

Decay of  $\psi(2S) \rightarrow J/\psi \pi \pi$

$$\mathcal{A}(\Psi' \rightarrow \Psi \pi^+ \pi^-)$$

$$= -\frac{4}{F_0^2} \left\{ \left[ \frac{g}{2} (m_{\pi\pi}^2 - 2M_\pi^2) + g_1 (v \cdot p_{\pi^+}) (v \cdot p_{\pi^-}) + g_3 M_\pi^2 \right] \varepsilon_\Psi^* \cdot \varepsilon_{\Psi'} \right. \\ \left. + g_2 [p_{\pi^+}^\mu p_{\pi^-}^\nu + p_{\pi^+}^\nu p_{\pi^-}^\mu] \varepsilon_{\Psi^*}^\mu \varepsilon_{\Psi'}^\nu \right\}$$

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	$g$	$g_1$	$g_3$	$\chi^2/d.f.$
$\psi(2S) \rightarrow J/\psi \pi^+ \pi^-$	$0.30 \pm 0.01$	$-0.11 \pm 0.01$	$0^*$	$25.3/24$
	$0.38 \pm 0.03$	$-0.59 \pm 0.19$	$1.55 \pm 0.58$	$20.1/23$

- D-wave part of the dipion system and is suppressed
- Neglected in JPIPI model

$$F_{\lambda_1 \lambda_2}^J = \langle JM \lambda_1 \lambda_2 | \mathcal{M} | JM \rangle$$

- Construct amplitude in helicity formalism
- Only S-wave component between  $f_0$  and  $J/\psi$

- This part is not invariant in Lorentz transformation
- The amplitude is calculated in  $\psi(2S)$  rest frame

Only S-wave

$$\mathcal{A} = \sum_{\lambda_{Z_c}} \sum_{\lambda_R} \sum_{\lambda_{\psi'}} \sum_{\lambda_{J/\psi}} A_{(Y \rightarrow \psi' \pi^+ \pi^-)} \cdot \left( C \cdot F_{\lambda_R, \lambda_{J/\psi}}^{J_{\psi'}} D_{\lambda_{\psi'}, -\lambda_{J/\psi}}^{*J_{\psi'}} \cdot F_{\lambda_{l^+}, \lambda_{l^-}}^{J_{J/\psi}} D_{\lambda_{J/\psi}, \Delta_{\lambda_l}}^{*J_{J/\psi}} \right)$$

$$C = \left[ \frac{g}{2} (m_{\pi\pi}^2 - 2M_\pi^2) + g_1 (v \cdot p_{\pi^+}) (v \cdot p_{\pi^-}) + g_3 M_\pi^2 \right]$$

Decay sequence  $Y \rightarrow \psi(2S)\pi^+\pi^-$

$$A = \phi_\mu(m_1)\omega_\nu^*(m_2)A^{\mu\nu} = \phi_\mu(m_1)\omega_\nu^*(m_2) \sum_i \Lambda_i U_i^{\mu\nu}$$

Decay of  $\psi(2S) \rightarrow J/\psi\pi\pi$

$$\begin{aligned} \mathcal{A}(\Psi' \rightarrow \Psi\pi^+\pi^-) \\ = -\frac{4}{F_0^2} \left\{ \left[ \frac{g}{2} (m_{\pi\pi}^2 - 2M_\pi^2) + g_1 (v \cdot p_{\pi^+}) (v \cdot p_{\pi^-}) + g_3 M_\pi^2 \right] \varepsilon_\Psi^* \cdot \varepsilon_{\Psi'} \right. \\ \left. + g_2 [p_{\pi^+\mu} p_{\pi^- \nu} + p_{\pi^+ \nu} p_{\pi^- \mu}] \varepsilon_{\Psi^*}^\mu \varepsilon_{\Psi'}^\nu \right\} \end{aligned}$$

Decay of  $J/\psi \rightarrow l^+l^-$

$$A = i e \omega_\beta(m_2) \bar{u}_{e^-} \gamma^\beta \nu_{e^+} \frac{e m_\psi}{f_\psi}$$

$$\mathcal{A} = \phi_\mu A^{\mu\nu} \omega_\nu^* (C \omega_\alpha \varepsilon^\alpha) \varepsilon^\beta \bar{u}_{e^-} \gamma_{\beta} \nu_{e^+}$$

$$C = \left[ \frac{g}{2} (m_{\pi\pi}^2 - 2M_\pi^2) + g_1 (v \cdot p_{\pi^+}) (v \cdot p_{\pi^-}) + g_3 M_\pi^2 \right]$$



$$\frac{d\sigma}{d\Phi_n} = 2 \sum_{i,j} \Lambda_i \Lambda_j^* \sum_{\mu=1}^2 U_i^{\mu\nu} M_{\nu\nu'} U_j^{*\mu\nu'}$$

$$\begin{aligned} M_{\nu\nu'} = C C^* \tilde{g}_{\nu\alpha}(p(\psi')) \tilde{g}_{\nu'\alpha'}(p(\psi')) \tilde{g}^{\alpha\beta}(p(J/\psi)) \tilde{g}^{\alpha'\beta'}(p(J/\psi)) \\ \cdot [p_\beta p'_{\beta'} + p'_{\beta} p_{\beta'} - g_{\beta\beta'} (p \cdot p' + p_l^2)] \end{aligned}$$

