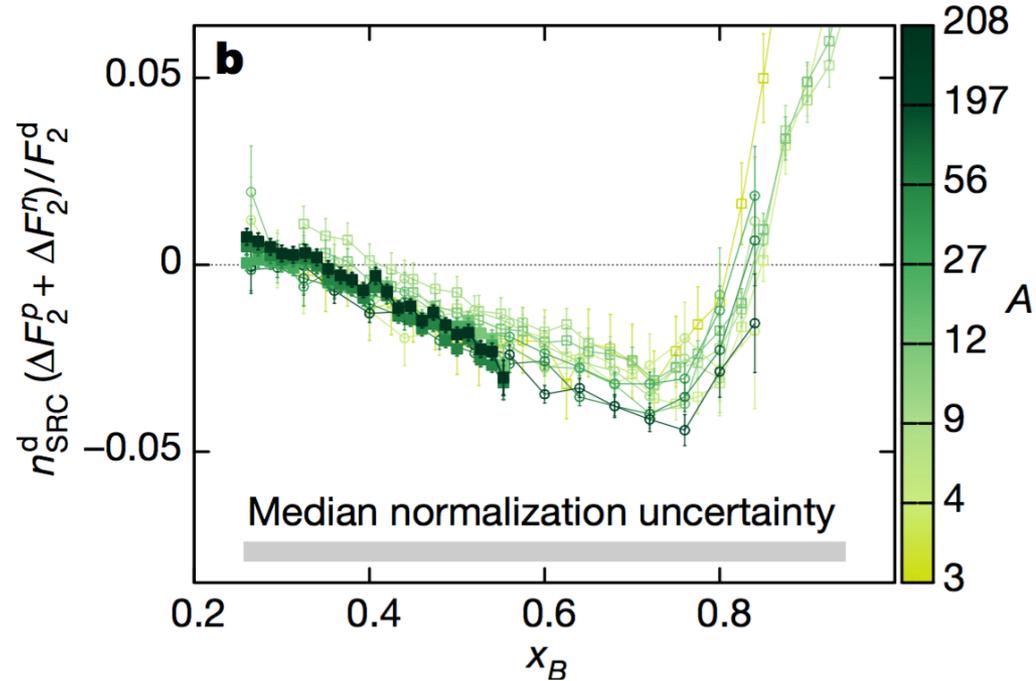
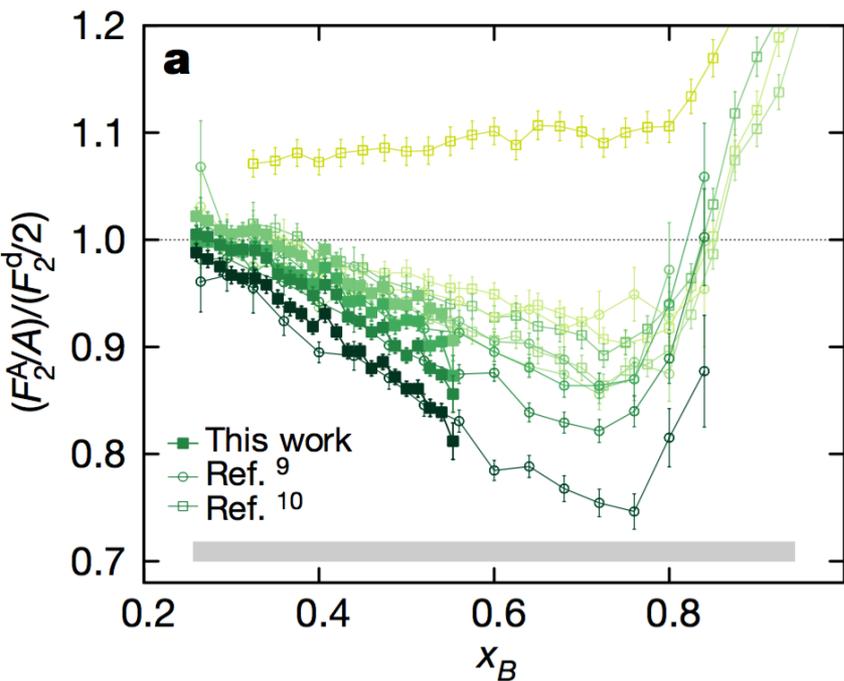
Divide by the SRC Factor



$$a_2^A = (n_{src}^A / A) / (n_{src}^d / 2)$$

5/4/20

# Quark sector: Isospin dependence



CLAS Coll., Nature 2019  
See also, Hen et al, 1908.02223

$$\frac{n_{\text{SRC}}^d (\Delta F_2^p + \Delta F_2^n)}{F_2^d} = \frac{\frac{F_2^A}{F_2^d} - (Z-N) \frac{F_2^p}{F_2^d} - N}{(A/2)a_2 - N}$$

# Universality of SRC: two facts

- EMC effects for different nuclei can be described by the same universal SRC contributions
  - Quark/gluon shall differ
- The same SRC factor for both quark and gluon sectors

# Jpsi production: build a model for SRC contributions

- Jpsi production in photo-nuclear collisions

$$\sigma_{\gamma A \rightarrow J/\psi}(\sqrt{s_{\gamma p}}) = A\sigma_{\gamma p \rightarrow J/\psi}(\sqrt{s_{\gamma p}}) + n_{src}^A(\sigma_{\gamma(pn) \rightarrow J/\psi}(\sqrt{s_{\gamma p}}) - 2\sigma_{\gamma p \rightarrow J/\psi}(\sqrt{s_{\gamma p}}))$$

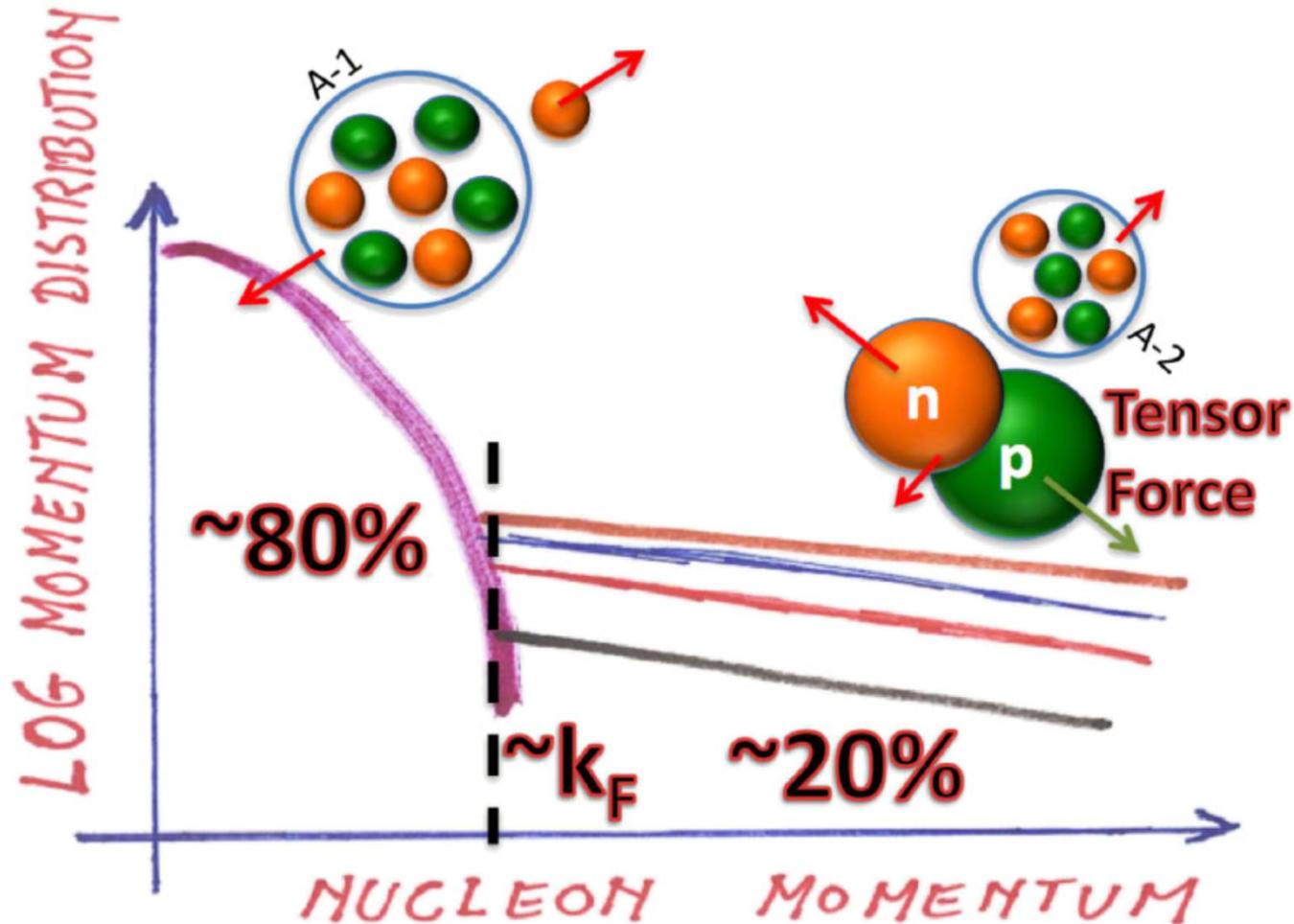
- Below the photon-proton threshold

$$\sigma_{\gamma A \rightarrow J/\psi}(\sqrt{s_{\gamma p}} < M_p + M_{J/\psi}) = n_{src}^A \sigma_{\gamma(pn) \rightarrow J/\psi}(\sqrt{s_{\gamma p}})$$

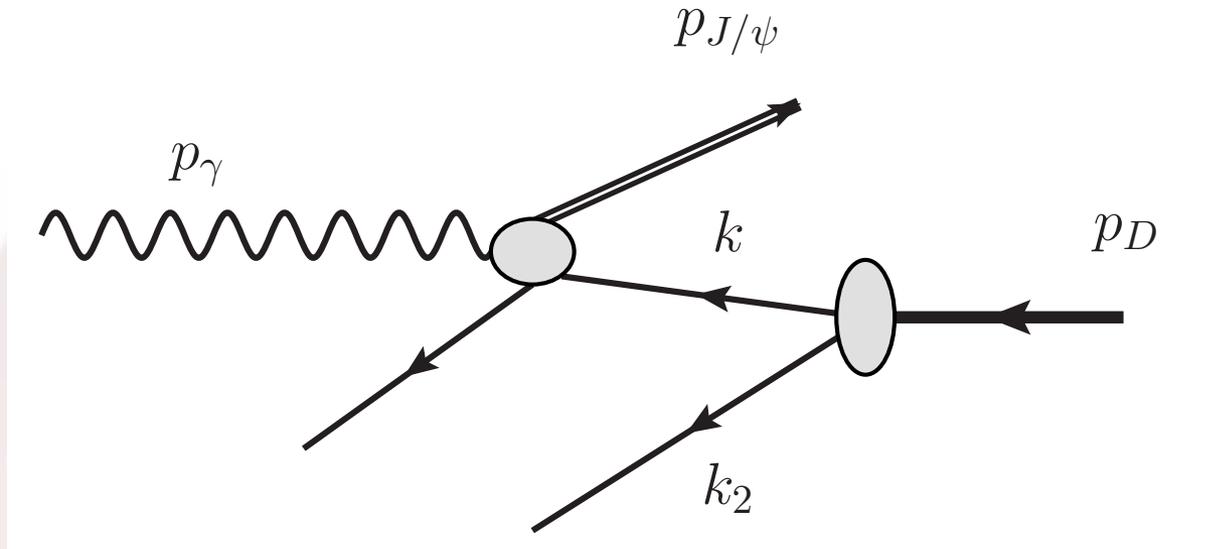
- Universality

$$\frac{\sigma_{\gamma A \rightarrow J/\psi}(\sqrt{s_{\gamma p}} < M_p + M_{J/\psi})}{\sigma_{\gamma d \rightarrow J/\psi}(\sqrt{s_{\gamma p}} < M_p + M_{J/\psi})} = \frac{n_{src}^A}{n_{src}^d} = \frac{F_2^A(x_B)}{F_2^d(x_B)} \Big|_{1.5 < x_B < 2.0}$$

# However: Mean Field Contributions



# Example: Deuteron Case

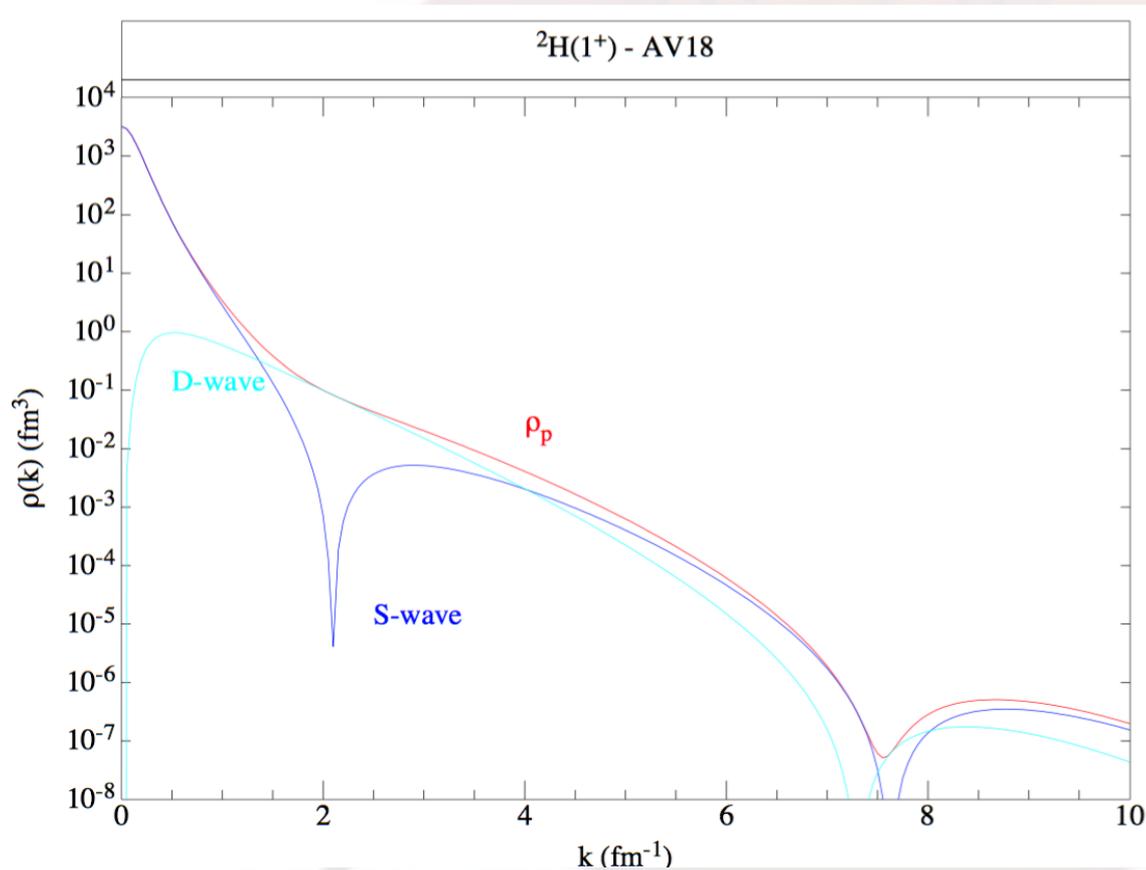


$$\sigma_{\gamma D}(W_{\gamma p}) = 2 \int d^3 k \rho_n(k) \tilde{\mathcal{F}}(k) \sigma_{\gamma p}(W_{\gamma p'})$$

Nucleon's  
Momentum distribution

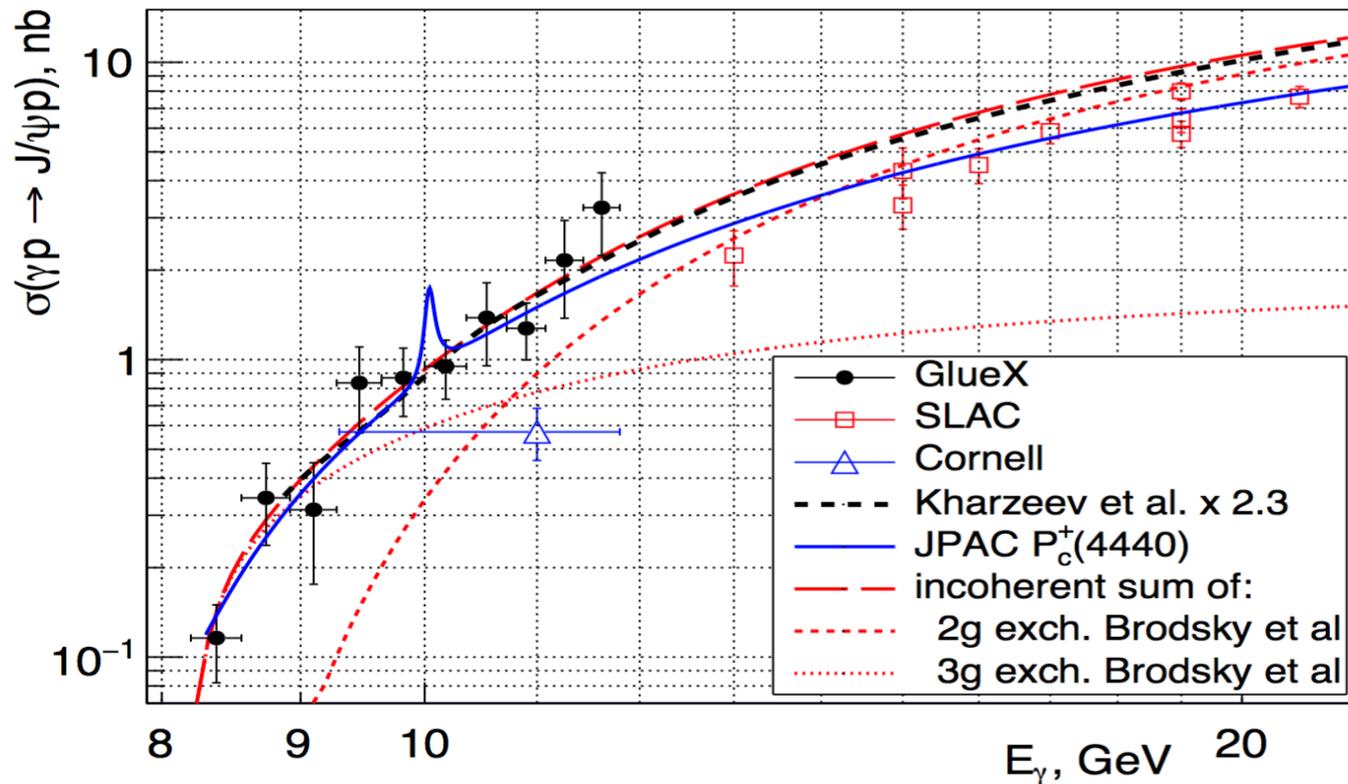
$$\int d^3 k \rho_n(k) = 1$$

# Nucleon momentum distribution in deuteron



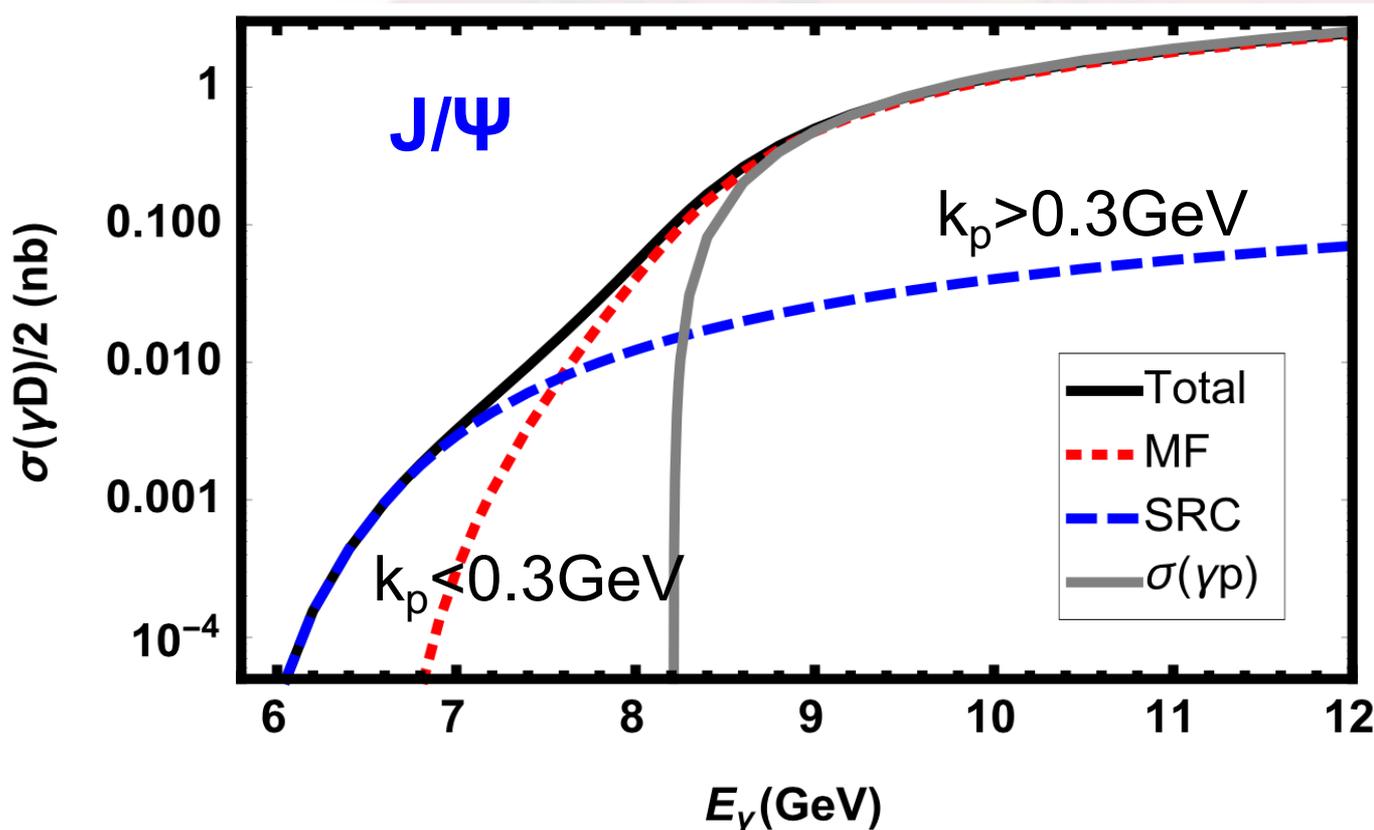
- Argonne potential: Wiringa et al., PRC 89, 024305 (2014)

# Photon-proton cross sections: Recent JLab Measurement



GlueX Coll., PRL 2019, 1905.10811

# Sub-threshold $J/\psi$ production in photon-deuteron collisions



around 7 GeV  
dominated by  
SRC

Hatta, Strikman, Xu, Yuan, 1911.11706

3/4/20

27

# Generic nucleus: spectral function

$$\sigma_{\gamma A} = A \int d^3k d\epsilon \rho_A(k, \epsilon) \tilde{\mathcal{F}}(k, \epsilon) \sigma_{\gamma p}(W_{\gamma p'})$$

- Spectral function describes nucleon momentum and energy distribution
  - Mean field: Gaussian distribution with width  $k_F/2$
  - SRC contribution has to be calculated

$$\bar{\sigma}_{\gamma A} = \frac{\sigma_{\gamma A}}{A} \equiv \int_{k < k_F} \bar{\sigma}_{MF}(k) + \int_{k > k_F} \bar{\sigma}_{SRC}(k)$$

# Spectral function from SRC

- Proton: (pn) and (pp) pair

$$\rho_A^{(SRC)p}(k, \epsilon) = C_{pn}^1 S_{pn}^1(k, \epsilon) + C_{pn}^0 S_{pn}^0(k, \epsilon) + 2C_{pp}^0 S_{pp}^0(k, \epsilon) ,$$

- Contacts:  $C_{pp}^0 = C_{nn}^0 = 1.140\%$  ,

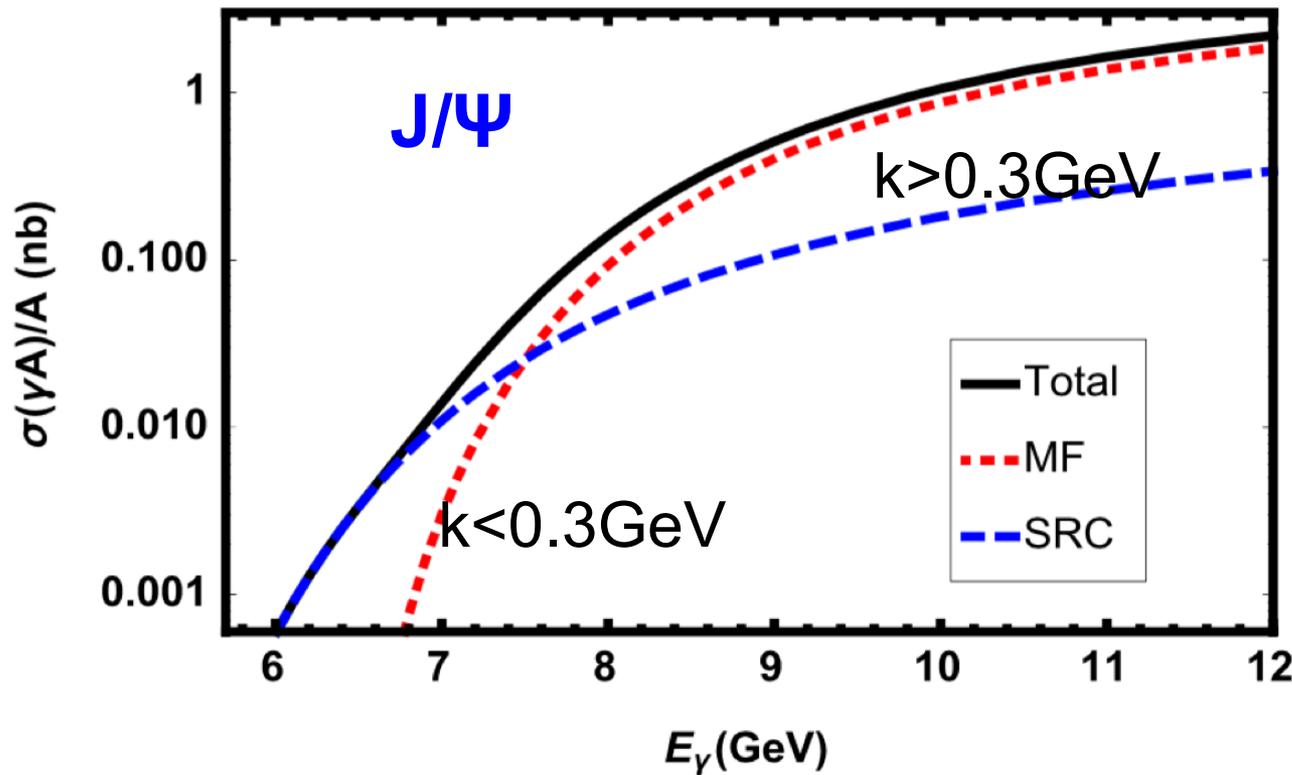
$$C_{pn}^0 = 1.244\% ,$$

$$C_{pn}^1 = 15.876\% .$$

Carbon-12

Duer et al., PRL 122, 172502 (2019)

# Sub-threshold production in photon-Carbon collisions



- 16% SRC
- 84% MF

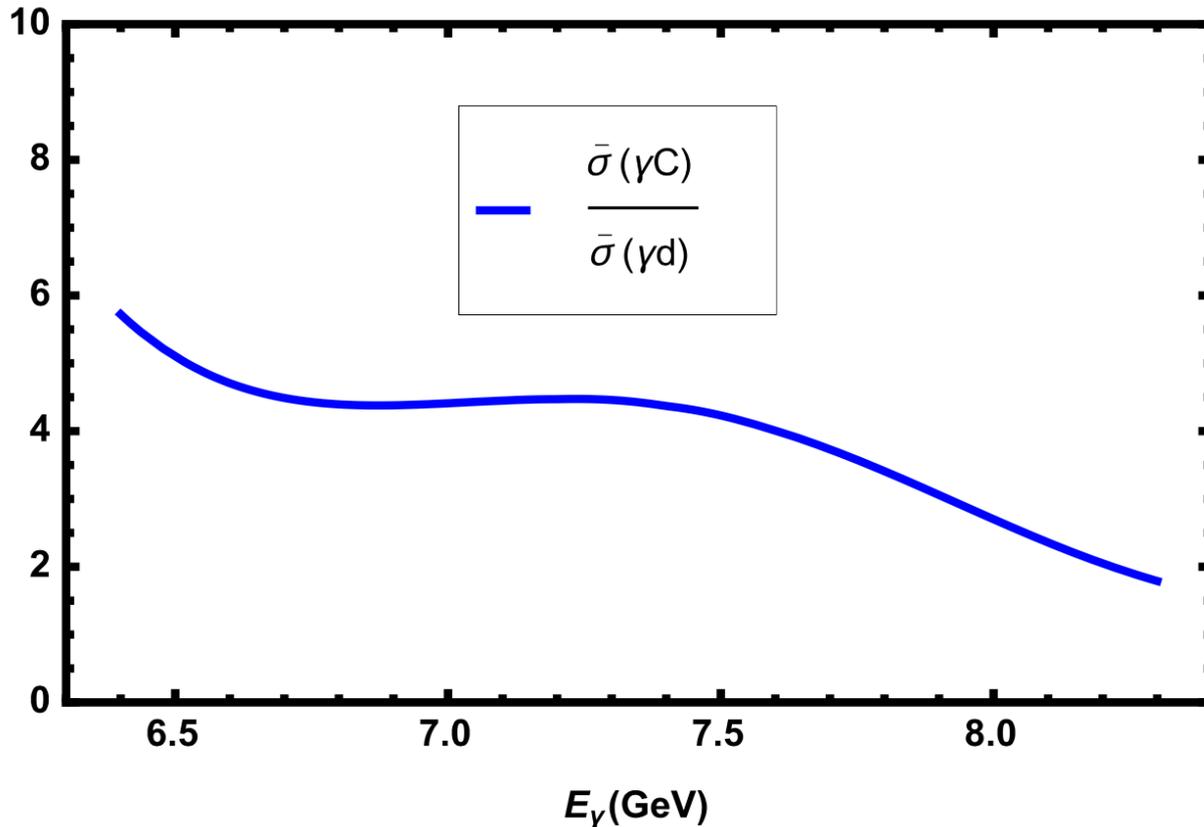
# SRC Universality

- Cross section ratios only depend on the probability of **SRC** pair

$$\frac{\tilde{\sigma}_{\gamma A \rightarrow J/\psi}}{\sigma_{\gamma d \rightarrow J/\psi}} \Big|_{E_\gamma \sim 7\text{GeV}} = \frac{n_{src}^A}{n_{src}^d} = \frac{F_2^A(x_B)}{F_2^d(x_B)} \Big|_{1.5 < x_B < 2.0}$$

- The same ratios measured from structure functions beyond  $x_B \sim 1$  at JLab

# Example: Carbon-12



- Cross section per nucleon

←  $a_2^C \approx 4.5$

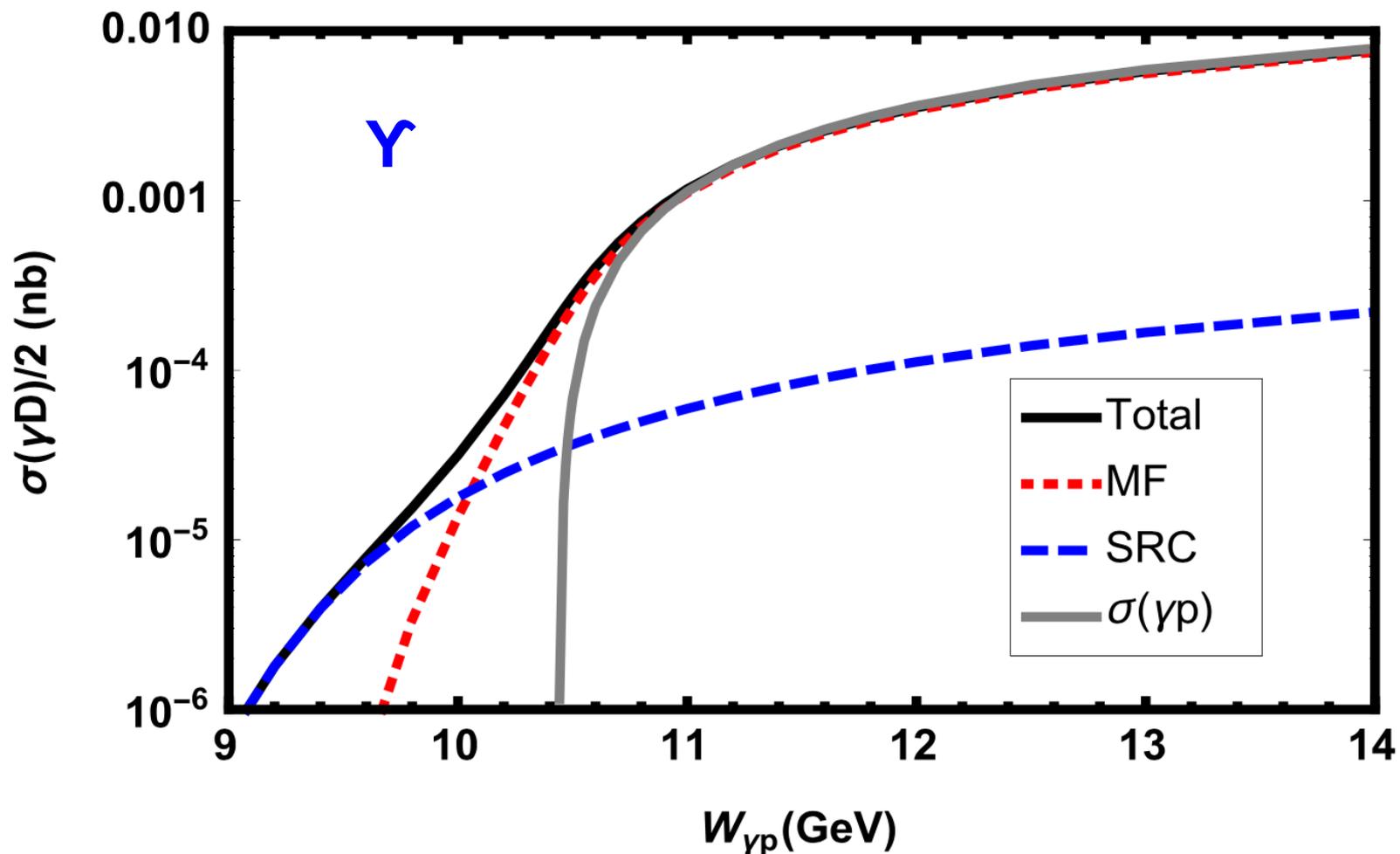
$$a_2^A = (n_{src}^A / A) / (n_{src}^d / 2)$$

# Corrections: Nuclear Absorption

$$\frac{1}{A} \int d^2\vec{b} dz \rho_A(\vec{b}, z) \exp \left( - \int_z^\infty dz' \sigma_{eff} \rho_A(\vec{b}, z') \right)$$

- Effective Abs. cross section  $\sim 4\text{mb}$
- Modification is proportional to  $A^{1/3}$ 
  - For Carbon-12, less than 10%
  - For heavy nucleus, like Pb, about 30%

# Extend to Bottomonium



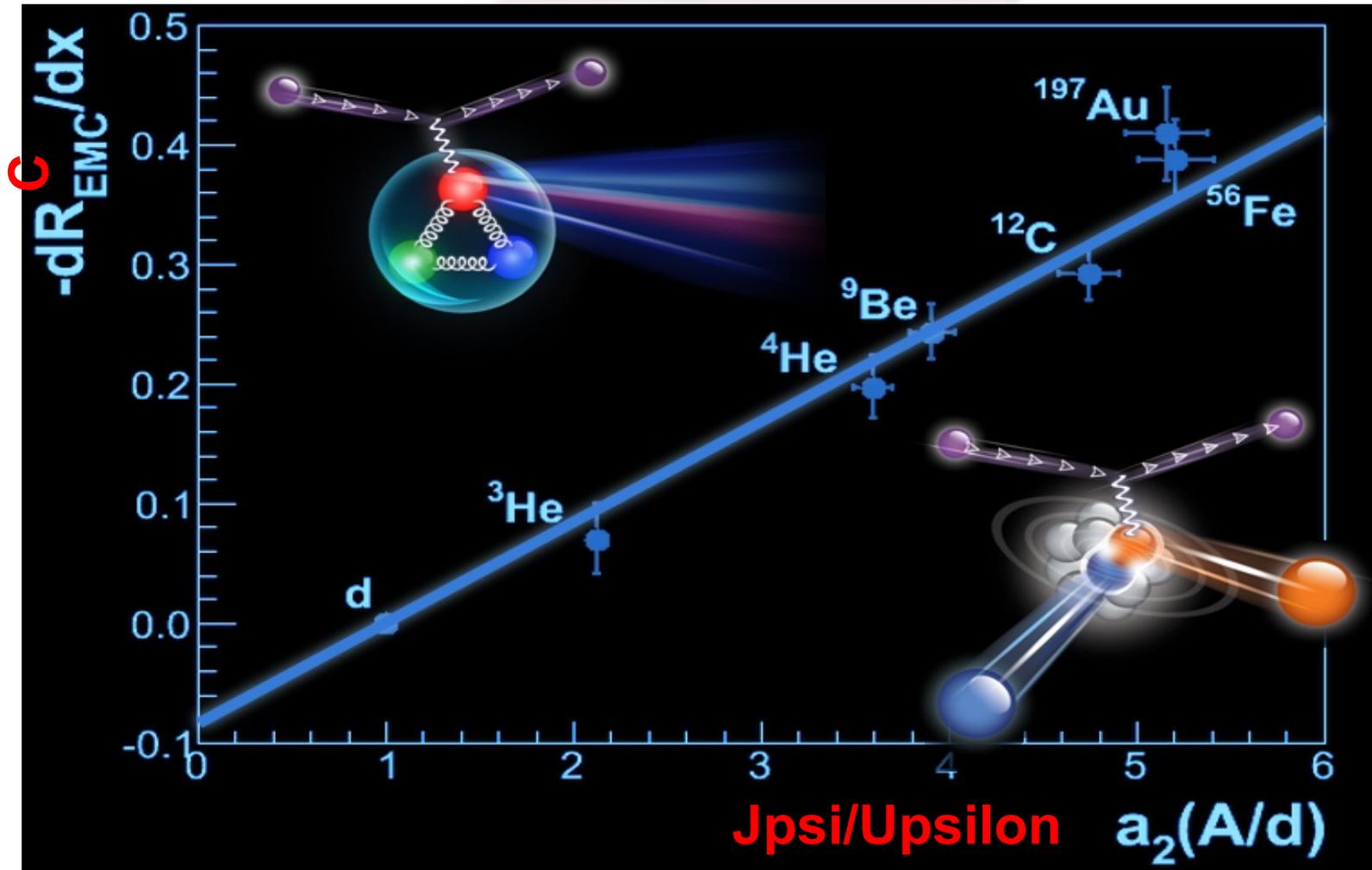
# SRC Scaling

- Sub-threshold Charm and Bottom Quarkonium production

$$\begin{aligned} \frac{\bar{\sigma}_{\gamma A \rightarrow J/\psi}}{\bar{\sigma}_{\gamma d \rightarrow J/\psi}} \Big|_{E_{\gamma} \sim 7 \text{ GeV}} &= \frac{\bar{\sigma}_{\gamma A \rightarrow \Upsilon}}{\bar{\sigma}_{\gamma d \rightarrow \Upsilon}} \Big|_{W_{\gamma p} \sim 9.7 \text{ GeV}} \\ &= \frac{n_{src}^A/A}{n_{src}^d/2} = \frac{F_2^A(x_B, Q^2)/A}{F_2^d(x_B, Q^2)/2} \Big|_{1.4 < x_B < 1.8} \end{aligned}$$

\*Cross section per nucleon

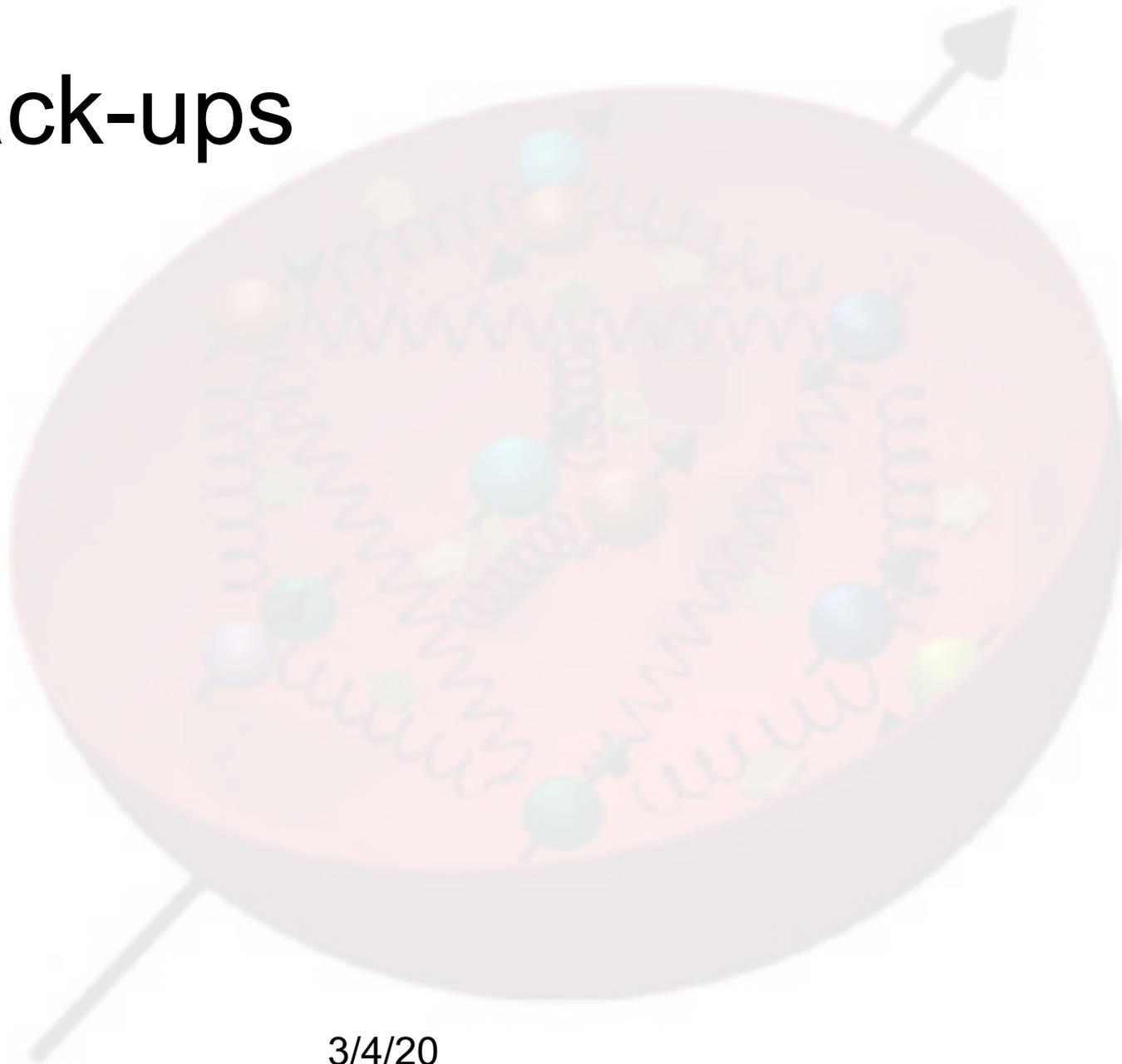
# Universality: Gluon Sector



# Summary

- Heavy flavor production in eA collisions provide the gluonic probe of the nucleon-nucleon short range correlation in nucleus
- Charmonium ( $J/\psi$ ) can be easily measured at Jlab
- Charm structure function and Upsilon can be studied at EIC in China

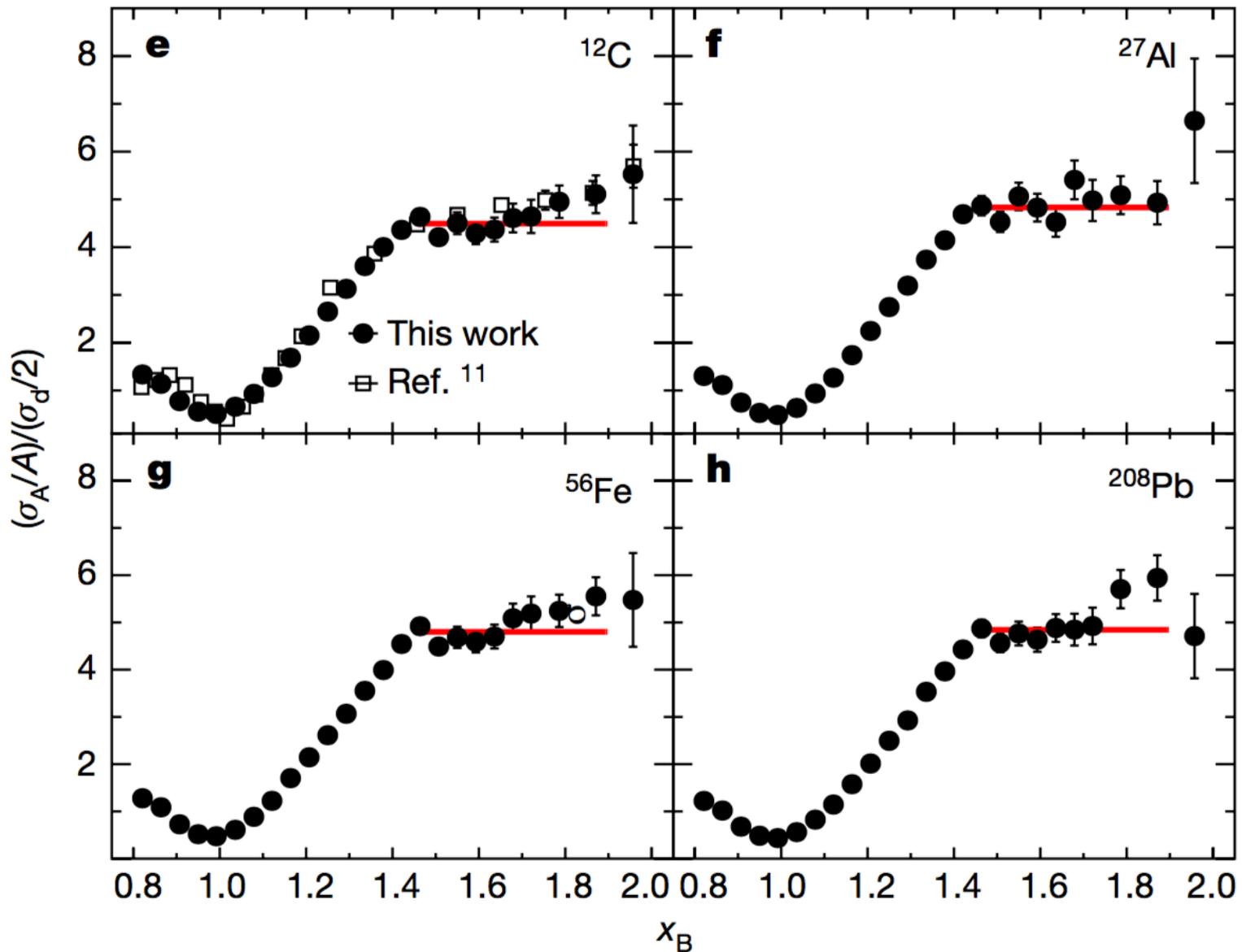
# Back-ups



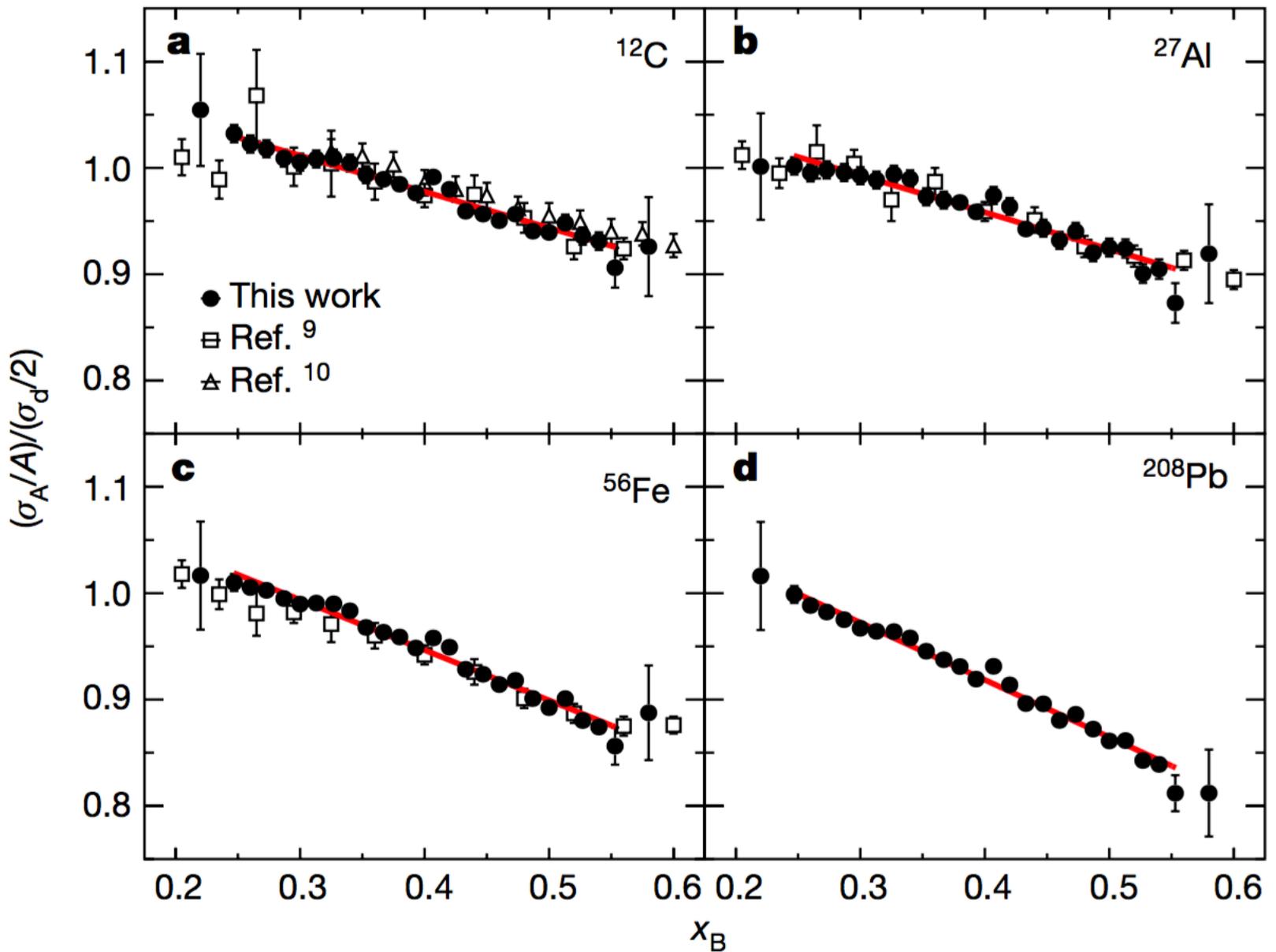
# SRC Scale Factor

Nucleus	This work		
	$a_2$	$a_2^p$	$a_2^n$
$^3\text{He}$			
$^4\text{He}$			
$^9\text{Be}$			
$^{12}\text{C}$	$4.49 \pm 0.17$	$4.49 \pm 0.17$	$4.49 \pm 0.17$
$^{27}\text{Al}$	$4.83 \pm 0.18$	$5.02 \pm 0.19$	$4.66 \pm 0.17$
$^{56}\text{Fe}$	$4.80 \pm 0.22$	$5.17 \pm 0.24$	$4.48 \pm 0.21$
$^{63}\text{Cu}$			
$^{197}\text{Au}$			
$^{208}\text{Pb}$	$4.84 \pm 0.20$	$6.14 \pm 0.25$	$3.99 \pm 0.17$

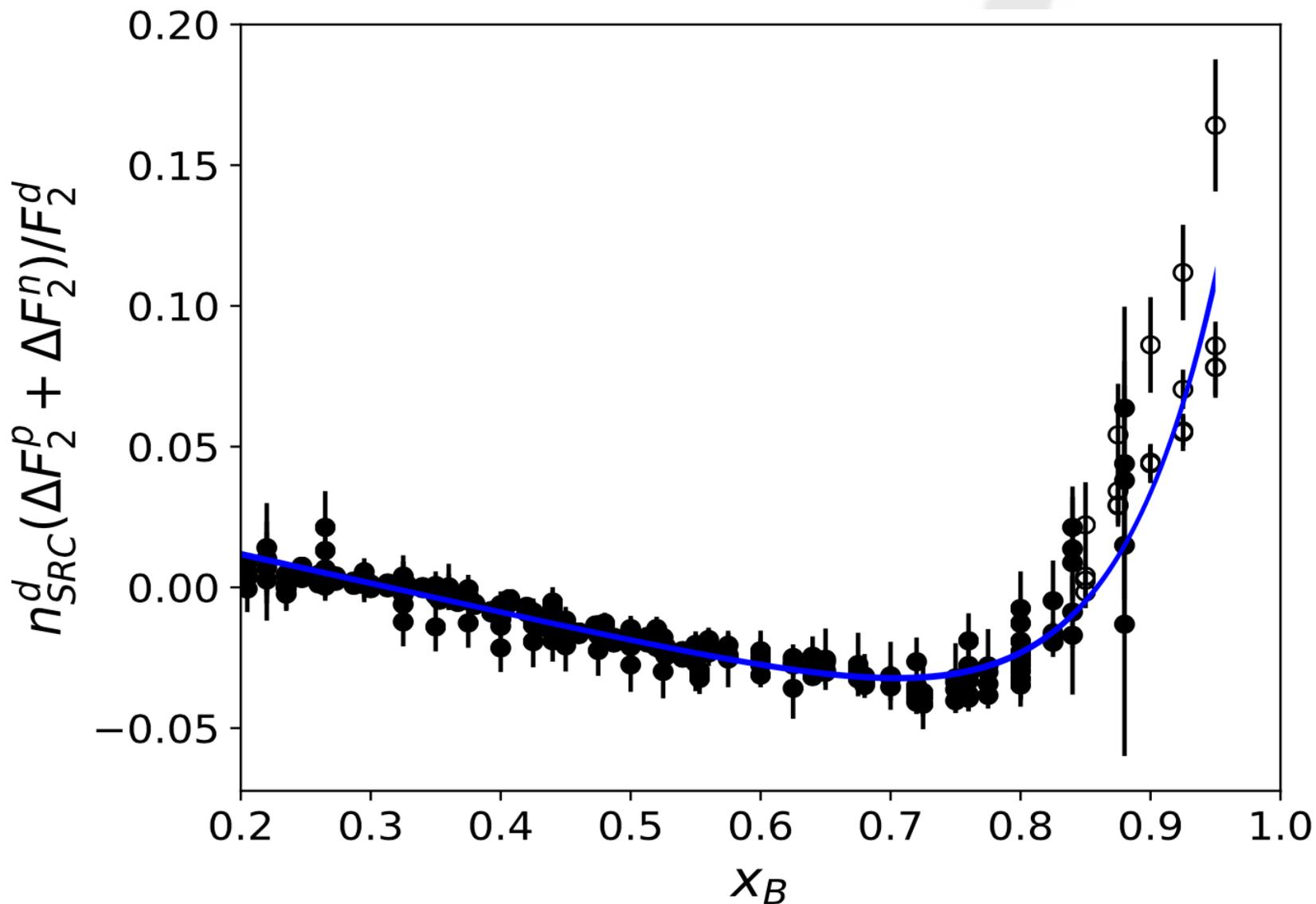
CLAS Coll., Nature 2019



CLAS Coll., Nature 2019

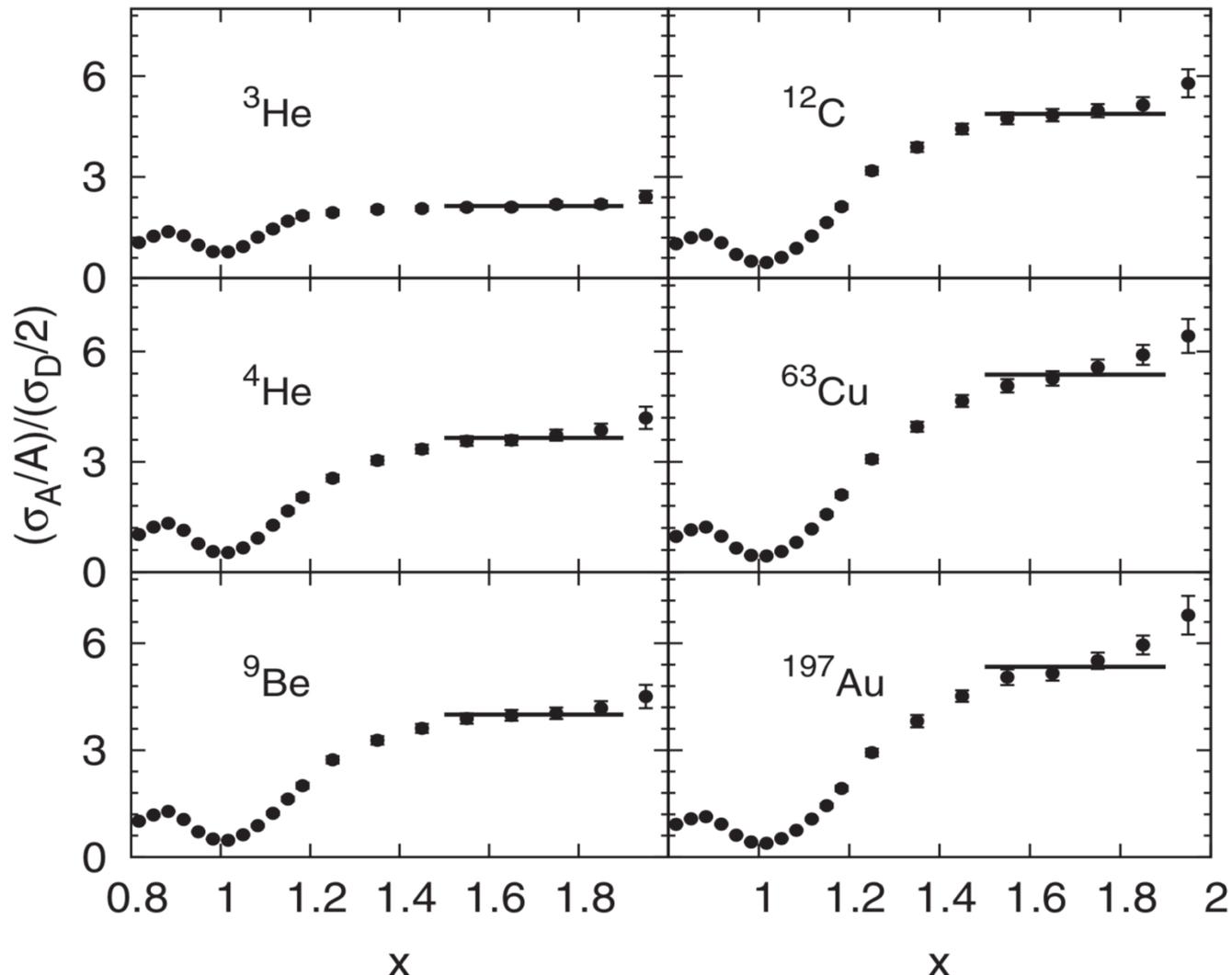


CLAS Coll., Nature 2019



Hen et al., 1908.02223: fit SRC function and  $F_p/F_n$  both

# 2012 High-Momentum Scaling

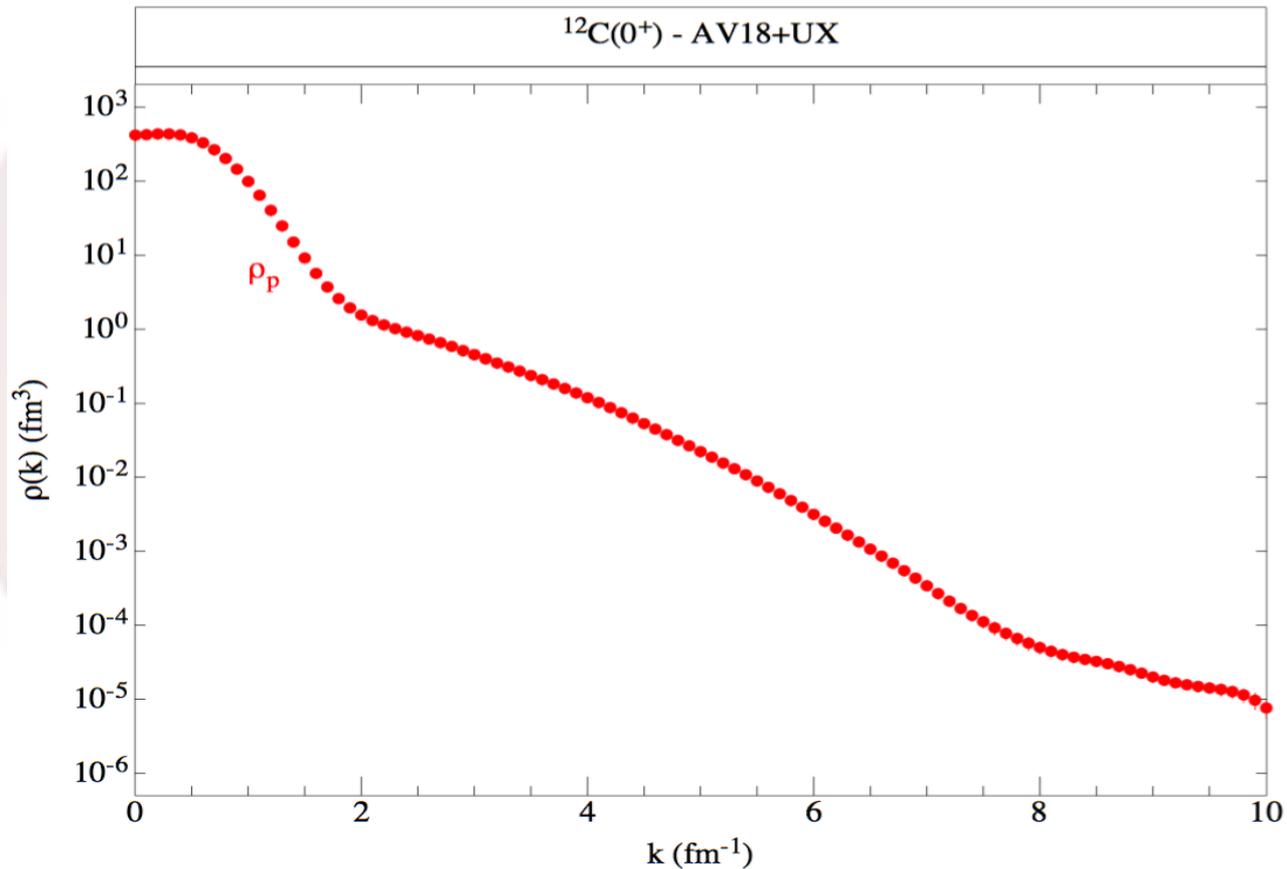


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Fomin, PRL (2012)



# Nucleon momentum distribution in Carbon

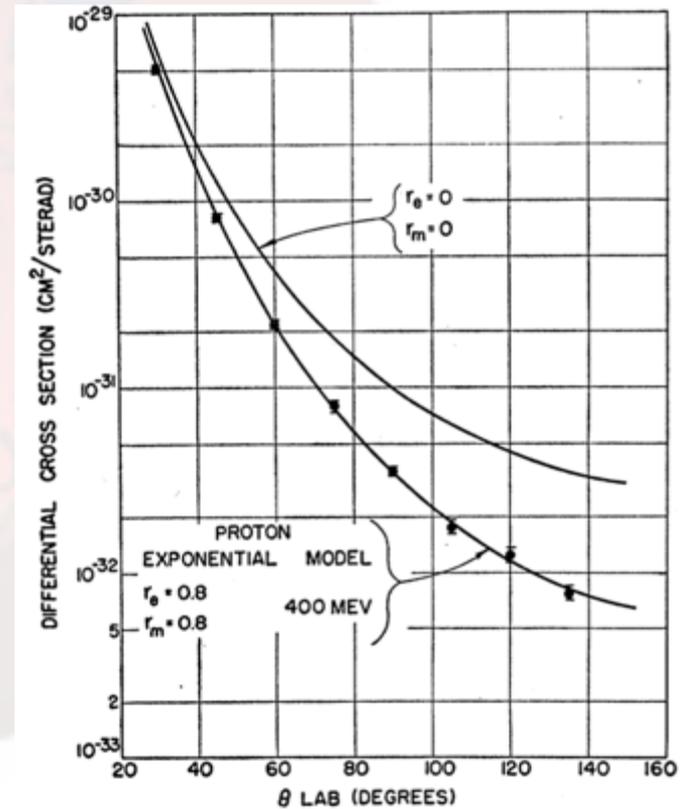
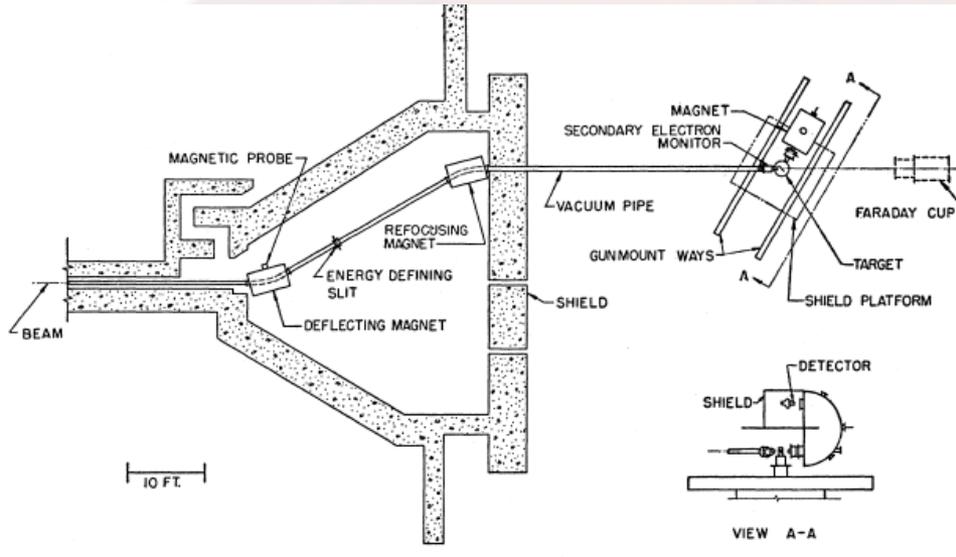


# Finite size of nucleon (charge radius)



Hofstadter

- Rutherford scattering with electron



Renewed interest on proton radius: