

BESIII粲强子物理研讨会



# A Data-driven Approach to Charmed Baryon Weak Decays

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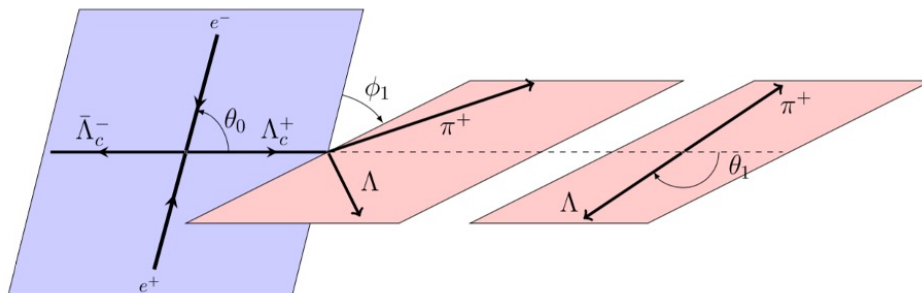
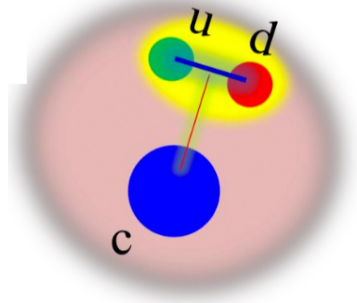
April 8, 2023 @ UCST, Hefei

# Outline

- Introduction
- Global fits based on  $SU(3)$
- Global fits based on topological diagrams
- Summary

Huiling Zhong, FX, Qiaoyi Wen, Yu Gu, JHEP 02 (2023) 235,  
& work to appear

# Introduction



CF

Channel	Channel
$\Lambda_c^+ \rightarrow \Lambda^0 \pi^+$	$\Xi_c^0 \rightarrow \Xi^0 \pi^0$
$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$	$\Xi_c^0 \rightarrow \Xi^0 \eta$
$\Lambda_c^+ \rightarrow p \bar{K}^0$	$\Xi_c^0 \rightarrow \Xi^0 \eta'$
$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$	$\Xi_c^0 \rightarrow \Xi^- \pi^+$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	$\Omega_c^0 \rightarrow \Xi^0 \bar{K}^0$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	
$\Lambda_c^+ \rightarrow \Lambda^0 K^+$	$\Xi_c^0 \rightarrow \Xi^0 K^0$
$\Lambda_c^+ \rightarrow p \pi^0$	$\Xi_c^0 \rightarrow \Sigma^+ \pi^-$
$\Lambda_c^+ \rightarrow p \eta$	$\Xi_c^0 \rightarrow \Sigma^- \pi^+$
$\Lambda_c^+ \rightarrow p \eta'$	$\Xi_c^0 \rightarrow \Xi^- K^+$
$\Lambda_c^+ \rightarrow n \pi^+$	$\Omega_c^0 \rightarrow \Sigma^0 \bar{K}^0$
$\Lambda_c^+ \rightarrow \Sigma^0 K^+$	$\Omega_c^0 \rightarrow \Sigma^+ K^-$
$\Lambda_c^+ \rightarrow \Sigma^+ K^0$	$\Omega_c^0 \rightarrow \Lambda^0 \bar{K}^0$
$\Xi_c^+ \rightarrow \Lambda^0 \pi^+$	$\Omega_c^0 \rightarrow \Xi^0 \pi^0$
$\Xi_c^+ \rightarrow p \bar{K}^0$	$\Omega_c^0 \rightarrow \Xi^- \pi^+$
$\Xi_c^+ \rightarrow \Sigma^0 \pi^+$	
$\Xi_c^+ \rightarrow \Sigma^+ \pi^0$	
$\Lambda_c^+ \rightarrow p K^0$	$\Omega_c^0 \rightarrow \Xi^0 K^0$
$\Lambda_c^+ \rightarrow n K^+$	$\Omega_c^0 \rightarrow \Lambda^0 \eta$
$\Xi_c^+ \rightarrow \Lambda^0 K^+$	$\Omega_c^0 \rightarrow \Sigma^0 \eta'$
$\Xi_c^+ \rightarrow p \pi^0$	$\Omega_c^0 \rightarrow \Lambda^0 \pi^0$
$\Xi_c^+ \rightarrow p \eta$	$\Omega_c^0 \rightarrow \Sigma^0 \pi^0$
$\Xi_c^+ \rightarrow p \eta'$	$\Omega_c^0 \rightarrow \Sigma^+ \pi^-$
$\Xi_c^+ \rightarrow n \pi^+$	$\Omega_c^0 \rightarrow \Sigma^- \pi^+$
$\Xi_c^+ \rightarrow \Sigma^0 K^+$	$\Omega_c^0 \rightarrow \Xi^- K^+$

SCS

DCS

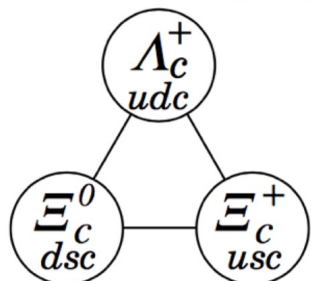
## Branching Fractions



## Decay Asymmetries (longitudinal, transverse)

$$2286.46 \pm 0.14 \text{ MeV}$$

$$(2.00 \pm 0.06) \times 10^{-13} \text{ s (S = 1.6)}$$



$$2470.87^{+0.28}_{-0.31} \text{ MeV}$$

$$(1.12^{+0.13}_{-0.10}) \times 10^{-13} \text{ s}$$

$$2467.87 \pm 0.30 \text{ MeV (S = 1.1)}$$

$$(4.42 \pm 0.26) \times 10^{-13} \text{ s (S = 1.3)}$$

# Experimental progress since 2022

## • BESIII

$$\mathcal{B}(\Lambda_c^+ \rightarrow n\pi^+) = (6.6 \pm 1.2 \pm 0.4) \times 10^{-4},$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow p\eta') = (5.62_{-2.04}^{+2.46} \pm 0.26) \times 10^{-4},$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda^0 K^+) = (6.21 \pm 0.44 \pm 0.26 \pm 0.34) \times 10^{-4},$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ K_S^0) = (4.8 \pm 1.4 \pm 0.2 \pm 0.3) \times 10^{-4},$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 K^+) = (4.7 \pm 0.9 \pm 0.1 \pm 0.3) \times 10^{-4}.$$

## • Belle

$$\mathcal{B}(\Lambda_c^+ \rightarrow p\eta') = (4.73 \pm 0.82 \pm 0.47 \pm 0.24) \times 10^{-4},$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda^0 K^+) = (6.57 \pm 0.17 \pm 0.11 \pm 0.35) \times 10^{-4},$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 K^+) = (3.58 \pm 0.19 \pm 0.06 \pm 0.19) \times 10^{-4},$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta) = (3.14 \pm 0.35 \pm 0.11 \pm 0.25) \times 10^{-3},$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta') = (4.16 \pm 0.75 \pm 0.21 \pm 0.33) \times 10^{-3},$$

$$\alpha(\Lambda_c^+ \rightarrow \Lambda^0 K^+) = -0.585 \pm 0.049 \pm 0.018,$$

$$\alpha(\Lambda_c^+ \rightarrow \Sigma^0 K^+) = -0.55 \pm 0.18 \pm 0.09,$$

$$\alpha(\Lambda_c^+ \rightarrow \Sigma^+ \eta) = -0.99 \pm 0.03 \pm 0.05,$$

$$\alpha(\Lambda_c^+ \rightarrow \Sigma^+ \eta') = -0.46 \pm 0.06 \pm 0.03.$$

CF

Channel	Channel
$\Lambda_c^+ \rightarrow \Lambda^0 \pi^+$	$\Xi_c^0 \rightarrow \Xi^0 \pi^0$
$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$	$\Xi_c^0 \rightarrow \Xi^0 \eta$
$\Lambda_c^+ \rightarrow p \bar{K}^0$	$\Xi_c^0 \rightarrow \Xi^0 \eta'$
$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$	$\Xi_c^0 \rightarrow \Xi^- \pi^+$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	$\Omega_c^0 \rightarrow \Xi^0 \bar{K}^0$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	
$\Lambda_c^+ \rightarrow \Lambda^0 K^+$	$\Xi_c^0 \rightarrow \Xi^0 K^0$
$\Lambda_c^+ \rightarrow p \pi^0$	$\Xi_c^0 \rightarrow \Sigma^+ \pi^-$
$\Lambda_c^+ \rightarrow p \eta$	$\Xi_c^0 \rightarrow \Sigma^- \pi^+$
$\Lambda_c^+ \rightarrow p \eta'$	$\Xi_c^0 \rightarrow \Xi^- K^+$
$\Lambda_c^+ \rightarrow n \pi^+$	$\Omega_c^0 \rightarrow \Sigma^0 \bar{K}^0$
$\Lambda_c^+ \rightarrow \Sigma^0 K^+$	$\Omega_c^0 \rightarrow \Sigma^+ K^-$
$\Lambda_c^+ \rightarrow \Sigma^+ K^0$	$\Omega_c^0 \rightarrow \Lambda^0 \bar{K}^0$
$\Xi_c^+ \rightarrow \Lambda^0 \pi^+$	$\Omega_c^0 \rightarrow \Xi^0 \pi^0$
$\Xi_c^+ \rightarrow p \bar{K}^0$	$\Omega_c^0 \rightarrow \Xi^- \pi^+$
$\Xi_c^+ \rightarrow \Sigma^0 \pi^+$	
$\Xi_c^+ \rightarrow \Sigma^+ \pi^0$	
$\Lambda_c^+ \rightarrow p K^0$	$\Omega_c^0 \rightarrow \Xi^0 K^0$
$\Lambda_c^+ \rightarrow n K^+$	$\Omega_c^0 \rightarrow \Lambda^0 \eta$
$\Xi_c^+ \rightarrow \Lambda^0 K^+$	$\Omega_c^0 \rightarrow \Sigma^0 \eta'$
$\Xi_c^+ \rightarrow p \pi^0$	$\Omega_c^0 \rightarrow \Lambda^0 \pi^0$
$\Xi_c^+ \rightarrow p \eta$	$\Omega_c^0 \rightarrow \Sigma^0 \pi^0$
$\Xi_c^+ \rightarrow p \eta'$	$\Omega_c^0 \rightarrow \Sigma^+ \pi^-$
$\Xi_c^+ \rightarrow n \pi^+$	$\Omega_c^0 \rightarrow \Sigma^- \pi^+$
$\Xi_c^+ \rightarrow \Sigma^0 K^+$	$\Omega_c^0 \rightarrow \Xi^- K^+$

SCS

DCS

# Experimental results as inputs

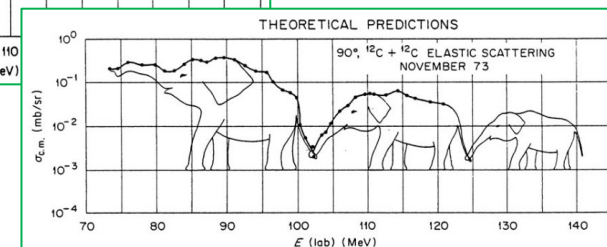
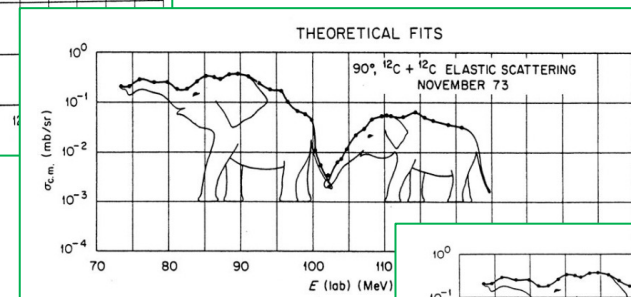
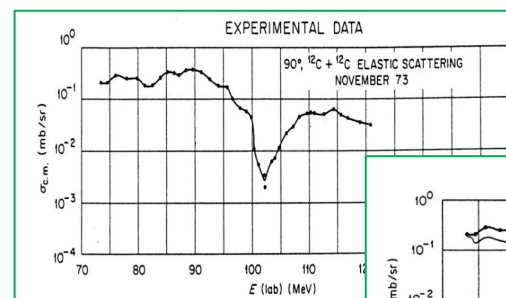
## 20 Branching ratios

Obs.	PDG	BESIII	Belle	Ave.
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda^0 \pi^+)$	$1.30 \pm 0.07$	$1.24 \pm 0.08^* [3]$		$1.30 \pm 0.07$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+)$	$1.29 \pm 0.07$	$1.27 \pm 0.09^* [3]$		$1.29 \pm 0.07$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow p K_S)$	$1.59 \pm 0.08$	$1.52 \pm 0.09^* [3]$		$1.59 \pm 0.08$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)$	$1.25 \pm 0.10$	$1.18 \pm 0.10^* [3]$		$1.25 \pm 0.10$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta)$	$0.44 \pm 0.20 [2, 4]$	$0.41 \pm 0.20^* [4]$	$0.314 \pm 0.044 [5]$	$0.32 \pm 0.04$
$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta)}{\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)}$		$0.35 \pm 0.16 [4]$		
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta')$	$1.5 \pm 0.6 [2, 4]$	$1.34 \pm 0.56^* [4]$	$0.416 \pm 0.085 [5]$	$0.44 \pm 0.15^1$
$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta')}{\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \omega)}$		$0.86 \pm 0.34 [4]$		
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Xi^0 K^+)$	$0.55 \pm 0.07 [2, 6]$	$0.590 \pm 0.094^* [6]$		$0.55 \pm 0.07$
$10^3 \mathcal{B}(\Lambda_c^+ \rightarrow p \eta)$	(Belle's data)	$1.24 \pm 0.30 [7]$	$1.42 \pm 0.12 [8]$	$1.40 \pm 0.11$
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \eta')$		$5.62^{+2.46}_{-2.04} \pm 0.26 [9]$	$4.73 \pm 0.97 [10]$	$4.85 \pm 0.90$
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda^0 K^+)$	$6.1 \pm 1.2 [11, 12]$	$6.21 \pm 0.61 [13]$	$6.57 \pm 0.40 [14]$	$6.44 \pm 0.32$
$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda^0 K^+)}{\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda^0 \pi^+)}$			$0.074 \pm 0.016 [12]$	
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 K^+)$	$5.2 \pm 0.8 [11, 12]$	$4.7 \pm 0.95 [15]$	$3.58 \pm 0.28 [14]$	$3.82 \pm 0.38^2$
$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 K^+)}{\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+)}$			$0.056 \pm 0.016 [12]$	
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow n \pi^+)$		$6.6 \pm 1.3 [16]$		$6.6 \pm 1.3$
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ K_S)$		$4.8 \pm 1.4 [15]$		$4.8 \pm 1.4$
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \pi^0)$	(Belle's data)	$< 2.7 [7]$	$< 0.80 [8]$	$< 0.77$
$10^2 \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)$	$1.43 \pm 0.32 [2, 17]$		$1.80 \pm 0.52^* [17]$	$1.43 \pm 0.32$
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- K^+)$	$0.39 \pm 0.12 [2, 18]$			$0.39 \pm 0.12$
$\frac{10^2 \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- K^+)}{\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)}$			$2.75 \pm 0.57 [18]$	
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Lambda^0 K_S)$	$3.2 \pm 0.7 [2, 19, 20]$			$3.2 \pm 0.7$
$\frac{\mathcal{B}(\Xi_c^0 \rightarrow \Lambda^0 K_S)}{\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)}$			$0.21 \pm 0.03 [20]$	
			$0.229 \pm 0.014 [19]$	
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Sigma^0 K_S)$	(Belle's data)		$0.54 \pm 0.16 [19]$	$0.54 \pm 0.16$
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Sigma^+ K^-)$	(Belle's data)		$1.8 \pm 0.4 [19]$	$1.8 \pm 0.4$
$10^2 \mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 \pi^+)$	$1.6 \pm 0.8 [17, 21]$			$1.6 \pm 0.8$
$\frac{\mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 \pi^+)}{\mathcal{B}(\Xi_c^+ \rightarrow \Xi^- 2\pi^+)}$	$0.55 \pm 0.16 [21]$			

## 9 decay asymmetries

$\alpha(\Lambda_c^+ \rightarrow \Lambda^0 \pi^+)$	$-0.84 \pm 0.09 [22-26]$	$-0.80 \pm 0.11^* [22]$	$-0.755 \pm 0.006 [14]$	$-0.76 \pm 0.01$
$\alpha(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+)$	(BESIII's data)	$-0.73 \pm 0.18 [22]$	$-0.463 \pm 0.018 [14]$	$-0.47 \pm 0.03^3$
$\alpha(\Lambda_c^+ \rightarrow p K_S)$	(BESIII's data)	$0.18 \pm 0.45 [22]$		$0.18 \pm 0.45$
$\alpha(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)$	$-0.55 \pm 0.11 [22, 23]$	$-0.57 \pm 0.12^* [22]$	$-0.48 \pm 0.03 [5]$	$-0.49 \pm 0.03$
$\alpha(\Xi_c^0 \rightarrow \Xi^- \pi^+)$	(Belle's data)		$-0.64 \pm 0.05 [27]$	$-0.64 \pm 0.05$
$\alpha(\Lambda_c^+ \rightarrow \Sigma^+ \eta)$			$-0.99 \pm 0.06 [5]$	$-0.99 \pm 0.06$
$\alpha(\Lambda_c^+ \rightarrow \Sigma^+ \eta')$			$-0.46 \pm 0.07 [5]$	$-0.46 \pm 0.07$
$\alpha(\Lambda_c^+ \rightarrow \Lambda^0 K^+)$			$-0.585 \pm 0.052 [14]$	$-0.585 \pm 0.052$
$\alpha(\Lambda_c^+ \rightarrow \Sigma^0 K^+)$			$-0.55 \pm 0.20 [14]$	$-0.55 \pm 0.20$

## time to interpret data



# Fits within $SU(3)$ frame

- w/ or w/o Flavor symmetry
- w/ or w/o mixing effect



# Flavor symmetry keeping

$$\mathcal{M} = \langle M \mathbf{B}_n | \mathcal{H}_{\text{eff}} | \mathbf{B}_c \rangle = i \bar{u}_f (A - B \gamma_5) u_i.$$

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_{q_1 c}^* V_{u q_2} (c_+ \mathcal{O}_+ + c_- \mathcal{O}_-) + h.c. \\ (6, \bar{15})$$

$$\Gamma = \frac{p_c}{8\pi} \left( \frac{(m_i + m_f)^2 - m_P^2}{m_i^2} |A|^2 + \frac{(m_i - m_f)^2 - m_P^2}{m_i^2} |B|^2 \right) \\ \alpha = \frac{2\kappa \text{Re}(A^* B)}{|A|^2 + \kappa^2 |B|^2}$$

$$A_0 = a_0 H(6)_{ij} (\mathbf{B}'_c)^{ik} (\mathbf{B}_n)_k^j (M)_\ell^l + a_1 H(6)_{ij} (\mathbf{B}'_c)^{ik} (\mathbf{B}_n)_k^\ell (M)_\ell^j + a_2 H(6)_{ij} (\mathbf{B}'_c)^{ik} (M)_k^\ell (\mathbf{B}_n)_\ell^j \\ + a_3 H(6)_{ij} (\mathbf{B}_n)_k^i (M)_\ell^j (\mathbf{B}'_c)^{k\ell} + a'_0 (\mathbf{B}_n)_j^i (M)_\ell^l H(\bar{15})_i^{jk} (\mathbf{B}_c)_k \\ + a_4 H(\bar{15})_k^{\ell i} (\mathbf{B}_c)_j (M)_i^j (\mathbf{B}_n)_\ell^k + a_5 (\mathbf{B}_n)_j^i (M)_i^\ell H(\bar{15})_\ell^{jk} (\mathbf{B}_c)_k \\ + a_6 (\mathbf{B}_n)_i^j (M)_\ell^m H(\bar{15})_m^{\ell i} (\mathbf{B}_c)_j + a_7 (\mathbf{B}_n)_i^\ell (M)_j^i H(\bar{15})_\ell^{jk} (\mathbf{B}_c)_k$$

$$B_0 = A_0 \Big|_{a_i \rightarrow b_i},$$

M.J. Savage and R.P. Springer, *SU(3) Predictions for Charmed Baryon Decays*, *Phys. Rev. D* **42** (1990) 1527 [INSPIRE].

C.Q. Geng, C.-W. Liu and T.-H. Tsai, *Asymmetries of anti-triplet charmed baryon decays*, *Phys. Lett. B* **794** (2019) 19 [arXiv:1902.06189] [INSPIRE].

$$\mathcal{M} = a_{15} (T_{c\bar{3}})_i (H_{\bar{15}})_j^{\{ik\}} (\bar{T}_8)_k^j P_l^l + b_{15} (T_{c\bar{3}})_i (H_{\bar{15}})_j^{\{ik\}} (\bar{T}_8)_k^l P_l^j \\ + c_{15} (T_{c\bar{3}})_i (H_{\bar{15}})_j^{\{ik\}} (\bar{T}_8)_l^j P_k^l + d_{15} (T_{c\bar{3}})_i (H_{\bar{15}})_l^{\{jk\}} (\bar{T}_8)_j^l P_k^i \\ + e_{15} (T_{c\bar{3}})_i (H_{\bar{15}})_l^{\{jk\}} (\bar{T}_8)_j^i P_k^l + a_6 (T_{c\bar{3}})^{[ik]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_k^j P_l^l \\ + b_6 (T_{c\bar{3}})^{[ik]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_k^l P_l^j + c_6 (T_{c\bar{3}})^{[ik]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_l^j P_k^l \\ + d_6 (T_{c\bar{3}})^{[kl]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_k^i P_l^j.$$

F. Huang, Z.-P. Xing and X.-G. He, *A global analysis of charmless two body hadronic decays for anti-triplet charmed baryons*, *JHEP* **03** (2022) 143 [arXiv:2112.10556] [INSPIRE].

$$\mathbf{B}_c = (\Xi_c^0, -\Xi_c^+, \Lambda_c^+), \\ \mathbf{B}_n = \begin{pmatrix} \frac{1}{\sqrt{6}}\Lambda^0 + \frac{1}{\sqrt{2}}\Sigma^0 & \Sigma^+ & p \\ \Sigma^- & \frac{1}{\sqrt{6}}\Lambda^0 - \frac{1}{\sqrt{2}}\Sigma^0 & n \\ \Xi^- & \Xi^0 & -\sqrt{\frac{2}{3}}\Lambda^0 \end{pmatrix}, \\ \mathbf{M} = \begin{pmatrix} \frac{1}{\sqrt{2}}(\pi^0 + c_\phi\eta + s_\phi\eta') & \pi^+ & K^+ \\ \pi^- & \frac{1}{\sqrt{2}}(-\pi^0 + c_\phi\eta + s_\phi\eta') & K^0 \\ K^- & \bar{K}^0 & -s_\phi\eta + c_\phi\eta' \end{pmatrix}$$

$$H(\bar{15})_k^{ij} = \left( \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & s_c & 1 \\ s_c & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & -s_c^2 & -s_c \\ -s_c^2 & 0 & 0 \\ -s_c & 0 & 0 \end{pmatrix} \right)$$

$$H(6)_{ij} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 2 & -2s_c \\ 0 & -2s_c & 2s_c^2 \end{pmatrix}$$



# Flavor symmetry breaking

$$\gamma = \frac{m_s}{3\Lambda} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + \frac{m_s}{3\Lambda} \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 2 \end{pmatrix}$$

(6,  $\overline{15}$ )

$$8 \otimes \overline{15} = \overline{42} \oplus 24^{(1)} \oplus \overline{15}^{(1)} \oplus \overline{15}^{(2)} \oplus \overline{15}^{(3)} \oplus 6^{(1)} \oplus \boxed{\overline{3}^{(1)}}$$

$$8 \otimes 6 = 24^{(2)} \oplus \overline{15}^{(4)} \oplus 6^{(2)} \oplus \boxed{\overline{3}^{(2)}}$$

$$\Delta \mathcal{L}_{QCD} = -m_s \bar{\psi} \lambda^8 \psi$$

$$\begin{aligned} \mathcal{H} = (\bar{3} + 6 + \overline{15}) \times (1 + \epsilon 8 + \mathcal{O}(\epsilon^2)) \supset \bar{3} + 6 + \overline{15} \\ + \epsilon (\bar{3}_i + 6_i + \overline{15}_1 + \overline{15}_2 + \overline{15}_3^1 + \overline{15}_3^2 \\ + \overline{24}_3 + \overline{42}_3 + \dots), \end{aligned}$$

M.J. Savage, *SU(3) violations in the nonleptonic decay of charmed hadrons*, *Phys. Lett. B* **257** (1991) 414 [[INSPIRE](#)].

D. Pirtskhalava and P. Uttayarat, *CP Violation and Flavor SU(3) Breaking in D-meson Decays*, *Phys. Lett. B* **712** (2012) 81 [[arXiv:1112.5451](#)] [[INSPIRE](#)].

Assume symmetry breaking originates from  $\overline{3}$

$$\begin{aligned} A' = & u_1 (\mathbf{B}_c)_i H(\overline{3})^i (\mathbf{B}_n)_k^j (M)_j^k + u_2 (\mathbf{B}_c)_i H(\overline{3})^j (\mathbf{B}_n)_k^i (M)_j^k \\ & + u_3 (\mathbf{B}_c)_i H(\overline{3})^j (\mathbf{B}_n)_j^k (M)_k^i \end{aligned}$$

$$B' = A' \Big|_{u_i \rightarrow v_i}$$

$$H(\overline{3}) = (s_c, 0, 0)$$

C.Q. Geng, Y.K. Hsiao, C.-W. Liu and T.-H. Tsai, *SU(3) symmetry breaking in charmed baryon decays*, *Eur. Phys. J. C* **78** (2018) 593 [[arXiv:1804.01666](#)] [[INSPIRE](#)].

# $\Xi_c - \Xi_c'$ mixing

$$R = 2\Gamma(\Xi_c^0 \rightarrow \Xi^- e^+ \nu_e) / 3\Gamma(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e)$$

$$\mathcal{B}_{\text{Belle}}(\Xi_c^0 \rightarrow \Xi^- e^+ \nu_e) = (1.31 \pm 0.04 \pm 0.07 \pm 0.38)\%,$$

$$\mathcal{B}_{\text{ALICE}}(\Xi_c^0 \rightarrow \Xi^- e^+ \nu_e) = (2.43 \pm 0.25 \pm 0.35 \pm 0.72)\%,$$

$$\mathcal{B}_{\text{LQCD}}(\Xi_c^0 \rightarrow \Xi^- e^+ \nu_e) = (2.38 \pm 0.44)\%$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) = (3.56 \pm 0.11 \pm 0.07)\%$$



$$R(\text{Belle}) = 0.33 \pm 0.10, \quad R(\text{ALICE}) = 0.60 \pm 0.21, \quad R(\text{LQCD}) = 0.59 \pm 0.11$$

$$R'_{av} = 0.46 \pm 0.07, \quad R_{av} = 0.59 \pm 0.10$$

$$R(SU(3)_F) = 1$$

$$|\theta_c| = 0.137(5)\pi$$

0.430398

$$|\Xi_c\rangle = \cos \theta_c |\Xi_c^{\bar{3}}\rangle + \sin \theta_c |\Xi_c^{\bar{6}}\rangle$$

$$|\Xi'_c\rangle = \cos \theta_c |\Xi_c^{\bar{6}}\rangle - \sin \theta_c |\Xi_c^{\bar{3}}\rangle$$

$$\theta = (1.200 \pm 0.090 \pm 0.020)^\circ$$

$$\theta = (1.220 \pm 0.130 \pm 0.010)^\circ$$

# Amplitude relations

Channel	$A$	Channel	$A$
$\Lambda_c^+ \rightarrow \Lambda^0 \pi^+$	$\frac{\sqrt{6}}{6}(-2a_1 - 2a_2 - 2a_3 + a_5 - 2a_6 + a_7)$	$\Xi_c^+ \rightarrow \Xi^0 \pi^+$	$-2a_3 - a_4 - a_6$
$\Lambda_c^+ \rightarrow p \bar{K}^0$	$-2a_1 + a_5 + a_6$	$\Xi_c^0 \rightarrow \Lambda^0 \bar{K}^0$	$\frac{\sqrt{6}}{6}(-4a_1 + 2a_2 + 2a_3 - 2a_5 + a_6 + a_7)$
$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$	$\frac{\sqrt{2}}{2}(-2a_1 + 2a_2 + 2a_3 + a_5 - a_7)$	$\Xi_c^0 \rightarrow \Sigma^0 \bar{K}^0$	$\frac{\sqrt{2}}{2}(-2a_2 - 2a_3 + a_6 - a_7)$
$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$	$\frac{\sqrt{2}}{2}(2a_1 - 2a_2 - 2a_3 - a_5 + a_7)$	$\Xi_c^0 \rightarrow \Sigma^+ K^-$	$2a_2 + a_4 + a_7$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	$\frac{\sqrt{2}}{6}c_\phi(-12a_0 - 6a_1 - 6a_2 + 6a_3 + 6a'_0 + 3a_5 + 3a_7) + s_\phi(2a_0 - a'_0 - a_4)$	$\Xi_c^0 \rightarrow \Xi^0 \pi^0$	$\frac{\sqrt{2}}{2}(-2a_1 + 2a_3 + a_4 - a_5)$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	$\frac{\sqrt{2}}{6}s_\phi(-12a_0 - 6a_1 - 6a_2 + 6a_3 + 6a'_0 + 3a_5 + 3a_7) - c_\phi(2a_0 - a'_0 - a_4)$	$\Xi_c^0 \rightarrow \Xi^0 \eta$	$\frac{\sqrt{2}}{6}c_\phi(12a_0 + 6a_1 - 6a_3 + 6a'_0 + 3a_4 + 3a_5) + \frac{1}{3}s_\phi(-6a_0 - 6a_2 - 3a'_0 - 3a_7)$
$\Lambda_c^+ \rightarrow \Xi^0 K^+$	$-2a_2 + a_4 + a_7$	$\Xi_c^0 \rightarrow \Xi^0 \eta'$	$\frac{\sqrt{2}}{6}s_\phi(12a_0 + 6a_1 - 6a_3 + 6a'_0 + 3a_4 + 3a_5) - \frac{1}{3}c_\phi(-6a_0 - 6a_2 - 3a'_0 - 3a_7)$
$\Xi_c^+ \rightarrow \Sigma^+ \bar{K}^0$	$2a_3 - a_4 - a_6$	$\Xi_c^0 \rightarrow \Xi^- \pi^+$	$2a_1 + a_5 + a_6$

$$\begin{aligned}
A(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+) &= -A(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0) \\
A(\Lambda_c^+ \rightarrow n K^+) &= \sin^2 \theta_c A(\Xi_c^+ \rightarrow \Xi^0 \pi^+) \\
A(\Xi_c^+ \rightarrow n \pi^+) &= \sin^2 \theta_c A(\Lambda_c^+ \rightarrow \Xi^0 K^+) \\
A(\Xi_c^+ \rightarrow \Sigma^+ K^0) &= \sin^2 \theta_c A(\Lambda_c^+ \rightarrow p \bar{K}^0) \\
A(\Lambda_c^+ \rightarrow p K^0) &= \sin^2 \theta_c A(\Xi_c^+ \rightarrow \Sigma^+ \bar{K}^0) \\
A(\Xi_c^0 \rightarrow \Sigma^- K^+) &= -\sin^2 \theta_c A(\Xi_c^0 \rightarrow \Xi^- \pi^+) \\
A(\Xi_c^0 \rightarrow p \pi^-) &= -\sin^2 \theta_c A(\Xi_c^0 \rightarrow \Sigma^+ K^-).
\end{aligned}$$

$$\begin{aligned}
A(\Lambda_c^+ \rightarrow \Sigma^+ K^0) &= A(\Xi_c^+ \rightarrow p \bar{K}^0) \\
A(\Lambda_c^+ \rightarrow n \pi^+) &= A(\Xi_c^+ \rightarrow \Xi^0 K^+) \\
A(\Xi_c^0 \rightarrow n \bar{K}^0) &= -A(\Xi_c^0 \rightarrow \Xi^0 K^0) \\
A(\Xi_c^0 \rightarrow p \pi^-) &= \sin \theta_c A(\Xi_c^0 \rightarrow p K^-) = -\sin \theta_c A(\Xi_c^0 \rightarrow \Sigma^+ \pi^-) = -\sin^2 \theta_c A(\Xi_c^0 \rightarrow \Sigma^+ K^-) \\
A(\Xi_c^0 \rightarrow \Sigma^- K^+) &= \sin \theta_c A(\Xi_c^0 \rightarrow \Xi^- K^+) = -\sin \theta_c A(\Xi_c^0 \rightarrow \Sigma^- \pi^+) = -\sin^2 \theta_c A(\Xi_c^0 \rightarrow \Xi^- \pi^+)
\end{aligned}$$

broken by SU(3) breaking

Channel	$s_c^{-1} A$	Channel	$s_c^{-1} A$
$\Lambda_c^+ \rightarrow \Lambda^0 K^+$	$\frac{\sqrt{6}}{6}(2a_1 - 4a_2 + 2a_3 + 3a_4 - a_5 + 2a_6 + 2a_7 - 2u_2 + u_3)$	$\Xi_c^+ \rightarrow \Xi^0 K^+$	$2a_2 + 2a_3 + a_6 - a_7 - u_2$
$\Lambda_c^+ \rightarrow p \pi^0$	$\frac{\sqrt{2}}{2}(2a_2 + 2a_3 - a_6 - a_7 + u_2)$	$\Xi_c^0 \rightarrow \Lambda^0 \pi^0$	$\frac{\sqrt{3}}{6}(-2a_1 - 2a_2 + 4a_3 + 3a_4 - a_5 - a_6 - a_7 + u_2 + u_3)$
$\Lambda_c^+ \rightarrow p \eta$	$\frac{\sqrt{2}}{2}c_\phi(4a_0 + 2a_2 - 2a_3 - 2a'_0 + a_6 - a_7 + u_2) + s_\phi(-2a_0 - 2a_1 + a'_0 + a_4 + a_5 + a_6 - u_3)$	$\Xi_c^0 \rightarrow \Lambda^0 \eta$	$\frac{\sqrt{3}}{6}c_\phi(12a_0 + 2a_1 + 2a_2 - 4a_3 + 6a'_0 + 3a_4 + a_5 + a_6 + a_7 + 2u_1 + u_2 + u_3) + \frac{\sqrt{6}}{6}s_\phi(-6a_0 - 4a_1 - 4a_2 + 2a_3 - 3a'_0 - 2a_5 + a_6 - 2a_7 + 2u_1)$
$\Lambda_c^+ \rightarrow p \eta'$	$\frac{\sqrt{2}}{2}s_\phi(4a_0 + 2a_2 - 2a_3 - 2a'_0 + a_6 - a_7 + u_2) - c_\phi(-2a_0 - 2a_1 + a'_0 + a_4 + a_5 + a_6 - u_3)$	$\Xi_c^0 \rightarrow \Lambda^0 \eta'$	$\frac{\sqrt{3}}{6}s_\phi(12a_0 + 2a_1 + 2a_2 - 4a_3 + 6a'_0 + 3a_4 + a_5 + a_6 + a_7 + 2u_1 + u_2 + u_3) - \frac{\sqrt{6}}{6}c_\phi(-6a_0 - 4a_1 - 4a_2 + 2a_3 - 3a'_0 - 2a_5 + a_6 - 2a_7 + 2u_1)$
$\Lambda_c^+ \rightarrow n \pi^+$	$2a_2 + 2a_3 + a_6 - a_7 + u_2$	$\Xi_c^0 \rightarrow p K^-$	$-2a_2 - a_4 - a_7 + u_1 + u_3$
$\Lambda_c^+ \rightarrow \Sigma^0 K^+$	$\frac{\sqrt{2}}{2}(2a_1 - 2a_3 - a_4 - a_5 + u_3)$	$\Xi_c^0 \rightarrow n \bar{K}^0$	$2a_1 - 2a_2 - 2a_3 + a_5 - a_7 + u_1$
$\Lambda_c^+ \rightarrow \Sigma^+ K^0$	$2a_1 - 2a_3 + a_4 - a_5 + u_3$	$\Xi_c^0 \rightarrow \Sigma^0 \pi^0$	$\frac{1}{2}(2a_1 + 2a_2 - a_4 + a_5 - a_6 + a_7 + 2u_1 + u_2 + u_3)$
$\Xi_c^+ \rightarrow \Lambda^0 \pi^+$	$\frac{\sqrt{6}}{6}(2a_1 + 2a_2 - 4a_3 - 3a_4 - a_5 - a_6 - a_7 - u_2 - u_3)$	$\Xi_c^0 \rightarrow \Sigma^0 \eta$	$\frac{1}{2}c_\phi(-4a_0 - 2a_1 - 2a_2 - 2a'_0 - a_4 - a_5 + a_6 - a_7 + u_2 + u_3) + \frac{\sqrt{2}}{2}s_\phi(2a_0 - 2a_3 + a'_0 + a_6)$
$\Xi_c^+ \rightarrow p \bar{K}^0$	$2a_1 - 2a_3 + a_4 - a_5 - u_3$	$\Xi_c^0 \rightarrow \Sigma^0 \eta'$	$\frac{1}{2}s_\phi(-4a_0 - 2a_1 - 2a_2 - 2a'_0 - a_4 - a_5 + a_6 - a_7 + u_2 + u_3) - \frac{\sqrt{2}}{2}c_\phi(2a_0 - 2a_3 + a'_0 + a_6)$
$\Xi_c^+ \rightarrow \Sigma^0 \pi^+$	$\frac{\sqrt{2}}{2}(2a_1 - 2a_2 + a_4 - a_5 + a_6 + a_7 + u_2 - u_3)$	$\Xi_c^0 \rightarrow \Xi^0 K^0$	$-2a_1 + 2a_2 + 2a_3 - a_5 + a_7 + u_1$
$\Xi_c^+ \rightarrow \Sigma^+ \pi^0$	$\frac{\sqrt{2}}{2}(-2a_1 + 2a_2 + a_4 + a_5 + a_6 - a_7 - u_2 + u_3)$	$\Xi_c^0 \rightarrow \Sigma^+ \pi^-$	$2a_2 + a_4 + a_7 + u_1 + u_3$
$\Xi_c^+ \rightarrow \Sigma^+ \eta$	$\frac{\sqrt{2}}{2}c_\phi(4a_0 + 2a_1 + 2a_2 - 2a'_0 - a_4 - a_5 - a_6 - a_7 - u_2 - u_3) + s_\phi(-2a_0 + 2a_3 + a'_0 - a_6)$	$\Xi_c^0 \rightarrow \Sigma^- \pi^+$	$2a_1 + a_5 + a_6 + u_1 + u_2$
$\Xi_c^+ \rightarrow \Sigma^+ \eta'$	$\frac{\sqrt{2}}{2}s_\phi(4a_0 + 2a_1 + 2a_2 - 2a'_0 - a_4 - a_5 - a_6 - a_7 - u_2 - u_3) - c_\phi(-2a_0 + 2a_3 + a'_0 - a_6)$	$\Xi_c^0 \rightarrow \Xi^- K^+$	$-2a_1 - a_5 - a_6 + u_1 + u_2$

# Coefficients from fit

## SU(3) breaking

## Exact SU(3)

(Fit 1)				(Fit 1')			
Coefficient	Value	Coefficient	Value	Coefficient	Value	Coefficient	Value
$a_0$	$-0.46 \pm 1.26$	$b_0$	$-0.78 \pm 3.10$	$a_0$	$-0.20 \pm 1.08$	$b_0$	$-0.75 \pm 2.41$
$a_1$	$-3.10^{+0.40}_{-0.48}$	$b_1$	$8.03^{+0.34}_{-0.48}$	$a_1$	$-3.95^{+0.15}_{-0.13}$	$b_1$	$3.40^{+0.85}_{-0.75}$
$a_2$	$1.28^{+0.15}_{-0.23}$	$b_2$	$2.14^{+1.42}_{-1.10}$	$a_2$	$0.98^{+0.19}_{-0.17}$	$b_2$	$4.17^{+0.30}_{-0.39}$
$a_3$	$1.44^{+0.30}_{-0.37}$	$b_3$	$0.67^{+0.66}_{-0.67}$	$a_3$	$-1.61 \pm 0.12$	$b_3$	$1.75^{+1.12}_{-0.88}$
$a'_0$	$1.69 \pm 2.51$	$b'_0$	$1.83 \pm 6.21$	$a'_0$	$1.16 \pm 2.16$	$b'_0$	$1.75 \pm 4.82$
$a_4$	$-0.03^{+0.38}_{-0.39}$	$b_4$	$-2.26^{+1.21}_{-1.42}$	$a_4$	$-0.13 \pm 0.25$	$b_4$	$-0.55^{+1.01}_{-1.12}$
$a_5$	$2.11^{+0.39}_{-0.36}$	$b_5$	$-2.09^{+0.60}_{-0.58}$	$a_5$	$1.03^{+0.30}_{-0.27}$	$b_5$	$-8.62^{+0.57}_{-0.55}$
$a_6$	$-3.13^{+0.77}_{-0.59}$	$b_6$	$-5.19^{+1.12}_{-0.66}$	$a_6$	$1.32^{+0.14}_{-0.17}$	$b_6$	$8.79^{+1.38}_{-1.59}$
$a_7$	$-0.35^{+0.36}_{-0.44}$	$b_7$	$-5.47^{+2.87}_{-2.11}$	$a_7$	$-1.12^{+0.33}_{-0.29}$	$b_7$	$0.23^{+1.07}_{-1.10}$
$u_1$	$-9.83^{+12.55}_{-1.94}$	$v_1$	$30.48 \pm 77.93$				
$u_2$	$-2.74^{+0.93}_{-0.77}$	$v_2$	$-14.11^{+3.77}_{-3.44}$				
$u_3$	$2.92^{+0.69}_{-0.74}$	$v_3$	$4.78^{+2.31}_{-2.26}$				

(Fit 2)				(Fit 2')			
Coefficient	Value	Coefficient	Value	Coefficient	Value	Coefficient	Value
$a_0$	$-0.47 \pm 1.23$	$b_0$	$-0.04 \pm 3.18$	$a_0$	$1.09 \pm 1.09$	$b_0$	$2.45 \pm 2.25$
$a_1$	$-4.58^{+0.73}_{-1.34}$	$b_1$	$8.08^{+1.74}_{-1.02}$	$a_1$	$-5.05^{+0.73}_{-1.31}$	$b_1$	$3.40^{+1.63}_{-0.98}$
$a_2$	$0.34^{+0.47}_{-0.63}$	$b_2$	$0.45^{+1.24}_{-1.35}$	$a_2$	$0.47^{+0.42}_{-0.53}$	$b_2$	$5.39^{+1.44}_{-0.76}$
$a_3$	$-2.14^{+0.40}_{-0.33}$	$b_3$	$0.03^{+0.85}_{-0.68}$	$a_3$	$-1.55^{+0.14}_{-0.16}$	$b_3$	$-0.53^{+0.98}_{-0.82}$
$a'_0$	$1.71 \pm 2.47$	$b'_0$	$3.64 \pm 6.36$	$a'_0$	$1.17 \pm 2.19$	$b'_0$	$1.68 \pm 2.45$
$a_4$	$0.15^{+0.39}_{-0.45}$	$b_4$	$-3.88^{+1.59}_{-1.36}$	$a_4$	$-0.41^{+0.38}_{-0.30}$	$b_4$	$-1.68^{+1.69}_{-1.31}$
$a_5$	$0.35^{+1.16}_{-2.65}$	$b_5$	$0.09^{+3.23}_{-1.46}$	$a_5$	$-1.01^{+1.38}_{-2.61}$	$b_5$	$-6.28^{+3.11}_{-1.69}$
$a_6$	$-1.94^{+0.52}_{-0.75}$	$b_6$	$-3.09^{+1.42}_{-1.53}$	$a_6$	$1.48^{+0.14}_{-0.17}$	$b_6$	$1.23^{+1.49}_{-2.12}$
$a_7$	$-2.79^{+0.89}_{-1.26}$	$b_7$	$-8.09^{+2.09}_{-2.49}$	$a_7$	$-1.87^{+0.64}_{-1.01}$	$b_7$	$3.75^{+3.38}_{-2.65}$
$u_1$	$0.07^{+4.27}_{-26.14}$	$v_1$	$26.62 \pm 218.96$	$\theta$	$0.89^{+0.24}_{-0.29}$		
$u_2$	$-2.52^{+0.90}_{-0.87}$	$v_2$	$-15.45^{+3.92}_{-2.75}$				
$u_3$	$3.37^{+0.65}_{-0.69}$	$v_3$	$4.80^{+2.20}_{-1.86}$				
$\theta$	$0.12^{+0.29}_{-0.28}$						

Identical mixing

$$(6.88^{+16.62}_{-16.04})^\circ$$

$$|\theta_c| = 0.137(5)\pi \quad 25^\circ \quad 0.430398$$

C.Q. Geng, X.-N. Jin, C.-W. Liu, PLB 833 (2023) 137736

$$\theta = (1.200 \pm 0.090 \pm 0.020)^\circ$$

$$\theta = (1.220 \pm 0.130 \pm 0.010)^\circ$$

H. Liu, L. Liu, P. Sun, J. Tan, W. Wang, Y. Yang, Q. Zhang, 2303.17863[hep-lat]

(Fit 3)				(Fit 3')			
Coefficient	Value	Coefficient	Value	Coefficient	Value	Coefficient	Value
$a_0$	$-4.09 \pm 1.15$	$b_0$	$-1.46 \pm 3.24$	$a_0$	$-0.20 \pm 1.09$	$b_0$	$-0.71 \pm 2.45$
$a_1$	$-7.86^{+2.42}_{-0.27}$	$b_1$	$6.60^{+0.78}_{-3.12}$	$a_1$	$-5.39^{+0.82}_{-2.11}$	$b_1$	$3.72^{+2.62}_{-1.14}$
$a_2$	$0.09^{+2.42}_{-0.26}$	$b_2$	$8.74^{+0.78}_{-2.28}$	$a_2$	$0.35^{+0.44}_{-0.75}$	$b_2$	$5.70^{+2.36}_{-0.88}$
$a_3$	$-2.09^{+0.17}_{-0.19}$	$b_3$	$-1.04^{+1.67}_{-1.21}$	$a_3$	$-1.55^{+0.14}_{-0.16}$	$b_3$	$-0.50^{+0.99}_{-0.82}$
$a'_0$	$-5.50 \pm 2.30$	$b'_0$	$0.25 \pm 6.48$	$a'_0$	$1.17 \pm 2.17$	$b'_0$	$1.67 \pm 4.89$
$a_4$	$0.22^{+0.43}_{-0.40}$	$b_4$	$-3.69^{+1.76}_{-2.17}$	$a_4$	$-0.43^{+0.37}_{-0.28}$	$b_4$	$-1.84^{+1.70}_{-1.21}$
$a_5$	$-6.53^{+4.83}_{-0.54}$	$b_5$	$0.24^{+1.22}_{-5.80}$	$a_5$	$-1.67^{+1.59}_{-4.21}$	$b_5$	$-5.52^{+5.03}_{-1.93}$
$a_6$	$1.59^{+0.13}_{-0.16}$	$b_6$	$11.40^{+1.61}_{-2.22}$	$a_6$	$1.49^{+0.14}_{-0.16}$	$b_6$	$11.27^{+1.41}_{-1.98}$
$a_7$	$-3.52^{+1.76}_{-0.50}$	$b_7$	$9.43^{+1.77}_{-5.10}$	$a_7$	$-2.08^{+0.70}_{-1.48}$	$b_7$	$4.55^{+5.00}_{-2.77}$
$u_1$	$-32.61 \pm 34.68$	$v_1$	$-19.78 \pm 108.09$	$\theta_1$	$0.97^{+0.26}_{-0.25}$		
$u_2$	$0.90^{+0.85}_{-0.78}$	$v_2$	$-1.99^{+1.72}_{-1.99}$	$\theta_2$	$0.01^{+3.84}_{-0.00}$		
$u_3$	$2.82^{+0.79}_{-0.81}$	$v_3$	$5.43^{+1.42}_{-1.54}$				
$\theta_1$	$1.23 \pm 0.27$						
$\theta_2$	$0.01^{+6.28}_{-0.01}$						

70°

different mixings

# Predictions from fit

Channel ( $\chi^2_{\min}/\text{d.o.f.}$ )	Fit 1 2.37	Fit 1' 2.34	Fit 2 2.16	Fit 2' 2.24	Fit 3 2.12	Fit 3' 2.29 )	Expt.
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda \pi^+)$	$1.28^{+0.13}_{-0.12}$	$1.28 \pm 0.08$	$1.29^{+0.13}_{-0.18}$	$1.28^{+0.18}_{-0.14}$	$1.30^{+0.14}_{-0.24}$	$1.28^{+0.31}_{-0.16}$	$1.30 \pm 0.07$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+)$	$1.29^{+0.09}_{-0.12}$	$1.31^{+0.06}_{-0.05}$	$1.28^{+0.11}_{-0.25}$	$1.30^{+0.12}_{-0.19}$	$1.28^{+0.38}_{-0.10}$	$1.30^{+0.16}_{-0.30}$	$1.29 \pm 0.07$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow p K_S)$	$1.57 \pm 0.14$	$1.58 \pm 0.09$	$1.61^{+0.18}_{-0.25}$	$1.58^{+0.15}_{-0.25}$	$1.65^{+0.78}_{-0.18}$	$1.59^{+0.16}_{-0.36}$	$1.59 \pm 0.08$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)$	$1.29^{+0.09}_{-0.12}$	$1.31^{+0.06}_{-0.05}$	$1.28^{+0.11}_{-0.25}$	$1.31^{+0.12}_{-0.19}$	$1.28^{+0.38}_{-0.11}$	$1.30^{+0.16}_{-0.30}$	$1.25 \pm 0.10$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta)$	$0.43 \pm 0.11$	$0.38 \pm 0.11$	$0.30^{+0.14}_{-0.12}$	$0.37^{+0.15}_{-0.14}$	$0.25 \pm 0.18$	$0.36^{+0.19}_{-0.18}$	$0.320 \pm 0.120$ [4, 10]
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta')$	$0.41^{+0.12}_{-0.13}$	$0.20 \pm 0.06$	$0.42^{+0.13}_{-0.14}$	$0.20 \pm 0.06$	$0.40^{+0.14}_{-0.12}$	$0.20^{+0.06}_{-0.08}$	$0.437 \pm 0.151$ [4, 10]
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Xi^0 K^+)$	$0.51 \pm 0.08$	$0.38^{+0.31}_{-0.32}$	$0.53^{+0.09}_{-0.11}$	$0.38^{+0.07}_{-0.09}$	$0.52^{+0.17}_{-0.09}$	$0.38^{+0.09}_{-0.13}$	$0.55 \pm 0.07$
$10^3 \mathcal{B}(\Lambda_c^+ \rightarrow p \eta)$	$1.50^{+0.18}_{-0.16}$	$1.37^{+1.20}_{-1.13}$	$1.42^{+0.22}_{-0.18}$	$1.42^{+0.17}_{-0.19}$	$1.30^{+0.26}_{-0.12}$	$1.42^{+0.19}_{-0.24}$	$1.42 \pm 0.12$
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \eta')$	$4.99 \pm 0.87$	$5.33^{+0.84}_{-0.85}$	$5.01^{+0.85}_{-1.15}$	$5.34^{+0.90}_{-1.10}$	$4.95^{+1.33}_{-1.08}$	$5.35^{+0.97}_{-1.47}$	$4.849 \pm 0.903$ [14, 15]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda K^+)$	$6.47^{+0.58}_{-0.61}$	$6.68^{+0.36}_{-0.35}$	$6.52^{+0.68}_{-0.98}$	$6.67^{+0.59}_{-0.82}$	$6.58^{+1.35}_{-0.49}$	$6.68^{+0.72}_{-1.20}$	$6.462 \pm 0.334$ [11, 12]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 K^+)$	$3.63^{+0.37}_{-0.40}$	$3.59^{+0.24}_{-0.22}$	$3.70^{+0.54}_{-0.39}$	$3.58^{+0.51}_{-0.58}$	$3.69^{+0.63}_{-1.10}$	$3.58^{+0.79}_{-0.87}$	$3.670 \pm 0.297$ [12, 13]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow n \pi^+)$	$6.51^{+1.42}_{-1.22}$	$8.16^{+0.78}_{-0.66}$	$6.82^{+1.43}_{-1.28}$	$8.19^{+1.55}_{-0.98}$	$7.04^{+1.89}_{-2.01}$	$8.20^{+2.64}_{-1.00}$	$6.6 \pm 1.3$ [16]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ K_S)$	$2.57^{+0.72}_{-0.75}$	$3.61^{+0.65}_{-0.61}$	$1.82^{+0.85}_{-0.64}$	$3.74^{+0.79}_{-0.89}$	$1.86^{+1.05}_{-1.01}$	$3.72^{+0.93}_{-1.20}$	$4.8 \pm 1.4$ [13]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \pi^0)$	$0.12^{+0.30}_{-0.26}$	$0.17 \pm 0.10$	$0.30 \pm 0.53$	$0.62^{+0.60}_{-0.62}$	$0.87^{+0.85}_{-0.81}$	$0.66^{+0.71}_{-0.63}$	$< 0.80$ [17]
$10^2 \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)$	$1.53^{+0.37}_{-0.40}$	$0.92^{+0.20}_{-0.18}$	$1.62^{+0.56}_{-0.84}$	$1.07^{+0.45}_{-0.69}$	$1.43^{+1.74}_{-2.09}$	$1.11^{+0.59}_{-1.09}$	$1.43 \pm 0.32$
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- K^+)$	$0.38^{+0.54}_{-0.81}$	$0.40^{+0.09}_{-0.08}$	$0.38^{+0.15}_{-2.03}$	$0.47^{+0.20}_{-0.31}$	$0.38^{+0.66}_{-0.52}$	$0.49^{+0.26}_{-0.49}$	$0.38 \pm 0.12$
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Lambda K_S)$	$3.14^{+0.86}_{-0.78}$	$4.28^{+0.58}_{-0.55}$	$2.96^{+1.22}_{-1.35}$	$3.53^{+1.39}_{-1.98}$	$3.37^{+4.20}_{-4.96}$	$3.36^{+0.18}_{-0.30}$	$3.34 \pm 0.67$
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Sigma^0 K_S)$	$0.69^{+0.40}_{-0.37}$	$0.79^{+0.26}_{-0.24}$	$0.60^{+0.38}_{-0.46}$	$0.72^{+0.43}_{-0.58}$	$0.69^{+1.00}_{-0.98}$	$0.69^{+0.48}_{-0.66}$	$0.69 \pm 0.24$
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Sigma^+ K^-)$	$1.85^{+0.67}_{-0.63}$	$1.73^{+0.41}_{-0.48}$	$1.89^{+0.76}_{-0.85}$	$1.80^{+0.96}_{-0.95}$	$1.81^{+2.38}_{-2.37}$	$1.81^{+1.43}_{-1.02}$	$1.8 \pm 0.4$
$10^2 \mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 \pi^+)$	$3.08^{+0.50}_{-0.49}$	$0.82^{+0.12}_{-0.10}$	$1.52^{+0.93}_{-0.94}$	$0.32^{+0.19}_{-0.24}$	$0.66^{+0.23}_{-0.25}$	$0.82^{+0.11}_{-0.13}$	$1.6 \pm 0.8$



# Predictions from fit

Channel ( $\chi^2_{\min}/\text{d.o.f.}$ )	Fit 1 2.37	Fit 1' 2.34	Fit 2 2.16	Fit 2' 2.24	Fit 3 2.12	Fit 3' 2.29	Expt.
$\alpha(\Lambda_c^+ \rightarrow \Lambda \pi^+)$	$-0.76^{+0.04}_{-0.02}$	$-0.76 \pm 0.01$	$-0.76^{+0.04}_{-0.03}$	$-0.75 \pm 0.06$	$-0.75^{+0.10}_{-0.05}$	$-0.75^{+0.08}_{-0.10}$	$-0.755 \pm 0.006$ [4, 12]
$\alpha(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+)$	$-0.47^{+0.06}_{-0.04}$	$-0.47^{+0.04}_{-0.02}$	$-0.47^{+0.09}_{-0.08}$	$-0.48^{+0.12}_{-0.06}$	$-0.47^{+0.13}_{-0.23}$	$-0.48^{+0.23}_{-0.07}$	$-0.466 \pm 0.026$ [4, 12]
$\alpha(\Lambda_c^+ \rightarrow p K_S)$	$-0.86^{+0.17}_{-0.13}$	$-0.48 \pm 0.19$	$-1.00 \pm 0.002$	$-0.14^{+0.35}_{-0.29}$	$-0.11^{+0.20}_{-0.53}$	$-0.13^{+0.47}_{-0.29}$	$0.18 \pm 0.45$
$\alpha(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)$	$-0.48^{+0.07}_{-0.04}$	$-0.48^{+0.04}_{-0.02}$	$-0.47^{+0.09}_{-0.08}$	$-0.48^{+0.12}_{-0.06}$	$-0.47^{+0.13}_{-0.23}$	$-0.48^{+0.23}_{-0.07}$	$-0.485 \pm 0.029$ [4, 10]
$\alpha(\Xi_c^0 \rightarrow \Xi^- \pi^+)$	$-0.65^{+0.08}_{-0.07}$	$-0.66 \pm 0.06$	$-0.65^{+0.16}_{-0.17}$	$-0.64^{+0.16}_{-0.20}$	$-0.64^{+0.21}_{-0.20}$	$-0.64^{+0.25}_{-0.31}$	$-0.64 \pm 0.05$
$\alpha(\Lambda_c^+ \rightarrow \Sigma^+ \eta)$	$-0.96^{+0.07}_{-0.08}$	$-0.96 \pm 0.05$	$-0.97^{+0.09}_{-0.10}$	$-1.00^{+0.05}_{-0.04}$	$-0.96^{+0.14}_{-0.11}$	$-0.99^{+0.08}_{-0.07}$	$-0.99 \pm 0.06$ [10]
$\alpha(\Lambda_c^+ \rightarrow \Sigma^+ \eta')$	$-0.46 \pm 0.08$	$-0.45 \pm 0.07$	$-0.45^{+0.09}_{-0.08}$	$-0.46^{+0.12}_{-0.10}$	$-0.46^{+0.08}_{-0.12}$	$-0.46^{+0.18}_{-0.11}$	$-0.46 \pm 0.07$ [10]
$\alpha(\Lambda_c^+ \rightarrow \Lambda K^+)$	$-0.58^{+0.11}_{-0.08}$	$-0.55 \pm 0.06$	$-0.58^{+0.09}_{-0.10}$	$-0.55^{+0.13}_{-0.11}$	$-0.57^{+0.08}_{-0.14}$	$-0.55^{+0.19}_{-0.10}$	$-0.585 \pm 0.052$ [12]
$\alpha(\Lambda_c^+ \rightarrow \Sigma^0 K^+)$	$-0.65^{+0.19}_{-0.21}$	$-0.98^{+0.02}_{-0.01}$	$-0.53^{+0.21}_{-0.27}$	$-0.98 \pm 0.03$	$-0.63^{+0.26}_{-0.19}$	$-0.98^{+0.05}_{-0.04}$	$-0.55 \pm 0.20$ [12]
$\alpha(\Lambda_c^+ \rightarrow \Xi^0 K^+)$	$0.99 \pm 0.05$	$0.90 \pm 0.04$	$1.00^{+0.03}_{-0.04}$	$0.91^{+0.09}_{-0.07}$	$0.97^{+0.07}_{-0.06}$	$0.91^{+0.13}_{-0.10}$	

- better with symmetry breaking terms in all schemes
- decay asymmetry for  $\Lambda_c^+ \rightarrow p K_S$  in all schemes prefers to be negative

# Comparison

channel	Fit-III	Fit-III'	GLT [18]	HXH [19]	ZWHY [20]	ZXMC [13, 37]	Expt.
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda^0 \pi^+)$	$1.30^{+0.12}_{-0.14}$	$1.27^{+0.08}_{-0.09}$	$1.30 \pm 0.07$	$1.307 \pm 0.069$	$1.32 \pm 0.34$	1.30	$1.30 \pm 0.07$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow p K_S)$	$1.65 \pm 0.11$	$1.59 \pm 0.10$	$1.57 \pm 0.08$	$1.587 \pm 0.077$	$1.57 \pm 0.05$	1.06	$1.59 \pm 0.08$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+)$	$1.27 \pm 0.09$	$1.30 \pm 0.06$	$1.27 \pm 0.06$	$1.272 \pm 0.056$	$1.3 \pm 0.32$	2.24	$1.29 \pm 0.07$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)$	$1.27 \pm 0.09$	$1.30 \pm 0.06$	$1.27 \pm 0.06$	$1.283 \pm 0.057$	$1.23 \pm 0.17$	2.24	$1.25 \pm 0.10$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta)$	$0.30^{+0.06}_{-0.07}$	$0.31 \pm 0.05$	$0.32 \pm 0.13$	$0.45 \pm 0.19$	$0.47 \pm 0.22$	0.74	$0.44 \pm 0.20$ $0.314 \pm 0.044$ [7]
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta')$	$0.39 \pm 0.08$	$0.24 \pm 0.05$	$1.44 \pm 0.56$	$1.5 \pm 0.60$	$0.93 \pm 0.28$	-	$1.50 \pm 0.60$ $0.416 \pm 0.085$ [7]
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Xi^0 K^+)$	$0.50^{+0.06}_{-0.09}$	$0.38 \pm 0.03$	$0.56 \pm 0.09$	$0.548 \pm 0.068$	$0.59 \pm 0.17$	0.73	$0.55 \pm 0.07$
$10^3 \mathcal{B}(\Lambda_c^+ \rightarrow p \eta)$	$1.27 \pm 0.11$	$1.36^{+0.11}_{-0.12}$	$1.15 \pm 0.27$	$1.27 \pm 0.24$	$1.14 \pm 0.35$	1.28	$1.42 \pm 0.12$
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \eta')$	$4.65^{+0.79}_{-0.77}$	$5.93^{+0.73}_{-0.71}$	$24.5 \pm 14.6$	$27 \pm 38$	$7.1 \pm 1.4$	-	$4.73 \pm 0.97$ [5] $5.62^{+2.46}_{-2.04} \pm 0.26$ [2]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda^0 K^+)$	$6.54^{+0.42}_{-0.49}$	$6.62^{+0.23}_{-0.22}$	$6.5 \pm 1.0$	$6.4 \pm 1.0$	$5.9 \pm 1.7$	10.7	$6.21 \pm 0.61$ [3] $6.57 \pm 0.40$ [6]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 K^+)$	$3.71^{+0.39}_{-0.36}$	$3.56^{+0.68}_{-0.69}$	$5.4 \pm 0.7$	$5.04 \pm 0.56$	$5.5 \pm 1.6$	7.2	$4.7 \pm 0.95$ [4] $3.58 \pm 0.28$ [6]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow n \pi^+)$	$6.47^{+1.33}_{-1.55}$	$8.15^{+0.69}_{-0.67}$	$8.5 \pm 2.0$	$3.5 \pm 1.1$	$7.7 \pm 2.0$	-	$6.6 \pm 1.3$ [1]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ K_S)$	$1.99^{+0.49}_{-0.46}$	$3.11^{+0.35}_{-0.34}$	$5.45 \pm 0.75$	$1.03 \pm 0.42$	$9.55 \pm 2.4$	7.2	$4.8 \pm 1.4$ [4]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \pi^0)$	$0.51^{+0.59}_{-0.61}$	$0.16 \pm 0.09$	$1.2 \pm 1.2$	$44.5 \pm 8.5$	$0.8^{+0.9}_{-0.8}$	1.26	$< 0.80$ [35]
$10^2 \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)$	$2.43^{+0.60}_{-0.64}$	$0.70^{+0.25}_{-0.22}$	$2.21 \pm 0.14$	$1.21 \pm 0.21$	$1.93 \pm 0.28$	6.47	$1.43 \pm 0.32$
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- K^+)$	$0.60^{+1.03}_{-0.67}$	$0.31^{+0.11}_{-0.09}$	$0.98 \pm 0.06$	$0.47 \pm 0.083$	$0.56 \pm 0.08$	3.90	$0.38 \pm 0.12$
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Lambda^0 K_S)$	$3.34^{+0.97}_{-0.98}$	$3.79^{+0.66}_{-0.61}$	$5.25 \pm 0.3$	$3.34 \pm 0.65$	$4.16 \pm 2.51$	6.65	$3.34 \pm 0.67$
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Sigma^0 K_S)$	$0.74^{+0.25}_{-0.30}$	$0.73^{+0.25}_{-0.25}$	$0.4 \pm 0.4$	$0.69 \pm 0.24$	$3.96 \pm 0.25$	0.2	$0.69 \pm 0.24$
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Sigma^+ K^-)$	$1.86^{+0.45}_{-0.71}$	$1.74^{+0.41}_{-0.51}$	$5.9 \pm 1.1$	$2.21 \pm 0.68$	$22.0 \pm 5.7$	4.6	$1.8 \pm 0.4$
$10^2 \mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 \pi^+)$	$0.55^{+0.19}_{-0.20}$	$0.81 \pm 0.11$	$0.38 \pm 0.20$	$0.54 \pm 0.18$	$0.93 \pm 0.36$	1.72	$1.6 \pm 0.8$

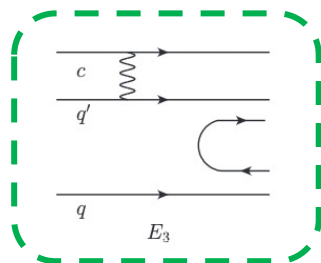
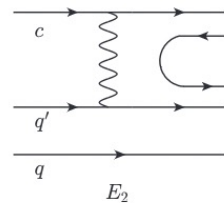
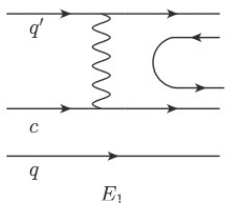
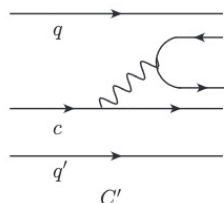
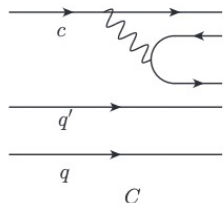
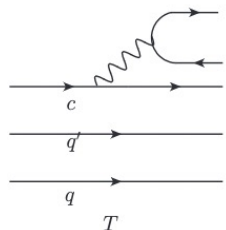


Fit within topological diagrams

# Working frame

$$\Gamma = \frac{p_c}{8\pi} \left( \frac{(m_i + m_f)^2 - m_P^2}{m_i^2} |A|^2 + \frac{(m_i - m_f)^2 - m_P^2}{m_i^2} |B|^2 \right),$$

$$\alpha = \frac{2\kappa \text{Re}(A^* B)}{|A|^2 + \kappa^2 |B|^2}, \beta = \frac{2\kappa \text{Im}(A^* B)}{|A|^2 + \kappa^2 |B|^2}, \gamma = \frac{|A|^2 - \kappa^2 |B|^2}{|A|^2 + \kappa^2 |B|^2},$$



22 parameters

$$A_T, A_C e^{i\delta_{AC}}, A_{C'} e^{i\delta_{AC'}}, A_{E_1} e^{i\delta_{AE_1}}, A_{E_2} e^{i\delta_{AE_2}}, A_{E_3} e^{i\delta_{AE_3}},$$

$$B_T, B_C e^{i\delta_{BC}}, B_{C'} e^{i\delta_{BC'}}, B_{E_1} e^{i\delta_{BE_1}}, B_{E_2} e^{i\delta_{BE_2}}, B_{E_3} e^{i\delta_{BE_3}}.$$

w/ or w/o  $\Lambda^0 - \Sigma^0$  mixing

Channel	Contributions	Channel	Contributions	Channel	Contributions
$\Lambda_c^+ \rightarrow \Lambda^0 \pi^+$	$T, C', E_1, E_3$	$\Lambda_c^+ \rightarrow \Xi^0 K^+$	$E_1, E_3$	$\Xi_c^0 \rightarrow \Xi^0 \pi^0$	$C', E_1$
$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$	$T, C', E_1, E_3$	$\Xi_c^+ \rightarrow \Sigma^+ \bar{K}^0$	$C, C'$	$\Xi_c^0 \rightarrow \Xi^0 \eta$	$C', E_1, E_2, E_3$
$\Lambda_c^+ \rightarrow p \bar{K}^0$	$C, E_2$	$\Xi_c^+ \rightarrow \Xi^0 \pi^+$	$T, C'$	$\Xi_c^0 \rightarrow \Xi^0 \eta'$	$C', E_1, E_2, E_3$
$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$	$C', E_1, E_3$	$\Xi_c^0 \rightarrow \Lambda^0 \bar{K}^0$	$C, C', E_2, E_3$	$\Xi_c^0 \rightarrow \Xi^- \pi^+$	$T, E_1$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	$C', E_1, E_2, E_3$	$\Xi_c^0 \rightarrow \Sigma^0 \bar{K}^0$	$C, C', E_2, E_3$	$\Omega_c^0 \rightarrow \Xi^0 \bar{K}^0$	$C, C'$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	$C', E_1, E_2, E_3$	$\Xi_c^0 \rightarrow \Sigma^+ K^-$	$E_2, E_3$		
$\Lambda_c^+ \rightarrow \Lambda^0 K^+$	$T, C', E_1, E_3$	$\Xi_c^+ \rightarrow \Sigma^+ \eta$	$C, C', E_1, E_2, E_3$	$\Xi_c^0 \rightarrow \Xi^0 K^0$	$C', E_2, E_3$
$\Lambda_c^+ \rightarrow p \pi^0$	$C, C', E_1, E_2, E_3$	$\Xi_c^+ \rightarrow \Sigma^+ \eta'$	$C, C', E_1, E_2, E_3$	$\Xi_c^0 \rightarrow \Sigma^+ \pi^-$	$E_2, E_3$
$\Lambda_c^+ \rightarrow p \eta$	$C, C', E_1, E_2, E_3$	$\Xi_c^+ \rightarrow \Xi^0 K^+$	$T, C', E_1, E_3$	$\Xi_c^0 \rightarrow \Sigma^- \pi^+$	$T, E_1$
$\Lambda_c^+ \rightarrow p \eta'$	$C, C', E_1, E_2, E_3$	$\Xi_c^0 \rightarrow \Lambda^0 \pi^0$	$C, C', E_1, E_2, E_3$	$\Xi_c^0 \rightarrow \Xi^- K^+$	$T, E_1$
$\Lambda_c^+ \rightarrow n \pi^+$	$T, C', E_1, E_3$	$\Xi_c^0 \rightarrow \Lambda^0 \eta$	$C, C', E_1, E_2, E_3$	$\Omega_c^0 \rightarrow \Sigma^0 \bar{K}^0$	$C', E_2, E_3$
$\Lambda_c^+ \rightarrow \Sigma^0 K^+$	$T, C', E_1, E_3$	$\Xi_c^0 \rightarrow \Lambda^0 \eta'$	$C, C', E_1, E_2, E_3$	$\Omega_c^0 \rightarrow \Sigma^+ K^-$	$E_2, E_3$
$\Lambda_c^+ \rightarrow \Sigma^+ K^0$	$C', E_2$	$\Xi_c^0 \rightarrow p K^-$	$E_2, E_3$	$\Omega_c^0 \rightarrow \Lambda^0 \bar{K}^0$	$C', E_2, E_3$
$\Xi_c^+ \rightarrow \Lambda^0 \pi^+$	$T, C', E_1, E_3$	$\Xi_c^0 \rightarrow n \bar{K}^0$	$C', E_2, E_3$	$\Omega_c^0 \rightarrow \Xi^0 \pi^0$	$C, E_1$
$\Xi_c^+ \rightarrow p \bar{K}^0$	$C', E_2$	$\Xi_c^0 \rightarrow \Sigma^0 \pi^0$	$C, C', E_1, E_2, E_3$	$\Omega_c^0 \rightarrow \Xi^- \pi^+$	$T, E_1$
$\Xi_c^+ \rightarrow \Sigma^0 \pi^+$	$T, C', E_1, E_3$	$\Xi_c^0 \rightarrow \Sigma^0 \eta$	$C, C', E_1, E_2, E_3$		
$\Xi_c^+ \rightarrow \Sigma^+ \pi^0$	$C, E_1, E_3$	$\Xi_c^0 \rightarrow \Sigma^0 \eta'$	$C, C', E_1, E_2, E_3$		

# Fitted parameters

w/ mixing

w/o mixing

w/  $E_3$

FitI				FitI'			
Coefficient	Value	Coefficient	Value	Coefficient	Value	Coefficient	Value
$A_T$	$-0.46 \pm 1.57$	$B_T$	$23.32 \pm 5.20$	$A_T$	$-0.27 \pm 1.71$	$B_T$	$24.19 \pm 5.07$
$A_C$	$5.84 \pm 1.99$	$B_C$	$37.02 \pm 3.94$	$A_C$	$5.70 \pm 2.01$	$B_C$	$37.20 \pm 3.85$
$A_{C'}$	$-4.42 \pm 0.68$	$B_{C'}$	$-31.08 \pm 2.52$	$A_{C'}$	$-4.31 \pm 0.71$	$B_{C'}$	$-31.32 \pm 2.58$
$A_{E_1}$	$-6.77 \pm 1.72$	$B_{E_1}$	$-26.82 \pm 4.52$	$A_{E_1}$	$-6.71 \pm 1.74$	$B_{E_1}$	$-26.76 \pm 4.90$
$A_{E_2}$	$-5.32 \pm 0.96$	$B_{E_2}$	$-7.51 \pm 4.15$	$A_{E_2}$	$-5.34 \pm 0.95$	$B_{E_2}$	$-8.02 \pm 4.34$
$A_{E_3}$	$1.64 \pm 1.70$	$B_{E_3}$	$-9.87 \pm 5.59$	$A_{E_3}$	$1.62 \pm 1.69$	$B_{E_3}$	$-10.07 \pm 6.12$
$\delta_{A_C}$	$1.81 \pm 0.44$	$\delta_{B_C}$	$-0.53 \pm 0.17$	$\delta_{A_C}$	$1.76 \pm 0.43$	$\delta_{B_C}$	$-0.53 \pm 0.17$
$\delta_{A_{C'}}$	$2.53 \pm 0.16$	$\delta_{B_{C'}}$	$-0.28 \pm 0.04$	$\delta_{A_{C'}}$	$2.51 \pm 0.15$	$\delta_{B_{C'}}$	$-0.27 \pm 0.04$
$\delta_{A_{E_1}}$	$1.84 \pm 0.30$	$\delta_{B_{E_1}}$	$1.40 \pm 0.30$	$\delta_{A_{E_1}}$	$1.80 \pm 0.31$	$\delta_{B_{E_1}}$	$1.37 \pm 0.30$
$\delta_{A_{E_2}}$	$1.38 \pm 0.35$	$\delta_{B_{E_2}}$	$-4.99 \pm 0.57$	$\delta_{A_{E_2}}$	$1.33 \pm 0.32$	$\delta_{B_{E_2}}$	$-5.03 \pm 0.51$
$\delta_{A_{E_3}}$	$1.90 \pm 0.89$	$\delta_{B_{E_3}}$	$-2.19 \pm 0.41$	$\delta_{A_{E_3}}$	$1.83 \pm 0.97$	$\delta_{B_{E_3}}$	$-2.24 \pm 0.39$
$\theta$	-			$\theta$	$-0.03 \pm 0.02$		

w/o  $E_3$

FitII				FitII'			
Coefficient	Value	Coefficient	Value	Coefficient	Value	Coefficient	Value
$A_T$	$-1.94 \pm 0.68$	$B_T$	$22.58 \pm 3.58$	$A_T$	$-2.08 \pm 0.72$	$B_T$	$23.07 \pm 3.61$
$A_C$	$6.09 \pm 1.35$	$B_C$	$39.75 \pm 2.98$	$A_C$	$5.95 \pm 1.40$	$B_C$	$39.69 \pm 2.95$
$A_{C'}$	$-4.58 \pm 0.41$	$B_{C'}$	$-30.62 \pm 1.68$	$A_{C'}$	$-4.52 \pm 0.42$	$B_{C'}$	$-30.61 \pm 1.69$
$A_{E_1}$	$-5.54 \pm 0.33$	$B_{E_1}$	$-18.68 \pm 1.10$	$A_{E_1}$	$-5.56 \pm 0.34$	$B_{E_1}$	$-18.60 \pm 1.08$
$A_{E_2}$	$-3.97 \pm 0.44$	$B_{E_2}$	$-4.33 \pm 2.34$	$A_{E_2}$	$-3.99 \pm 0.44$	$B_{E_2}$	$-4.33 \pm 2.32$
$A_{E_3}$	-	$B_{E_3}$	-	$A_{E_3}$	-	$B_{E_3}$	-
$\delta_{A_C}$	$1.98 \pm 0.27$	$\delta_{B_C}$	$-0.38 \pm 0.10$	$\delta_{A_C}$	$1.97 \pm 0.28$	$\delta_{B_C}$	$-0.39 \pm 0.10$
$\delta_{A_{C'}}$	$2.48 \pm 0.10$	$\delta_{B_{C'}}$	$-0.27 \pm 0.04$	$\delta_{A_{C'}}$	$2.48 \pm 0.10$	$\delta_{B_{C'}}$	$-0.27 \pm 0.04$
$\delta_{A_{E_1}}$	$1.78 \pm 0.11$	$\delta_{B_{E_1}}$	$1.71 \pm 0.15$	$\delta_{A_{E_1}}$	$1.79 \pm 0.11$	$\delta_{B_{E_1}}$	$1.71 \pm 0.15$
$\delta_{A_{E_2}}$	$1.39 \pm 0.26$	$\delta_{B_{E_2}}$	$-5.32 \pm 0.62$	$\delta_{A_{E_2}}$	$1.39 \pm 0.26$	$\delta_{B_{E_2}}$	$-5.29 \pm 0.62$
$\delta_{A_{E_3}}$	-	$\delta_{B_{E_3}}$	-	$\delta_{A_{E_3}}$	-	$\delta_{B_{E_3}}$	-
$\theta$	-			$\theta$	$1.61 \pm 0.02$		

P-wave amplitudes have large sizes compared with corresponding s-wave one

The uncertainty of  $E_3$  is large

# TDA predictions in various schemes

Better: w/o  $E_3$

$\Lambda^0/\Sigma^0$  involved decays  
do not work well;

To introduce a mixing  
seems not a prescription

negative  $\alpha$

Obs.	Fit I		Fit I'		Fit II		Fit II'		Expt.
	$\chi^2_i$	Pred.	$\chi^2_i$	Pred.	$\chi^2_i$	Pred.	$\chi^2_i$	Pred.	
	$(\chi^2_{\min}/\text{d.o.f.})$	12.50		14.05		8.60		8.78	
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda^0 \pi^+)$	0.00	$1.30^{+0.85}_{-0.67}$	0.84	$1.36^{+0.92}_{-0.73}$	0.02	$1.29^{+0.19}_{-0.16}$	0.41	$1.35^{+0.20}_{-0.18}$	$1.30 \pm 0.07$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+)$	0.12	$1.26^{+0.82}_{-0.65}$	2.51	$1.16^{+0.76}_{-0.61}$	0.21	$1.25^{+0.18}_{-0.16}$	0.03	$1.28^{+0.17}_{-0.15}$	$1.29 \pm 0.07$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow p K_S)$	0.03	$1.58^{+0.49}_{-0.40}$	0.03	$1.58^{+0.49}_{-0.40}$	0.05	$1.57^{+0.32}_{-0.29}$	0.01	$1.58^{+0.33}_{-0.29}$	$1.59 \pm 0.08$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)$	0.01	$1.27^{+0.54}_{-0.47}$	0.01	$1.26^{+0.56}_{-0.47}$	0.44	$1.32^{+0.16}_{-0.15}$	0.22	$1.30 \pm 0.15$	$1.25 \pm 0.10$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta)$	0.12	$0.33^{+0.26}_{-0.19}$	0.13	$0.33^{+0.26}_{-0.19}$	0.09	$0.33^{+0.09}_{-0.08}$	0.10	$0.33^{+0.09}_{-0.08}$	$0.32 \pm 0.04$ [2, 4, 5]
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta')$	0.06	$0.40^{+0.14}_{-0.12}$	0.06	$0.40^{+0.14}_{-0.12}$	0.49	$0.34 \pm 0.04$	0.37	$0.35^{+0.05}_{-0.04}$	$0.44 \pm 0.15$ [2, 4, 5]
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Xi^0 K^+)$	0.04	$0.54^{+0.40}_{-0.30}$	0.01	$0.54^{+0.41}_{-0.31}$	0.38	$0.59 \pm 0.05$	0.02	$0.54 \pm 0.05$	$0.55 \pm 0.07$
$10^3 \mathcal{B}(\Lambda_c^+ \rightarrow p \eta)$	0.00	$1.40^{+0.59}_{-0.50}$	0.00	$1.41^{+0.59}_{-0.49}$	0.08	$1.37^{+0.32}_{-0.29}$	0.14	$1.36^{+0.33}_{-0.29}$	$1.40 \pm 0.11$ [7, 8]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \eta')$	0.40	$5.42^{+1.47}_{-1.32}$	0.42	$5.43^{+1.49}_{-1.35}$	0.53	$5.50^{+0.64}_{-0.57}$	0.79	$5.65^{+0.61}_{-0.57}$	$4.85 \pm 0.90$ [9, 10]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda^0 K^+)$	3.01	$5.89^{+3.52}_{-2.78}$	1.29	$6.08^{+3.93}_{-3.25}$	3.54	$5.84^{+0.95}_{-0.77}$	0.79	$6.16^{+0.98}_{-0.84}$	$6.44 \pm 0.32$ [11–14]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 K^+)$	6.65	$4.80^{+2.95}_{-2.31}$	3.31	$4.51^{+2.90}_{-2.34}$	5.76	$4.73^{+0.77}_{-0.63}$	0.00	$3.80^{+0.70}_{-0.58}$	$3.82 \pm 0.38$ [11, 12, 14, 15]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow n \pi^+)$	0.29	$7.30^{+4.98}_{-3.95}$	0.21	$7.19^{+5.12}_{-3.98}$	0.25	$7.25^{+1.16}_{-0.95}$	0.43	$7.46^{+1.11}_{-0.96}$	$6.6 \pm 1.3$ [16]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ K_S)$	0.64	$3.68^{+1.06}_{-0.91}$	0.67	$3.66^{+1.02}_{-0.88}$	1.70	$2.98^{+0.57}_{-0.56}$	1.65	$3.00^{+0.58}_{-0.52}$	$4.8 \pm 1.4$ [15]
$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \pi^0)$	0.17	$0.32^{+2.22}_{-1.31}$	0.18	$0.32^{+2.24}_{-1.33}$	2.32	$1.17^{+0.93}_{-0.72}$	1.62	$0.98^{+0.96}_{-0.69}$	$< 0.77$ [7, 8]
$10^2 \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)$	0.33	$1.61^{+0.61}_{-0.50}$	0.36	$1.62^{+0.62}_{-0.51}$	0.03	$1.38^{+0.26}_{-0.22}$	0.00	$1.44^{+0.27}_{-0.21}$	$1.43 \pm 0.32$ [2, 17]
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- K^+)$	1.81	$0.23^{+0.11}_{-0.09}$	1.51	$0.24^{+0.11}_{-0.10}$	1.69	$0.23 \pm 0.07$	1.22	$0.26^{+0.08}_{-0.06}$	$0.39 \pm 0.12$ [2, 18]
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Lambda^0 K_S)$	11.30	$0.85^{+2.03}_{-1.34}$	10.05	$0.98^{+2.33}_{-1.46}$	10.48	$0.93^{+0.89}_{-0.62}$	10.38	$0.94^{+1.00}_{-0.70}$	$3.2 \pm 0.7$ [2, 19, 20]
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Sigma^0 K_S)$	1.16	$0.71^{+1.83}_{-1.20}$	1.32	$0.72^{+1.79}_{-1.15}$	2.46	$0.79^{+0.78}_{-0.54}$	2.28	$0.78^{+0.75}_{-0.53}$	$0.54 \pm 0.16$ [19]
$10^3 \mathcal{B}(\Xi_c^0 \rightarrow \Sigma^+ K^-)$	0.01	$1.83^{+2.24}_{-1.61}$	0.01	$1.83^{+2.35}_{-1.68}$	0.04	$1.88^{+0.47}_{-0.40}$	0.01	$1.83^{+0.47}_{-0.40}$	$1.8 \pm 0.4$ [19]
$10^2 \mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 \pi^+)$	0.68	$0.94^{+0.55}_{-0.39}$	0.85	$0.86^{+0.59}_{-0.40}$	1.17	$0.73^{+0.26}_{-0.19}$	1.22	$0.72^{+0.25}_{-0.18}$	$1.6 \pm 0.8$ [17, 21]
$\alpha(\Lambda_c^+ \rightarrow \Lambda^0 \pi^+)$	6.13	$-0.74^{+0.44}_{-0.29}$	6.16	$-0.74^{+0.48}_{-0.29}$	5.87	$-0.74^{+0.12}_{-0.09}$	7.86	$-0.73^{+0.12}_{-0.09}$	$-0.76 \pm 0.01$ [2, 14]
$\alpha(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+)$	53.57	$-0.69^{+0.42}_{-0.29}$	53.55	$-0.69^{+0.46}_{-0.30}$	53.86	$-0.69^{+0.12}_{-0.09}$	52.03	$-0.69^{+0.12}_{-0.09}$	$-0.47 \pm 0.03$ [2, 14]
$\alpha(\Lambda_c^+ \rightarrow p K_S)$	0.66	$-0.19^{+0.34}_{-0.30}$	0.64	$-0.18^{+0.32}_{-0.29}$	0.90	$-0.25^{+0.22}_{-0.20}$	0.99	$-0.27^{+0.23}_{-0.21}$	$0.18 \pm 0.45$
$\alpha(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)$	0.00	$-0.49^{+0.35}_{-0.28}$	0.00	$-0.49^{+0.35}_{-0.28}$	0.30	$-0.51^{+0.10}_{-0.09}$	0.01	$-0.49^{+0.10}_{-0.09}$	$-0.49 \pm 0.03$ [2, 5]
$\alpha(\Xi_c^0 \rightarrow \Xi^- \pi^+)$	0.00	$-0.64^{+0.34}_{-0.26}$	0.00	$-0.64^{+0.34}_{-0.27}$	0.36	$-0.61 \pm 0.14$	0.02	$-0.63^{+0.15}_{-0.14}$	$-0.64 \pm 0.05$
$\alpha(\Lambda_c^+ \rightarrow \Sigma^+ \eta)$	0.12	$-0.97^{+0.37}_{-0.17}$	0.15	$-0.97^{+0.37}_{-0.17}$	0.54	$-0.95^{+0.10}_{-0.05}$	0.34	$-0.95^{+0.10}_{-0.05}$	$-0.99 \pm 0.06$ [5]
$\alpha(\Lambda_c^+ \rightarrow \Sigma^+ \eta')$	0.01	$-0.47^{+0.19}_{-0.18}$	0.00	$-0.46^{+0.20}_{-0.19}$	0.25	$-0.42 \pm 0.09$	0.19	$-0.43^{+0.09}_{-0.09}$	$-0.46 \pm 0.07$ [5]
$\alpha(\Lambda_c^+ \rightarrow \Lambda^0 K^+)$	0.05	$-0.57^{+0.44}_{-0.31}$	0.02	$-0.58^{+0.44}_{-0.32}$	0.73	$-0.54^{+0.13}_{-0.11}$	4.38	$-0.69^{+0.14}_{-0.12}$	$-0.585 \pm 0.052$ [14]
$\alpha(\Lambda_c^+ \rightarrow \Sigma^0 K^+)$	0.13	$-0.62^{+0.47}_{-0.31}$	0.05	$-0.59^{+0.47}_{-0.31}$	0.04	$-0.59^{+0.14}_{-0.11}$	0.25	$-0.45^{+0.15}_{-0.13}$	$-0.55 \pm 0.20$ [14]
$\alpha(\Lambda_c^+ \rightarrow \Xi^0 K^+)$		$-0.94^{+0.38}_{-0.19}$		$-0.95^{+0.39}_{-0.19}$		$-0.91^{+0.08}_{-0.05}$		$-0.87^{+0.08}_{-0.05}$	

# Predictions for more observables

Channel	Fit I			
	$\mathcal{B}$	$\alpha$	$\beta$	$\gamma$
$\Lambda_c^+ \rightarrow \Lambda^0 \pi^+$	$(1.30^{+0.85}_{-0.67}) \times 10^{-2}$	$-0.73^{+0.44}_{-0.29}$	$-0.01^{+0.56}_{-0.57}$	$0.68^{+0.29}_{-0.43}$
$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$	$(1.26^{+0.82}_{-0.65}) \times 10^{-2}$	$-0.69^{+0.42}_{-0.29}$	$-0.01 \pm 0.54$	$0.72^{+0.26}_{-0.41}$
$\Lambda_c^+ \rightarrow p K_S$	$(1.58^{+0.49}_{-0.40}) \times 10^{-2}$	$-0.19^{+0.34}_{-0.30}$	$0.24 \pm 0.30$	$-0.95^{+0.17}_{-0.08}$
$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$	$(1.27^{+0.54}_{-0.47}) \times 10^{-2}$	$-0.49^{+0.34}_{-0.29}$	$-0.04^{+0.35}_{-0.33}$	$-0.87^{+0.26}_{-0.14}$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	$(0.33^{+0.26}_{-0.19}) \times 10^{-2}$	$-0.97^{+0.37}_{-0.17}$	$0.18^{+0.42}_{-0.46}$	$-0.16^{+0.54}_{-0.51}$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	$(0.40^{+0.14}_{-0.12}) \times 10^{-2}$	$-0.47^{+0.19}_{-0.18}$	$0.46^{+0.20}_{-0.22}$	$0.76^{+0.11}_{-0.17}$
$\Lambda_c^+ \rightarrow \Xi^0 K^+$	$(0.54^{+0.40}_{-0.30}) \times 10^{-2}$	$-0.94^{+0.37}_{-0.20}$	$-0.30^{+0.56}_{-0.47}$	$0.17^{+0.39}_{-0.52}$
$\Lambda_c^+ \rightarrow p \eta$	$(1.40^{+0.59}_{-0.50}) \times 10^{-3}$	$0.01^{+0.39}_{-0.38}$	$-0.08^{+0.41}_{-0.36}$	$-1.00^{+0.19}_{-0.09}$
$\Lambda_c^+ \rightarrow p \eta'$	$(5.42^{+1.47}_{-1.32}) \times 10^{-4}$	$-0.34^{+0.25}_{-0.24}$	$-0.94^{+0.06}_{-0.12}$	$0.05^{+0.26}_{-0.25}$
$\Lambda_c^+ \rightarrow \Lambda^0 K^+$	$(5.89^{+3.52}_{-2.78}) \times 10^{-4}$	$-0.57^{+0.45}_{-0.32}$	$0.23^{+0.49}_{-0.54}$	$-0.78^{+0.43}_{-0.25}$
$\Lambda_c^+ \rightarrow \Sigma^0 K^+$	$(4.80^{+2.95}_{-2.31}) \times 10^{-4}$	$-0.62^{+0.47}_{-0.31}$	$0.25^{+0.51}_{-0.58}$	$-0.74^{+0.46}_{-0.30}$
$\Lambda_c^+ \rightarrow n \pi^+$	$(7.30^{+4.98}_{-3.95}) \times 10^{-4}$	$-0.83^{+0.48}_{-0.27}$	$-0.01^{+0.59}_{-0.63}$	$0.56^{+0.38}_{-0.48}$
$\Lambda_c^+ \rightarrow \Sigma^+ K_S$	$(3.68^{+1.06}_{-0.91}) \times 10^{-4}$	$-0.87^{+0.20}_{-0.11}$	$-0.00^{+0.26}_{-0.27}$	$-0.49^{+0.27}_{-0.24}$
$\Lambda_c^+ \rightarrow p \pi^0$	$(0.32^{+2.22}_{-1.31}) \times 10^{-4}$	$-0.25^{+0.70}_{-0.65}$	$-0.30^{+0.71}_{-0.67}$	$0.92^{+0.70}_{-0.65}$
$\Xi_c^0 \rightarrow \Xi^- \pi^+$	$(1.61^{+0.61}_{-0.50}) \times 10^{-2}$	$-0.64^{+0.34}_{-0.26}$	$-0.68^{+0.33}_{-0.23}$	$-0.36^{+0.32}_{-0.27}$
$\Xi_c^0 \rightarrow \Xi^- K^+$	$(0.23^{+0.11}_{-0.09}) \times 10^{-3}$	$-0.14^{+0.48}_{-0.44}$	$0.00 \pm 0.00$	$-0.99^{+0.19}_{-0.05}$
$\Xi_c^0 \rightarrow \Lambda^0 K_S$	$(0.85^{+2.03}_{-1.34}) \times 10^{-3}$	$-0.05^{+0.71}_{-0.62}$	$-0.44^{+0.75}_{-0.54}$	$-0.90^{+0.72}_{-0.55}$
$\Xi_c^0 \rightarrow \Sigma^0 K_S$	$(0.71^{+1.83}_{-1.20}) \times 10^{-3}$	$-0.05^{+0.72}_{-0.63}$	$-0.48^{+0.76}_{-0.54}$	$-0.88^{+0.70}_{-0.60}$
$\Xi_c^0 \rightarrow \Sigma^+ K^-$	$(1.83^{+2.24}_{-1.61}) \times 10^{-3}$	$-0.10^{+0.61}_{-0.59}$	$-0.55^{+0.66}_{-0.48}$	$0.83^{+0.34}_{-0.60}$
$\Xi_c^+ \rightarrow \Xi^0 \pi^+$	$(0.94^{+0.55}_{-0.39}) \times 10^{-2}$	$0.03^{+0.51}_{-0.42}$	$0.98^{+0.12}_{-0.24}$	$0.21^{+0.35}_{-0.44}$

# Summary

- Two independent fitting methods are investigated to explore the features of charmed baryon weak decays.
- In flavor symmetry framework, the  $\Xi_c$  mixing effect with identical or different mixing angles is studied both in flavor symmetry keeping or breaking cases.
- The data prefer the symmetry breaking case.
- The identical mixing angle is fitted to be  $6.88^\circ$ .
- In our TDA approach, the case without  $E_3$  is more preferred.
- More observables, including transverse decay asymmetries, can be predicted in TDA.
- Decays involving  $\Lambda^0/\Sigma^0$  can not be fitted well, requiring a further study.